



## What are the uses of a nullstream?

- 1) Estimation of instrument-noise PSD
- 2) Detector calibration
- 3) GW detection in the presence of non-Gaussian noise
- 4) CBC parameter estimation (?)
- 5) Stochastic searches



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## ET Nullstream vs Network Nullstream

- 1) ET nullstream (in contrast to a network nullstream)
  - a) also works in the simultaneous presence of many GW signals;
  - b) is not affected by changing source directions (like in the case of BNS observations due to Earth rotation).
- 2) Dependence of network nullstream on source-direction estimates poses a significant limitation (e.g., see glitch vetoing slide)



## **Estimation of PSD of Instrument Noise**

### Binary neutron stars (800,000 mergers per year)

Time segment	Number of BNS contributing energy above 2Hz
1 minute	100
10 minutes	300
1 hour	500
4 hours	800
24 hours	2500

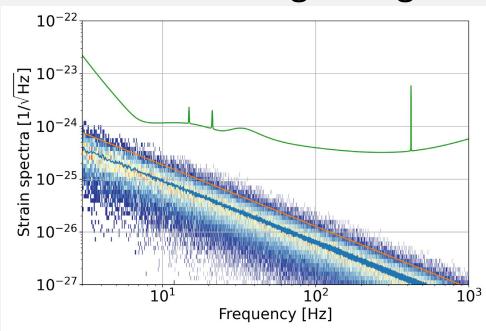
## Binary black holes (100,000 mergers per year)

Time segment	Number of BBH contributing energy above 2Hz
1 minute	2
24 hours	300

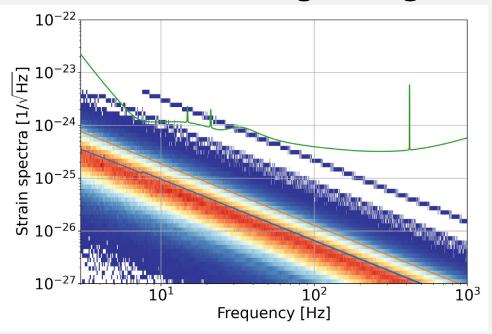


# **Astrophysical Foreground: BNS**

# 24 hours PSD/FFT time 100 PSDs forming histogram



# 1 min PSD/FFT time 7200 PSDs forming histogram

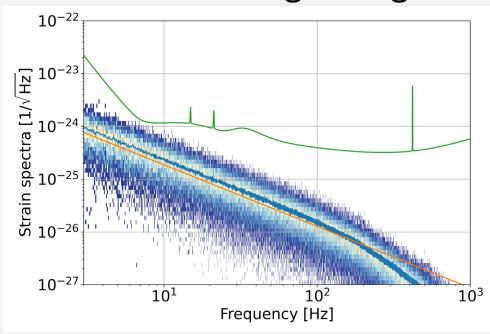


It seems that there is no significant impact of BNS foreground on estimates of instrument-noise PSDs.

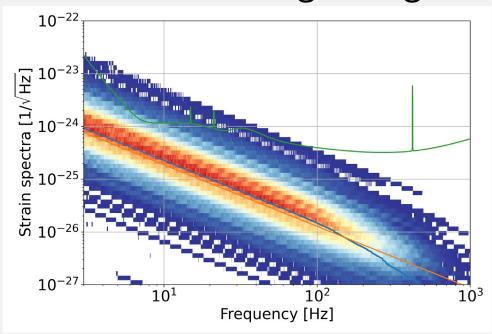


# **Astrophysical Foreground: BBH**

# 24 hours PSD/FFT time 100 PSDs forming histogram



# 1 min PSD/FFT time 7200 PSDs forming histogram



BBH signals can be expected to significantly perturb estimates of instrument-noise PSDs.



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### ET Nullstream for PSD Estimates

Data from k=1,2,3 ET components as sum of GW signal and noise

$$d_k(t) = s_k(t) + n_k(t)$$

Definition of nullstream

$$N(t) = d_1(t) + d_2(t) + d_3(t) = n_1(t) + n_2(t) + n_3(t)$$

Instrument noise PSD obtained as cross-correlation with nullstream

$$\langle n_k | n_k \rangle = \langle d_k | N \rangle$$



### **Detector Calibration**

#### Self-calibration of Networks of Gravitational Wave Detectors

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**Basic idea**: construct matched filter to detect residuals of GW signals in the nullstream. The filter provides information about calibration errors.

### Calibration errors

Required for network nullstreams

$$\tilde{N}^{123} = \tilde{N}_{\rm n}^{123} + \sum_{a} A^{(a)} c^{(a)}(f) [F_{+}^{(a)} \tilde{h}_{+}(f) + F_{\times}^{(a)} \tilde{h}_{\times}(f)] e^{2\pi i f \tau^{a}}$$

- Nullstream residuals are low SNR (since calibration errors are small). So, one needs to combine analyses of many CBC signals to obtain useful information about calibration errors.
- 2) Absolute calibration can in principle be achieved with one detector being accurately calibrated at one frequency, or with accurate source-distance estimates, e.g., from EM counterparts.



# **Optimal GW Searches Using the Nullstream**

- 1) With nullstream, it is in principle sufficient to see the GW signal in only one detector (instead of requiring coincident detections).
- 2) Reject transients if they appear in the nullstream. ET superior to 3-detector network: since the nullstream does not depend on GW direction, weaker glitches can be vetoed.
- 3) In ET, efficiency of glitch veto limited by calibration errors (calibration errors can cause glitches not to be vetoed).

Coherent network analysis technique for discriminating gravitational-wave bursts from instrumental noise

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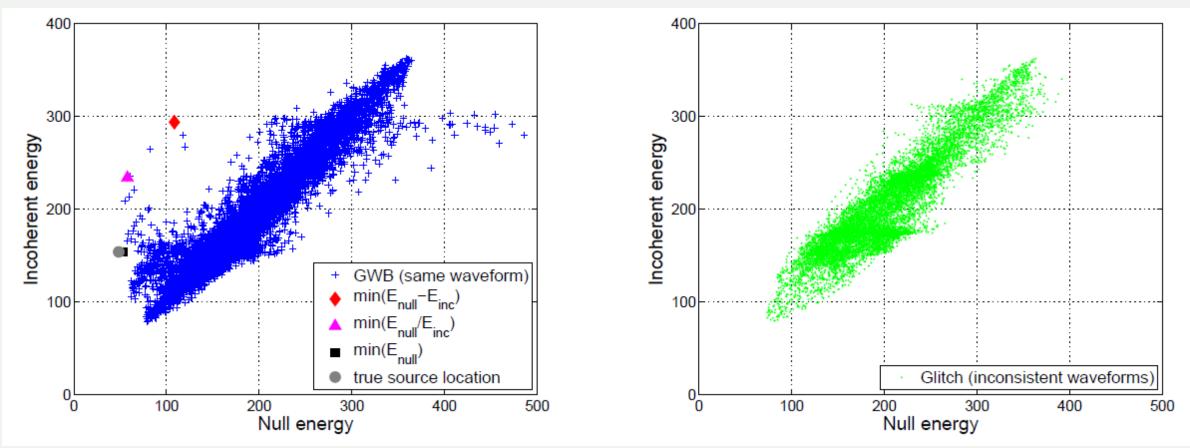
Jet Propulsion Laboratory, California Institute of Technology, Pasadena, CA 91109

(Dated: October 30, 2018)



# **Glitch Vetoing**

Each point in these plots is a trial sky location to construct a network nullstream.



Analgous study for ET under way (Goncharov, Nitz).



# **Nullstream and CBC Parameter Estimation**

#### Null-stream-based Bayesian Unmodeled Framework to Probe Generic Gravitational-wave Polarizations

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Explicitly shown in Wong et al, nullstream does not help for CBC PE if noise is Gaussian.

What if a relatively weak glitch perturbs a GW signal? Can you faithfully subtract it without nullstream? If not, how would such a glitch PE?



### **Stochastic GW Searches**

### **Auto-correlation**

$$\rho = \sqrt{T} \left[ \int_0^\infty df \, \frac{\mathcal{R}^2(f) S_h^2(f)}{P_n^2(f)} \right]^{1/2}$$

Requires estimate of instrumentnoise PSD, which can be affected by calibration errors.

### **Cross-correlation**

$$\rho = \sqrt{2T} \left[ \int_{f_{\min}}^{f_{\max}} df \, \frac{\Gamma_{IJ}^2(f) S_h^2(f)}{P_{nI}(f) P_{nJ}(f)} \right]^{1/2}$$

GW cross-PSD typically significantly reduced across two different interferometers compared to the GW PSD.

Both stochastic searches are limited by instrument-noise correlations.

Sensitivity curves for searches for gravitational-wave backgrounds

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