

Report on  
collection of  
EoS to be used  
for injections

A Sedrakian

Current  
astrophysical  
constraints

Equation of  
state of dense  
matter

Phase transition  
to quark matter

# Report on collection of EoS to be used for injections

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FIAS (Frankfurt) and IFT (Wroclaw University)

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FIAS Frankfurt Institute  
for Advanced Studies



Uniwersytet  
Wrocławski

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## CDF based equations of states

- Using EoS in a form of density functional: the pressure of dense zero-temperature matter is a functional of energy-density:  $P(\varepsilon(r))$ .
  - The parameters of the functional are adjusted to the available data (astrophysics, laboratory and ab initio calculations)
  - DFT has been extended to baryon octet and includes hyperons and Delta-resonances
  - Fast in implementation to generate quickly families of EoS
- 
- **Relativistic models of nuclear matter as DFT:**
    - (a) relativistic covariance, causality is fulfilled (+)
    - (b) The Lorentz structure of interactions is maintained explicitly (+)
    - (c) straightforward extension to the strange sector and resonances (+)
    - (d) fast implementation (+)
    - (e) not a QFT in the QED/QCD sense (-)
  - **Extended to finite-temperature and iso-entropic case**  
The models are studied at  $S = \text{Const.}$  and  $Y_e = \text{Const.}$  (early stages of evolution, no significant entropy gradients in the core)
  - **Mapping of CDF onto the Taylor expansion of energy of nuclear matter**  
A family of models are generated with varying symmetry energy, its slope, etc.

## Nuclear matter Lagrangian:

$$\begin{aligned}
 \mathcal{L}_{NM} = & \underbrace{\sum_B \bar{\psi}_B \left[ \gamma^\mu \left( i\partial_\mu - g_{\omega BB} \omega_\mu - \frac{1}{2} g_{\rho BB} \boldsymbol{\tau} \cdot \boldsymbol{\rho}_\mu \right) - (m_B - g_{\sigma BB} \sigma) \right]}_{\text{baryons}} \psi_B \\
 & + \underbrace{\frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma - \frac{1}{2} m_\sigma^2 \sigma^2 - \frac{1}{4} \omega^{\mu\nu} \omega_{\mu\nu} + \frac{1}{2} m_\omega^2 \omega^\mu \omega_\mu}_{\text{mesons}} \\
 & - \underbrace{\frac{1}{4} \boldsymbol{\rho}^{\mu\nu} \boldsymbol{\rho}_{\mu\nu} + \frac{1}{2} m_\rho^2 \boldsymbol{\rho}^\mu \cdot \boldsymbol{\rho}_\mu}_{\text{mesons}} + \underbrace{\sum_\lambda \bar{\psi}_\lambda (i\gamma^\mu \partial_\mu - m_\lambda) \psi_\lambda}_{\text{leptons}} - \underbrace{\frac{1}{4} F^{\mu\nu} F_{\mu\nu}}_{\text{electromagnetism}} ,
 \end{aligned}$$

- $B$ -sum is over the baryonic octet
- Meson fields include  $\sigma$  meson,  $\boldsymbol{\rho}_\mu$ -meson and  $\omega_\mu$ -meson
- Leptons include electrons, muons and neutrinos for  $T \neq 0$

Two types of relativistic density functionals based on relativistic Lagrangians

- linear mesonic fields, density-dependent couplings (DDME2, DD2, etc.)
- non-linear mesonic fields; coupling constant are just numbers (NL3, GM1-3, etc.)

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constraints

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matter

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## Fixing the couplings: nucleonic sector

$$g_{iN}(\rho_B) = g_{iN}(\rho_0)h_i(x), \quad h_i(x) = a_i \frac{1 + b_i(x + d_i)^2}{1 + c_i(x + d_i)^2} \quad i = \sigma, \omega,$$

$$g_{\rho N}(\rho_B) = g_{\rho N}(\rho_0) \exp[-a_\rho(x - 1)], \quad i = \rho, (\pi - HF)$$

Meson ( $i$ )	$m_i$ (MeV)	$a_i$	$b_i$	$c_i$	$d_i$	$g_{iN}$
$\sigma$	550.1238	1.3881	1.0943	1.7057	0.4421	10.5396
$\omega$	783	1.3892	0.9240	1.4620	0.4775	13.0189
$\rho$	763	0.5647				7.3672

$h_i(1) = 1$ ,  $h_i''(0) = 0$  and  $h_i''(1) = h_i''(1)$ , which reduce the number of free parameters to three in this sector.

- DD-ME2 parametrization, G. Lalazissis, et al., Phys. Rev. **C71**, 024312 (2005)
- DD2 parametrizations, S. Typel, Eur. Phys. J. **A52**, 16 (2016)
- DD-ME2+LQ parametrizations, J. J. Li, Sedrakian, Phys. Rev. **C100**, 015809 (2019)

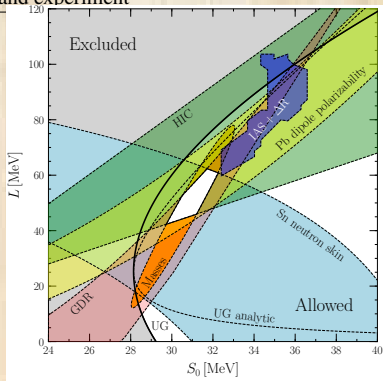
## Taylor expansion of nuclear energy

$$E(\chi, \delta) \simeq E_0 + \frac{1}{2!} K_0 \chi^2 + \frac{1}{3!} Q_{\text{sym}} \chi^3 + E_{\text{sym}} \delta^2 + L \delta^2 \chi + \mathcal{O}(\chi^4, \chi^2 \delta^2), \quad (1)$$

where  $\delta = (n_n - n_p)/(n_n + n_p)$  and  $\chi = (\rho - \rho_0)/3\rho_0$ .

## Consistency between the density functional and experiment

- saturation density  
 $\rho_0 = 0.152 \text{ fm}^{-3}$
- binding energy per nucleon  
 $E/A = -16.14 \text{ MeV}$ ,
- incompressibility  
 $K_{\text{sat}} = 251.15 \text{ MeV}$ ,
- skewness  $Q_{\text{sat}} = 479$
- symmetry energy  
 $E_{\text{sym}} = 32.30 \text{ MeV}$ ,
- symmetry energy slope  
 $L_{\text{sym}} = 51.27 \text{ MeV}$ ,
- symmetry incompressibility  
 $K_{\text{sym}} = -87.19 \text{ MeV}$



Credit: Tews, et al ApJ, 2017

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## Consistency between the density functional with experiment and ab initio theory

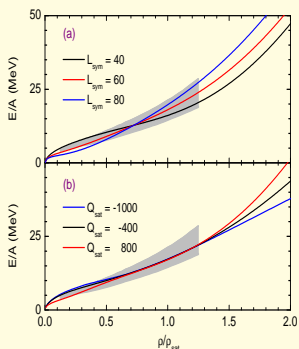
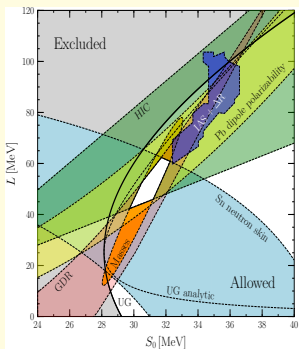
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constraints

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- Uncertainties will be quantified in terms of variation of higher-order characteristics around the central fit values.
- Low density physics depends strongly on the value of  $L_{\text{sym}}$  with strong correlation to the radius of the star and tidal deformability
- High-density physics strongly depends on the value of  $Q_{\text{sym}}$  with strong correlations to the mass of the star.

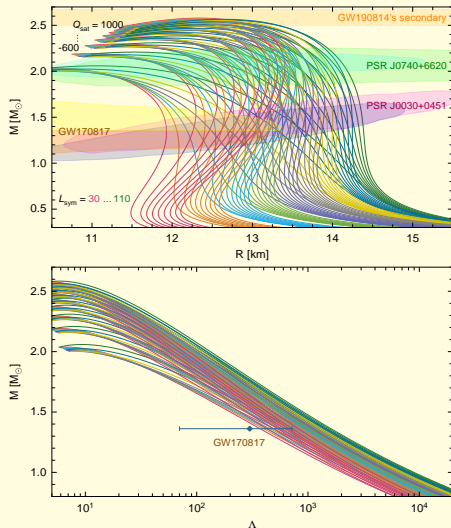
Report on  
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- Variation of  $-600 \leq Q_{\text{sat}} \leq 1000$  MeV and  $30 \leq L \leq 110$
- Computed  $9 \times 9 = 81$  matrix of EoS



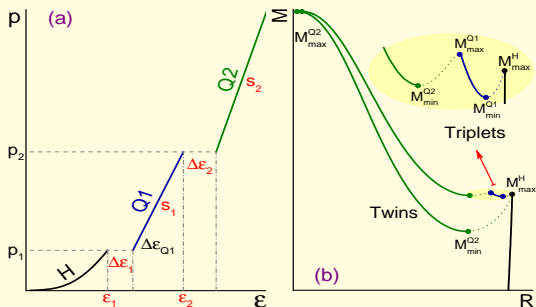
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Left: EoS with two sequential phase transitions. Right: Mass-radius relationships, emergences of minima in the function  $M(R)$ .

Case when  $NY\Delta$ -matter makes a first order phase *sequential* transitions to various *generic new phases* (we had in mind phases of color superconducting phases).

$$p(\epsilon) = \begin{cases} p_1, & \epsilon_1 < \epsilon < \epsilon_1 + \Delta\epsilon_1 \\ p_1 + s_1[\epsilon - (\epsilon_1 + \Delta\epsilon_1)], & \epsilon_1 + \Delta\epsilon_1 < \epsilon < \epsilon_2 \\ p_2, & \epsilon_2 < \epsilon < \epsilon_2 + \Delta\epsilon_2 \\ p_2 + s_2[\epsilon - (\epsilon_2 + \Delta\epsilon_2)], & \epsilon > \epsilon_2 + \Delta\epsilon_2. \end{cases}$$

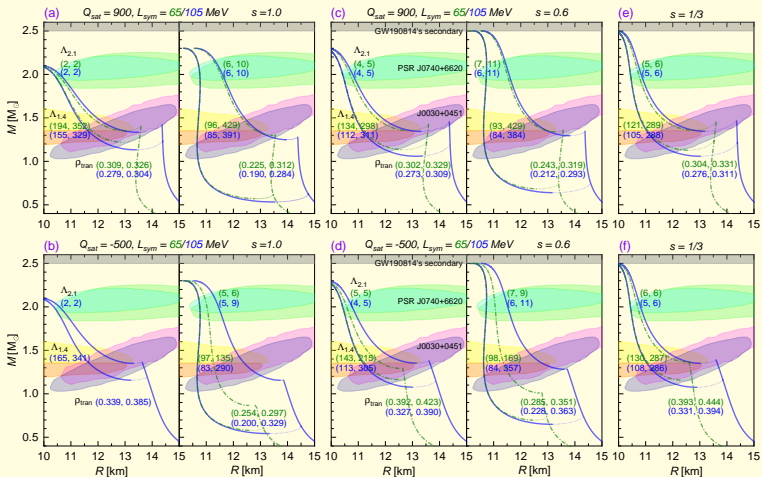
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Low-density quark-hadron phase transition case.

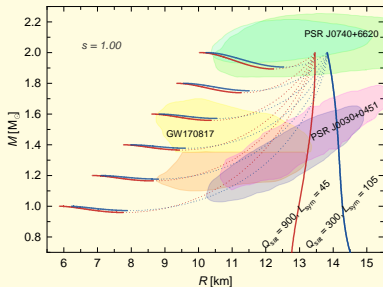
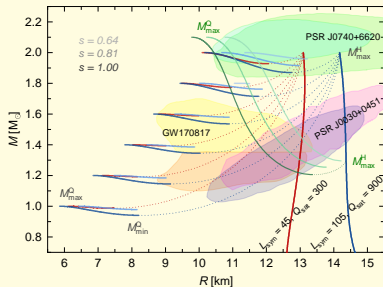
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High-density phase transition case.

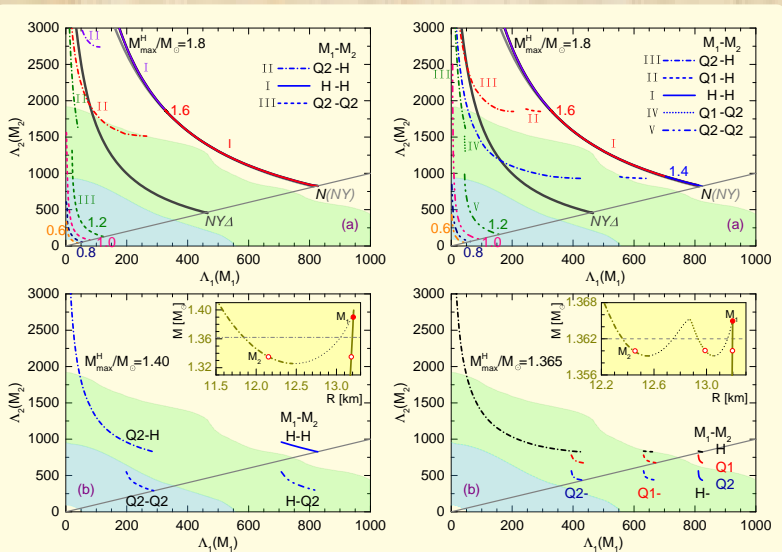
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Tidal deformabilities of compact objects with a single (left) and double (right) phase transition(s) for a fixed value of binary chirp mass  $\mathcal{M} = 1.186 M_\odot$ .

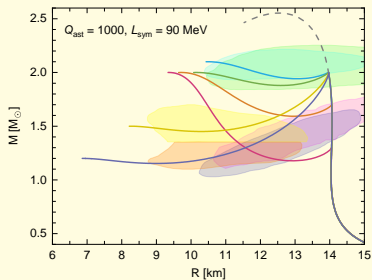
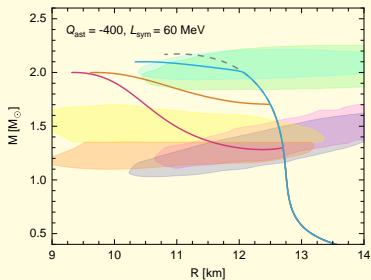
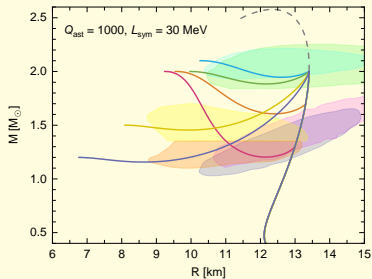
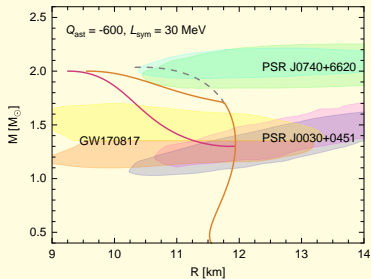
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Models available in the injection format.