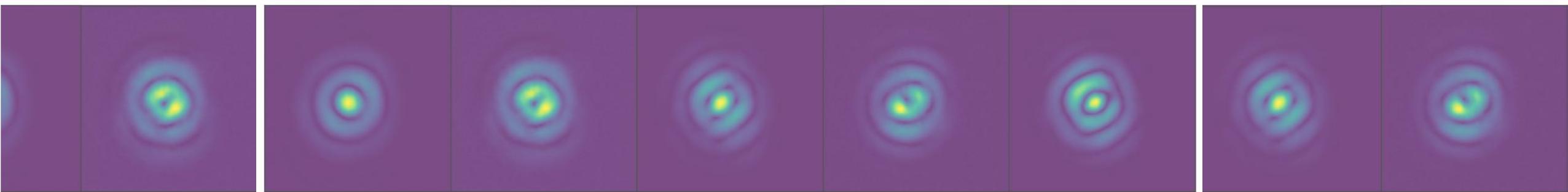


# Locked cavity scan using heterodyne detection with a phase camera



Ricardo Cabrita

Aaron Goodwin-Jones, Joris van Heijningen, Pavel Demin, Martin van Beuzekom, Matteo Tacca, Giacomo Bruno, Clement Lauzin

Bologna, ET Symposium 28 May 2025



LA LIBERTÉ DE CHERCHER



[ricardo.cabrita@uclouvain.be](mailto:ricardo.cabrita@uclouvain.be)

# Increasing circulating power in GW detectors

## Next generation detectors

Arm circ. power	CE	ET (HF)
	1.5 MW	3 MW

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actual	350 kW	96 kW

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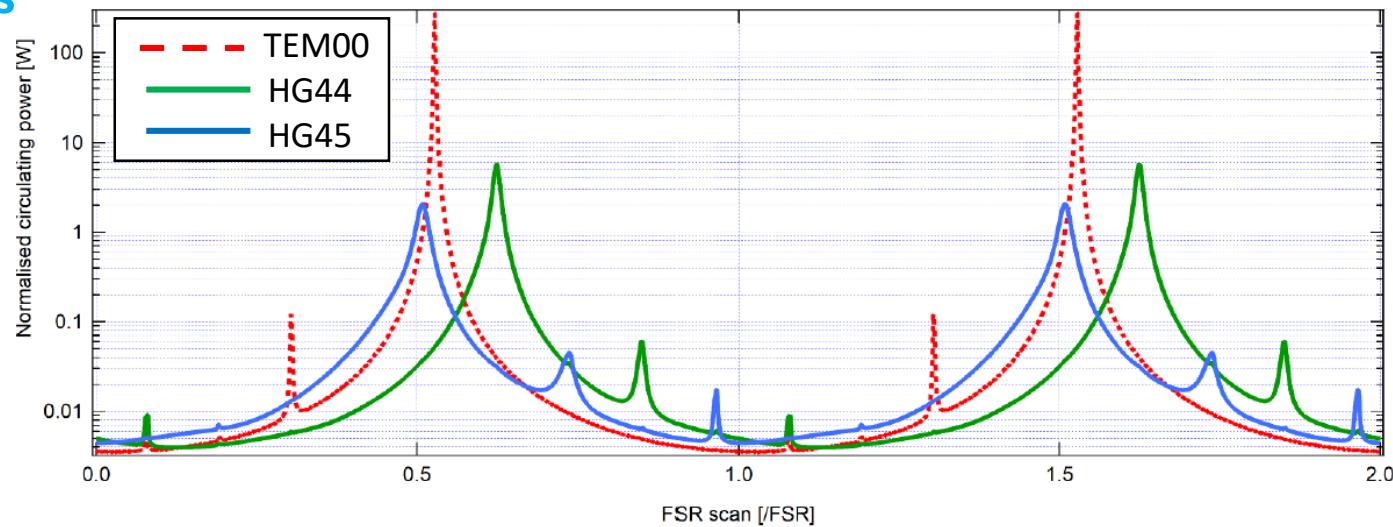
Power losses to

- scattering,
- point defects,
- ITF working point degradation – over 6 hour thermal transient in LIGO.

# (some) issues with high optical power

Thermal effects can shift the cavity eigenmodes

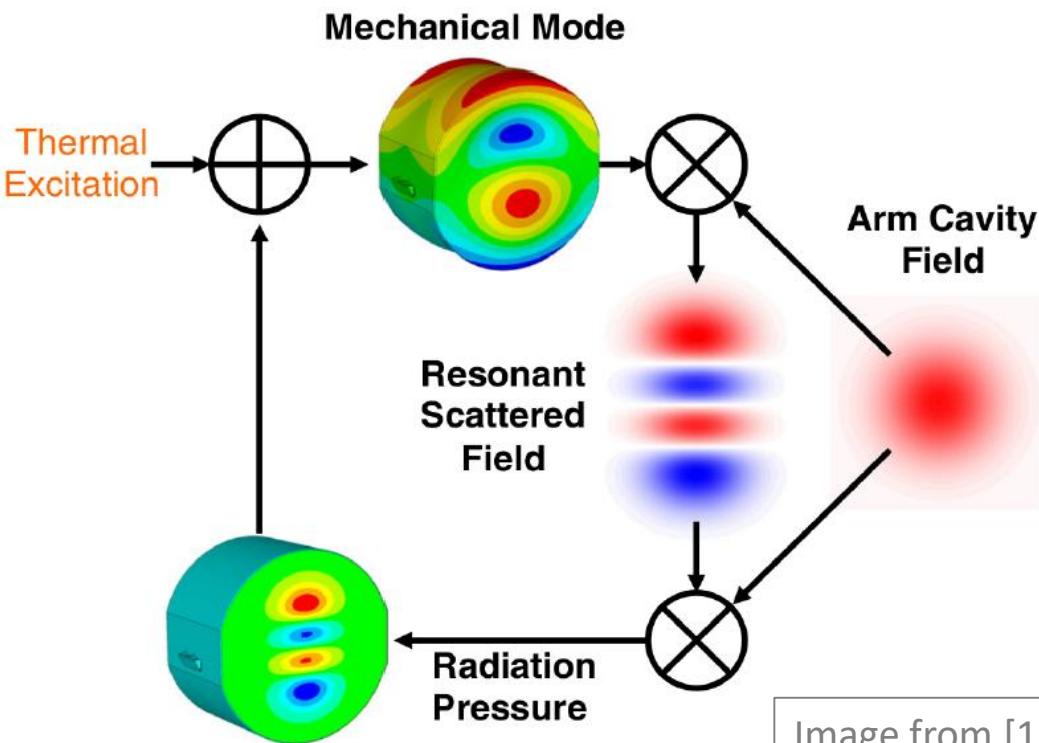
Simulation by J.  
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VIR-0831A-24



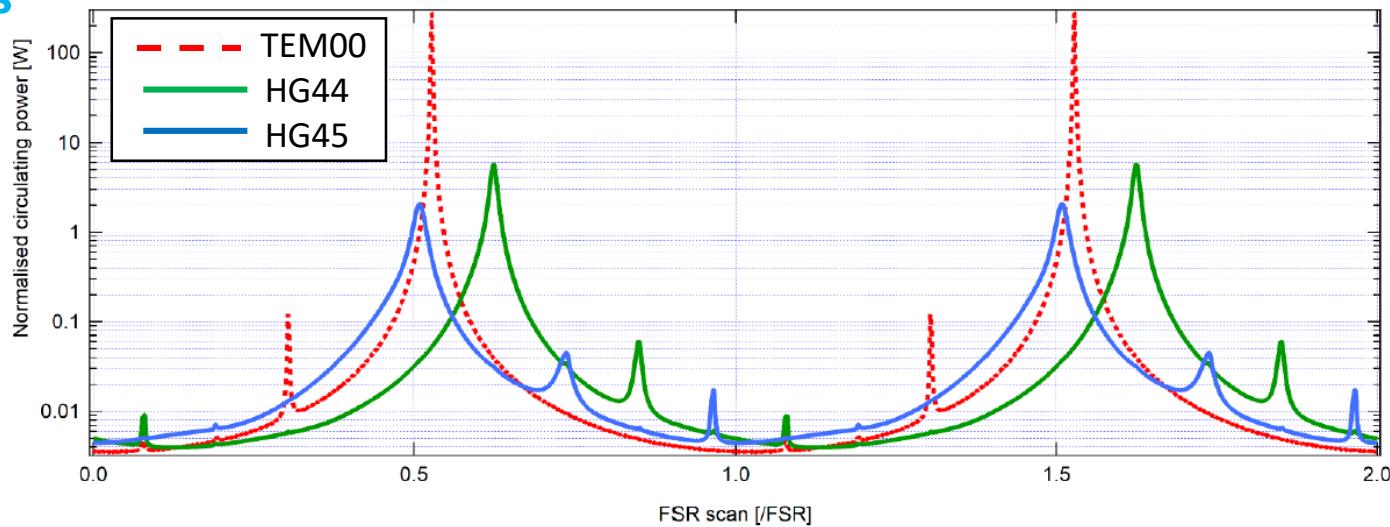
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## Parametric instabilities



Simulation by J.  
Degallaix –  
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VIR-0831A-24



high power + optical HOM overlapping with acoustic mode + radiation pressure

Suppression by injecting HOM with opposing phase (V. Bossilkov) [2]

# Cavities with high circulating power...

With continuous wave laser....

$$I = \frac{2P}{\pi w_0^2}$$

Group	Tot. Pwr. (MW)	Intensity (MW/cm <sup>2</sup> )	Waist (mm)	Application
H. Mueller:	0.14	123000	0.0085	PEM/dipole trapping
LIDA	0.124	4700	0.0285	Dark matter detection
LIGO	0.350	0.154	12	GW detection
IJClab (ps laser)	0.710	0.56	9	Extreme radiation/accelerators
Photodetachment	10	636	1	Fusion reactor – neutral beam
ET (CE)	3	0.95	14.2	GW detection

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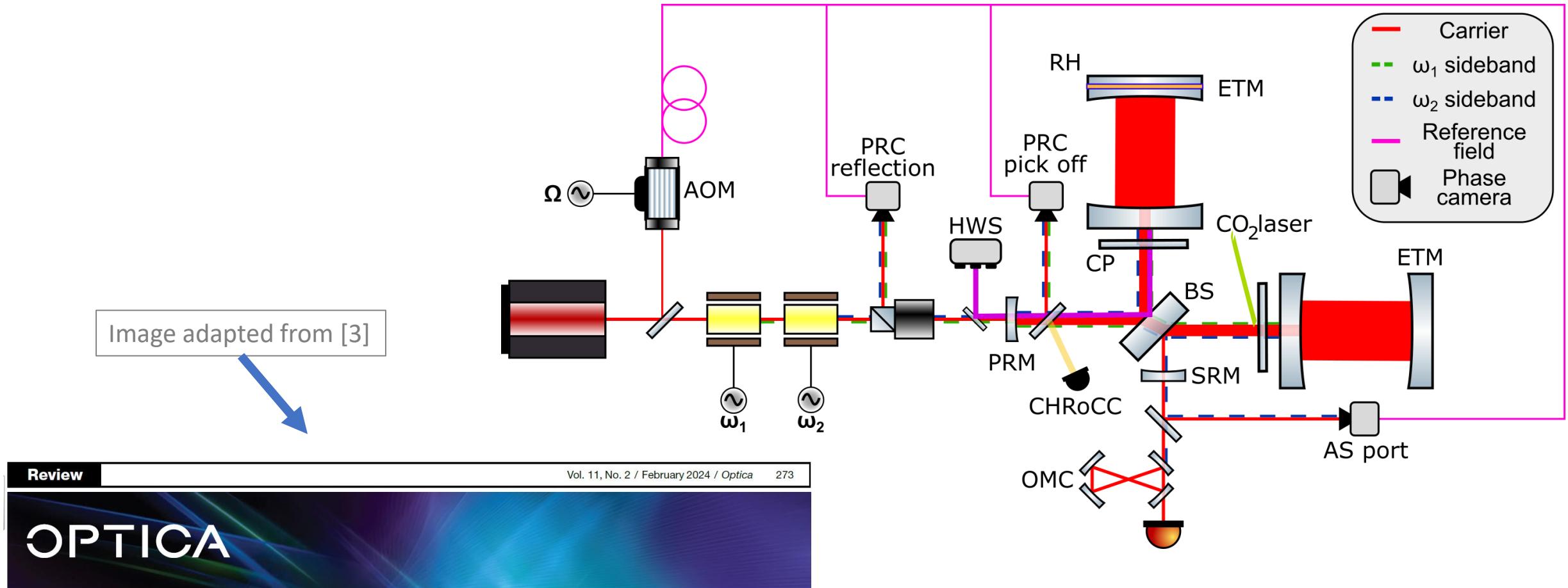
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unique to GW detection: Combination of high power with very low losses!

# Mode sensing and control in Virgo



**Transverse mode control in quantum enhanced interferometers: a review and recommendations for a new generation**

AARON W. GOODWIN-JONES,<sup>1,2,\*</sup> RICARDO CABRITA,<sup>3</sup> MIKHAIL KOROBKO,<sup>4</sup> MARTIN VAN BEUZEKOM,<sup>5</sup> DANIEL D. BROWN,<sup>1,6</sup> VIVIANA FAFONE,<sup>7,8</sup> JORIS VAN HEIJNINGEN,<sup>3</sup> ALESSIO ROCCHI,<sup>8</sup> MITCHELL G. SCHIWORSKI,<sup>1,6</sup> AND MATTEO TACCA<sup>5</sup>

- No feedback loop
- No way to online monitor thermal transient.

# Locked cavity monitoring with the phase camera

Optical injection scheme + phase camera

- Monitoring cavity g-factor while locked
- Test phase sensitive measurements of HOMs – for PI suppression of HOM of arbitrary order

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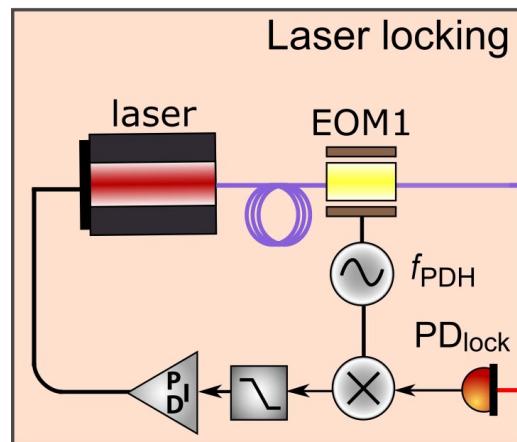
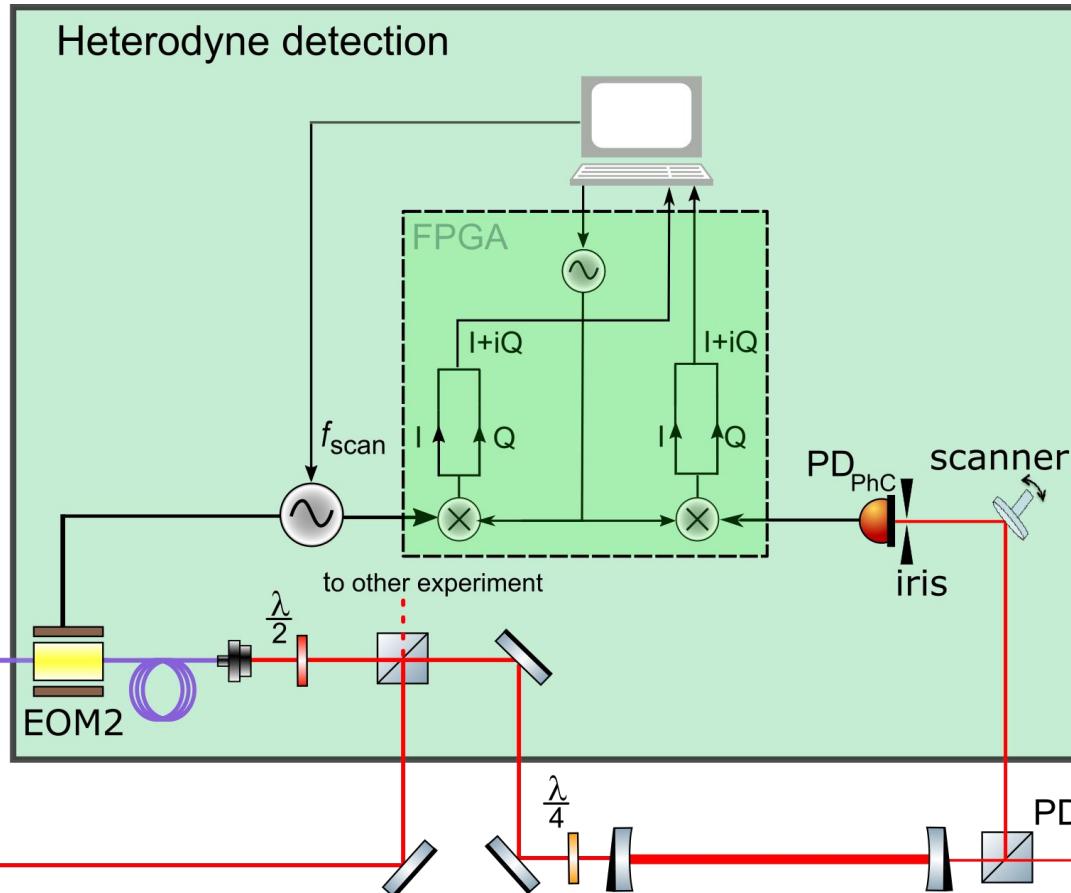


Table-top set-up at UCLouvain



- Invar bar cavity (open air)
- 32 cm, (nominal) Finesse 360

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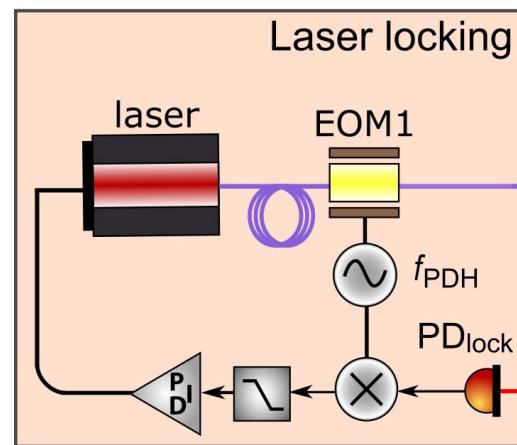
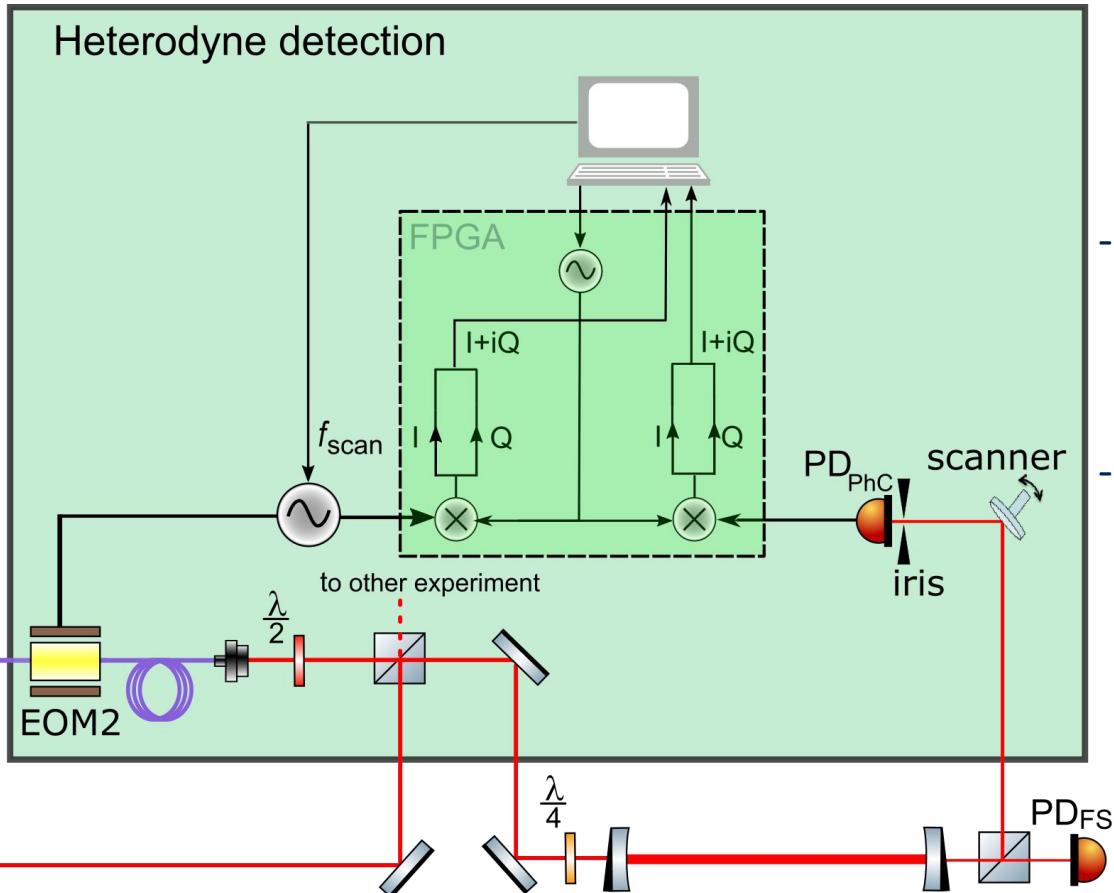


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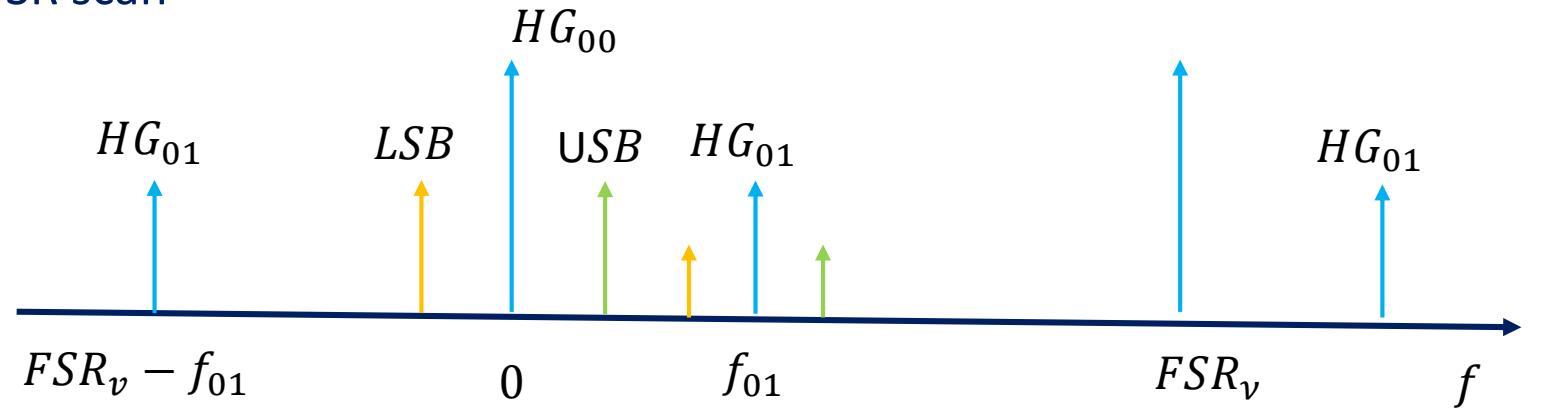
Nikhef

- Scanning EOM2 modulation frequency injects sideband HOM at key frequencies

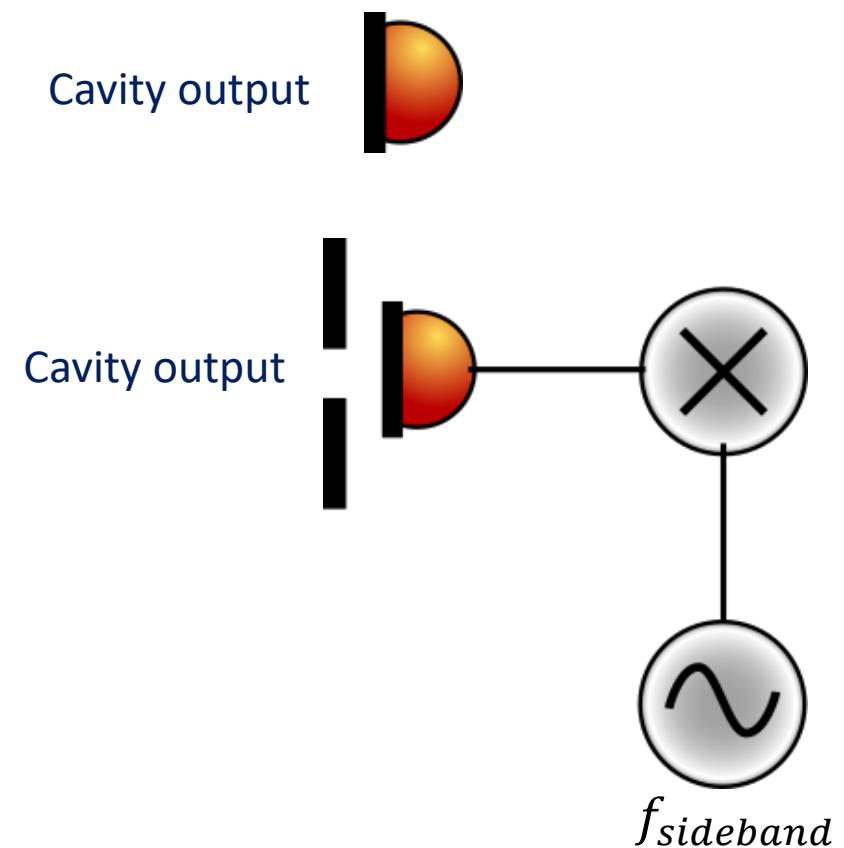
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# Sideband HOM injection with EOM

FSR scan

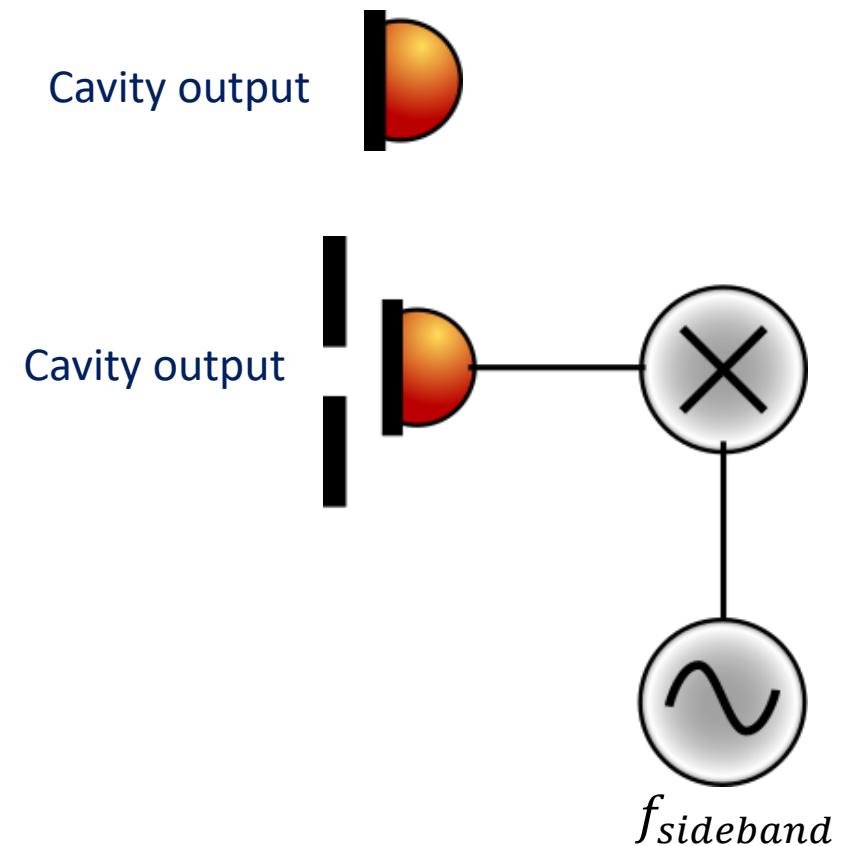
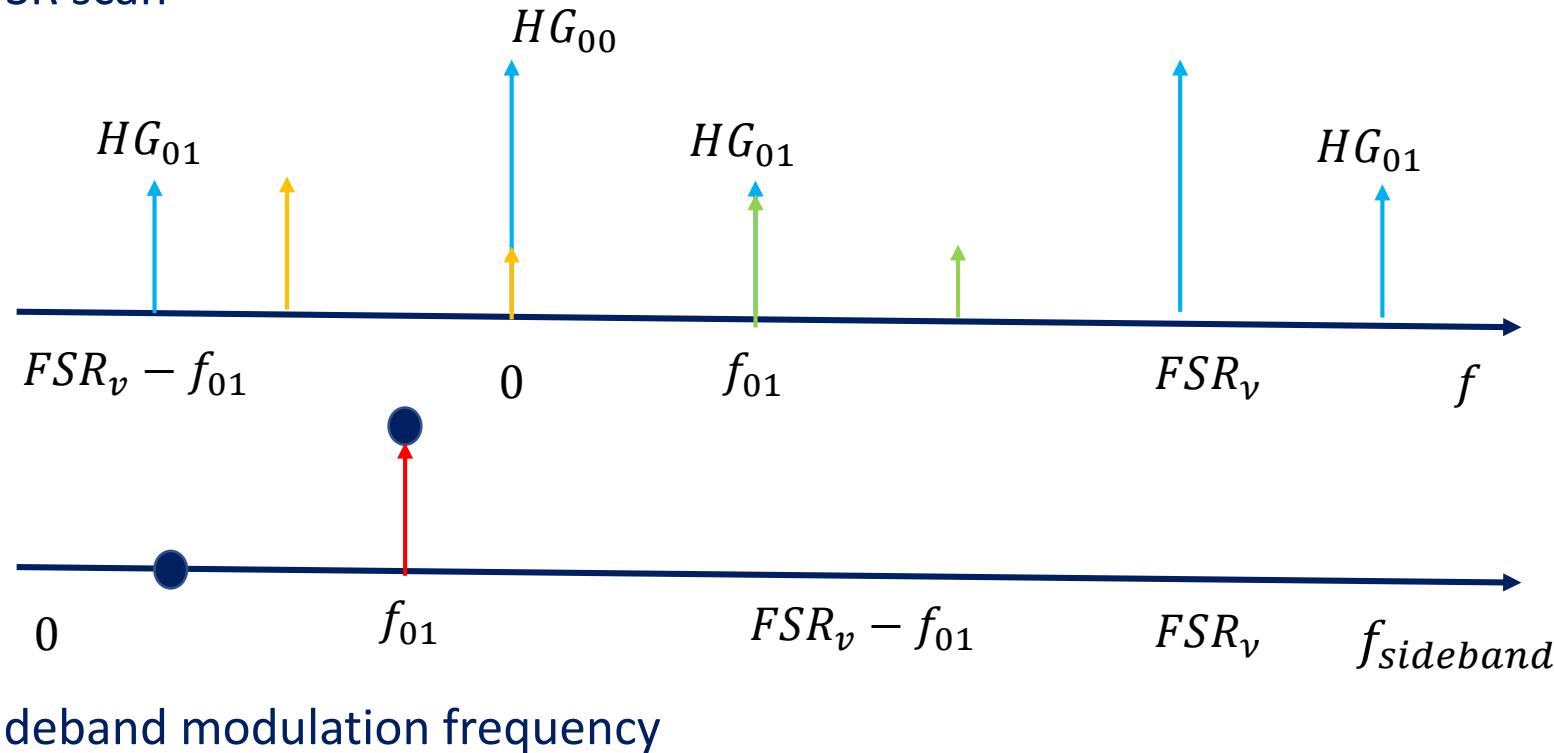


Sideband modulation frequency



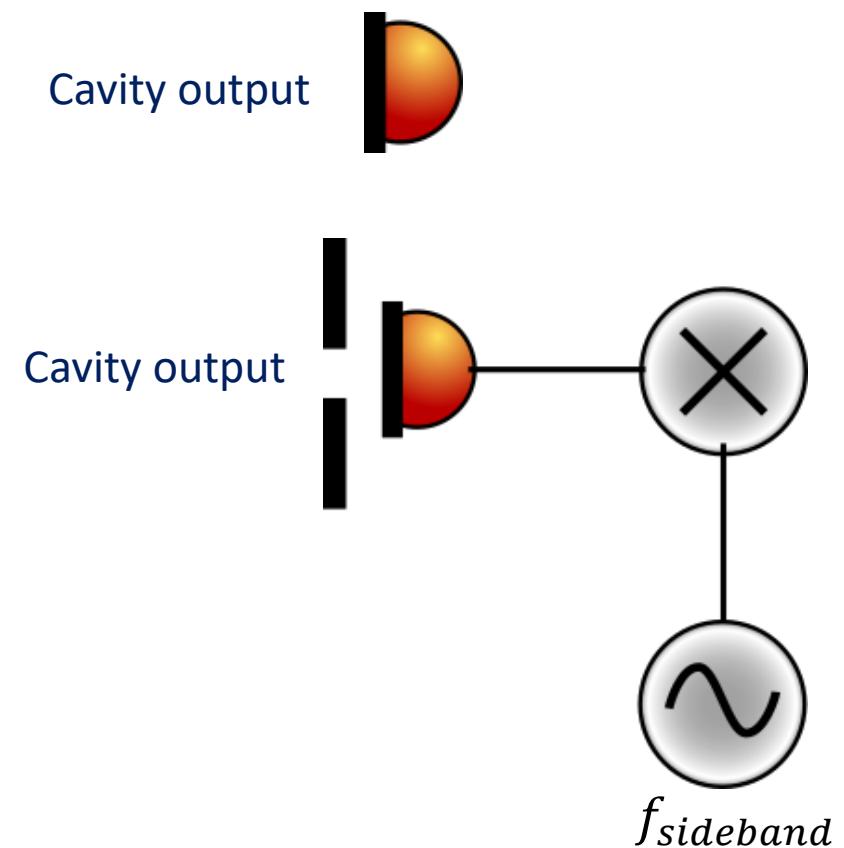
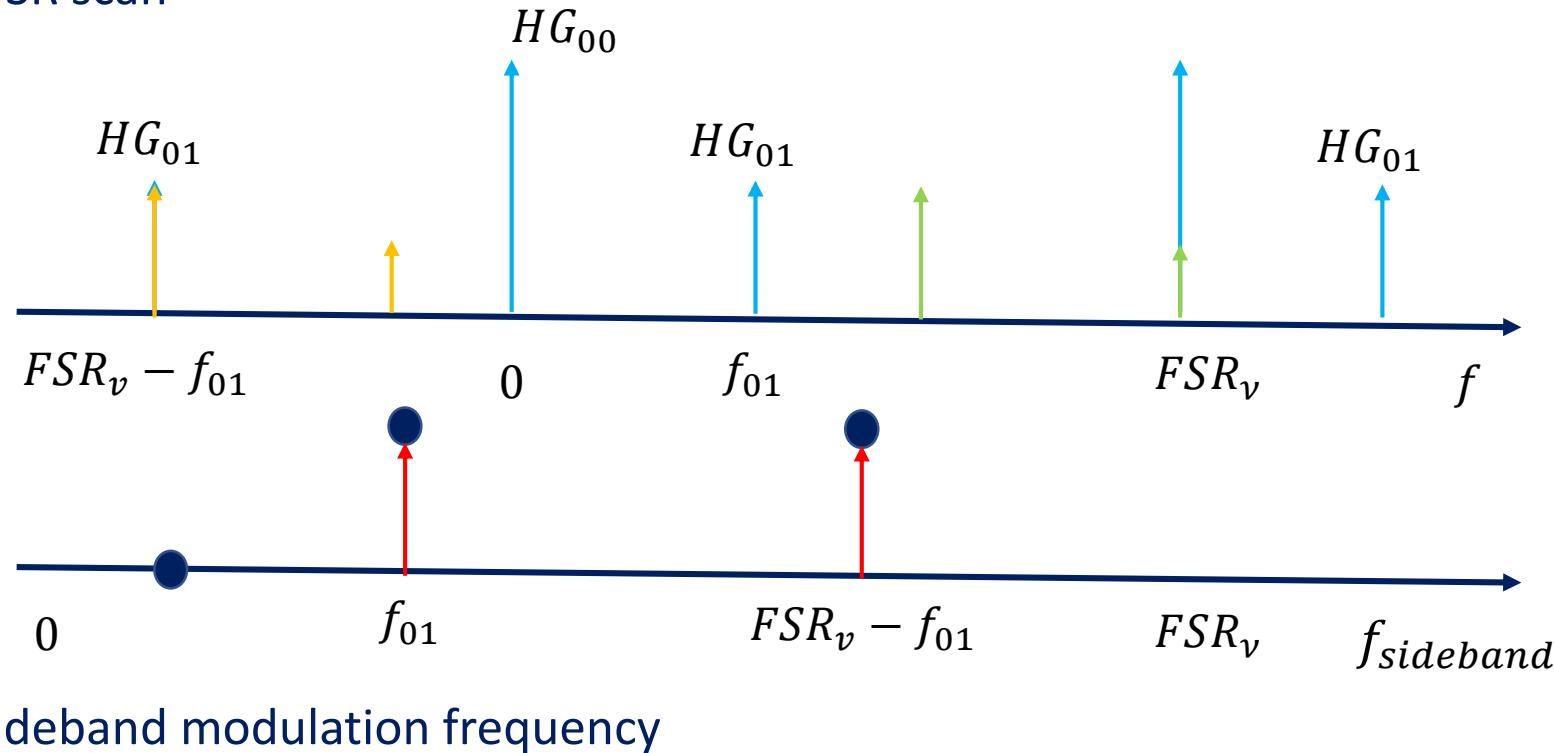
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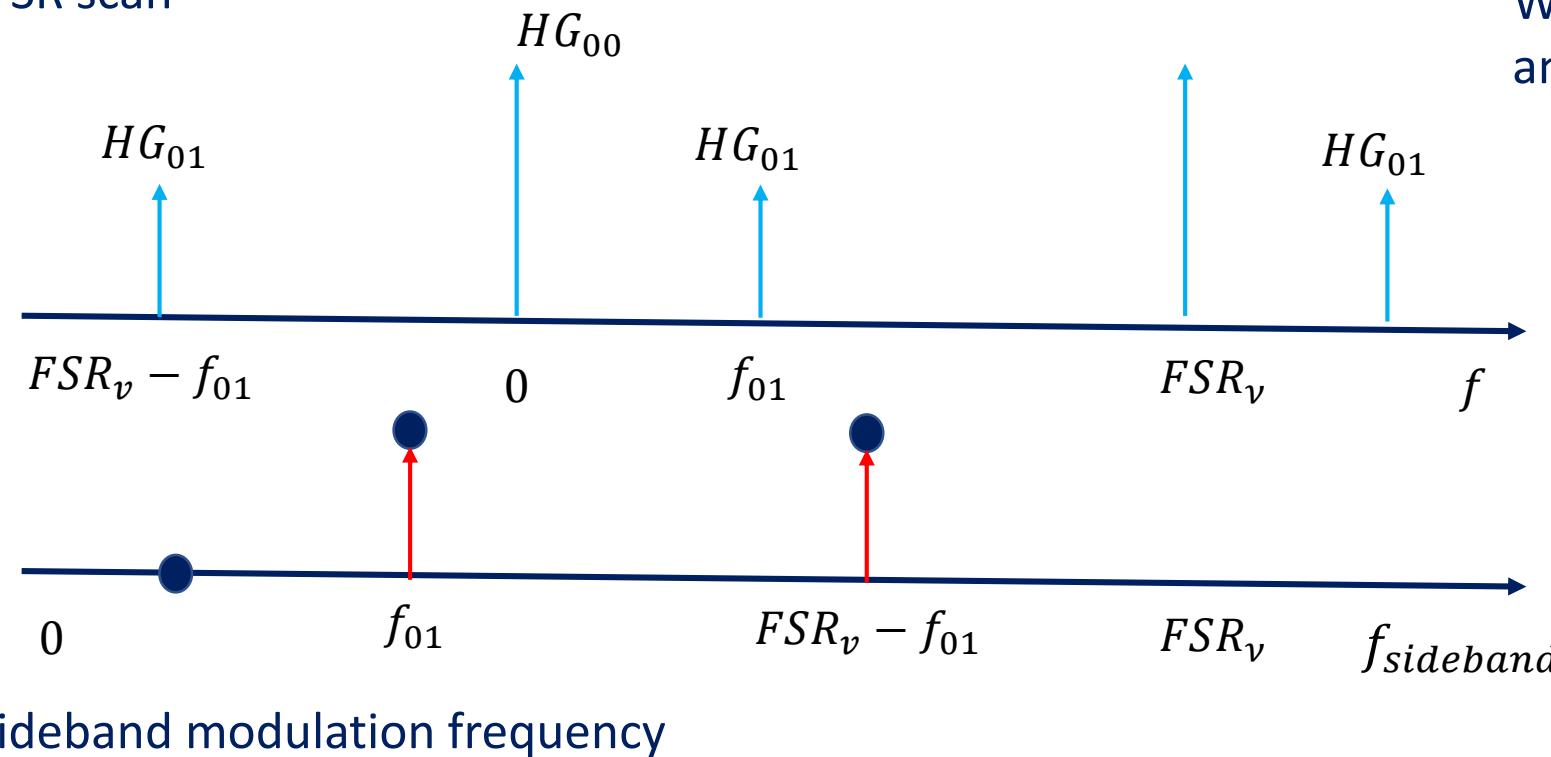
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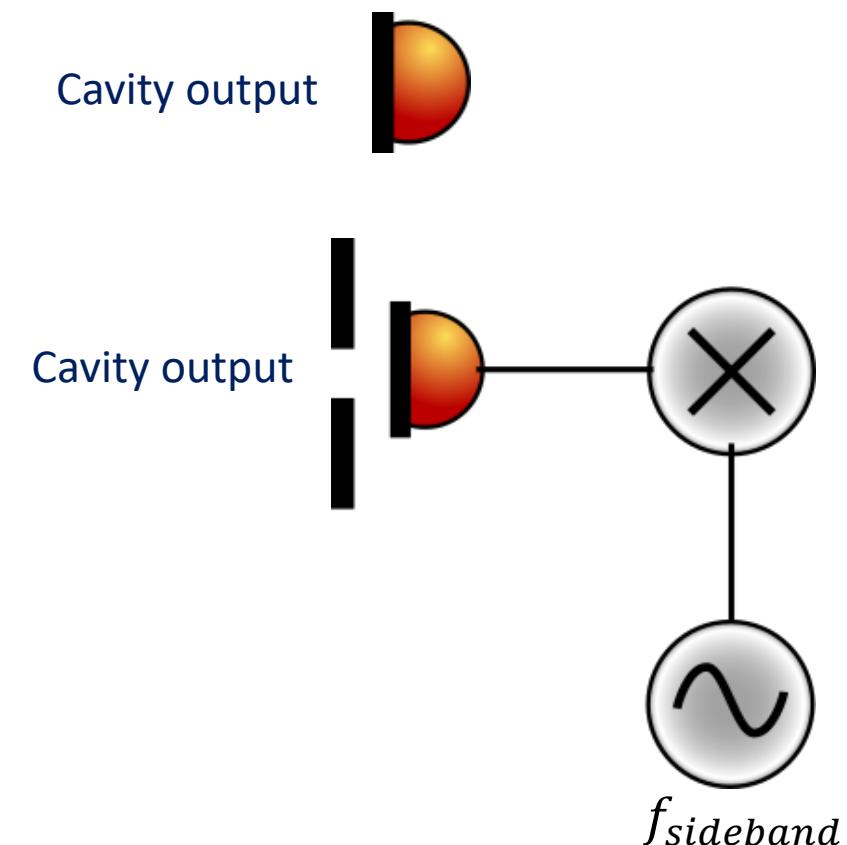


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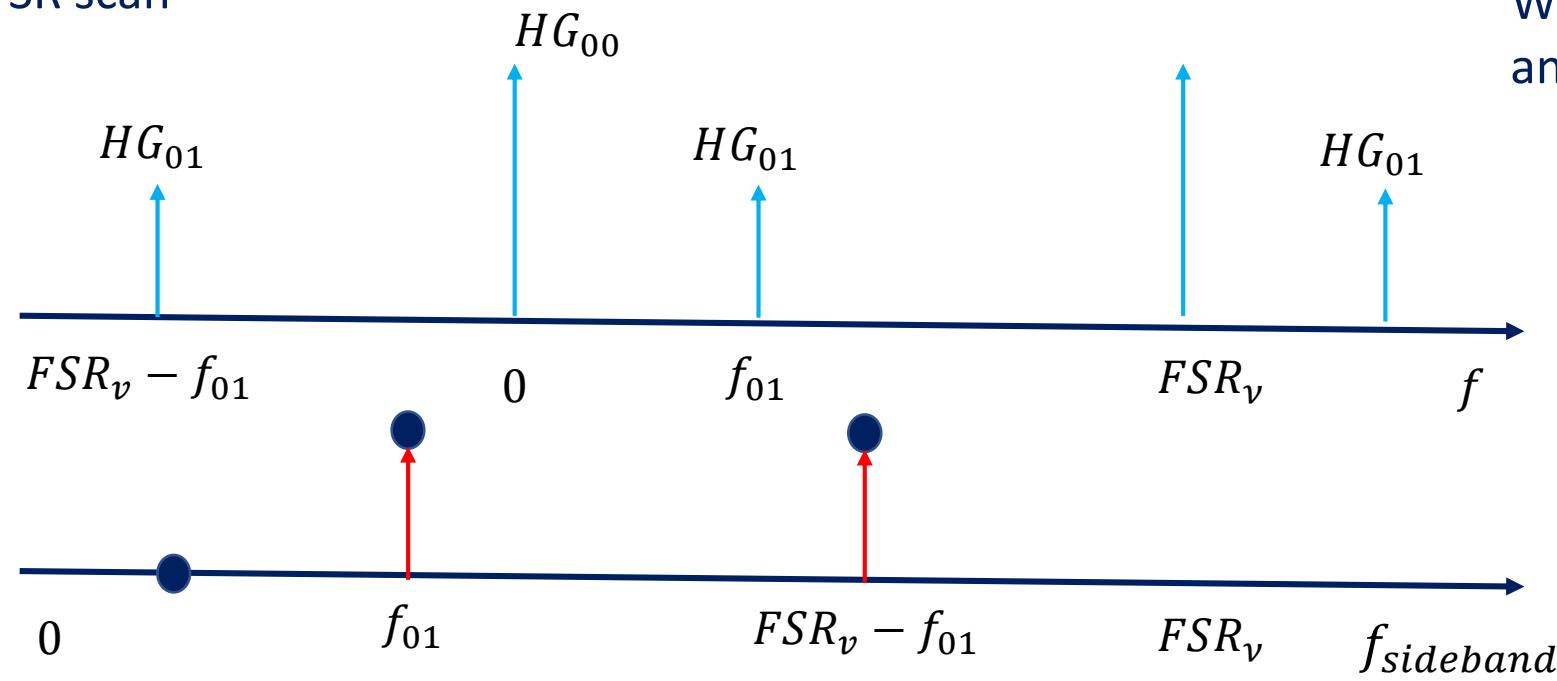


We obtain a spectrum from the LSB and another from the USB at  $FSR_v - f_{m+N}$ !

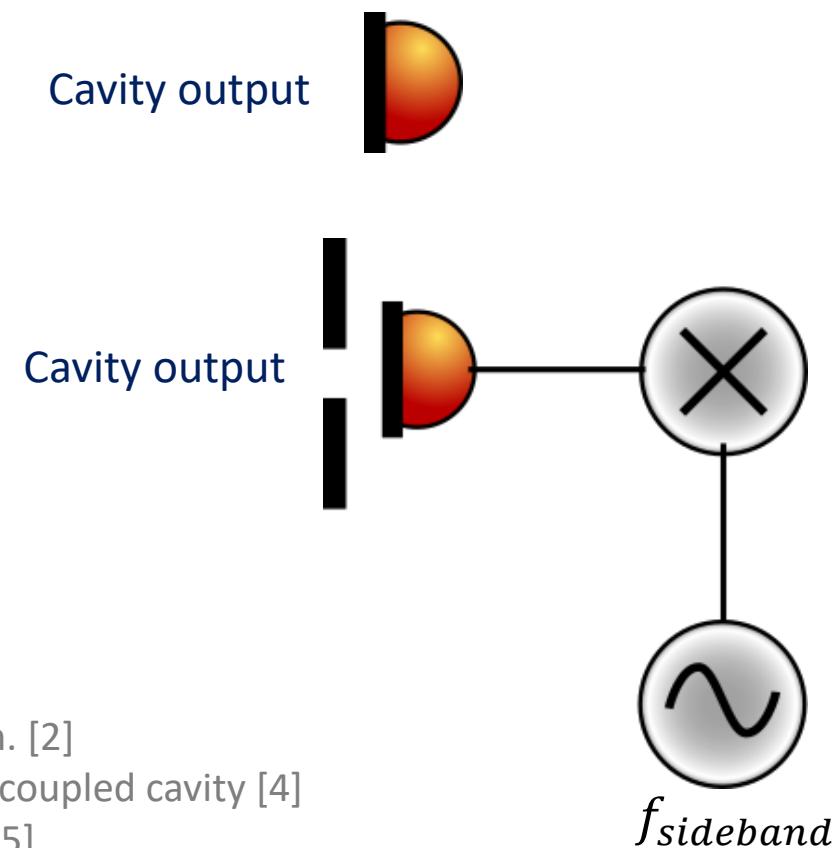


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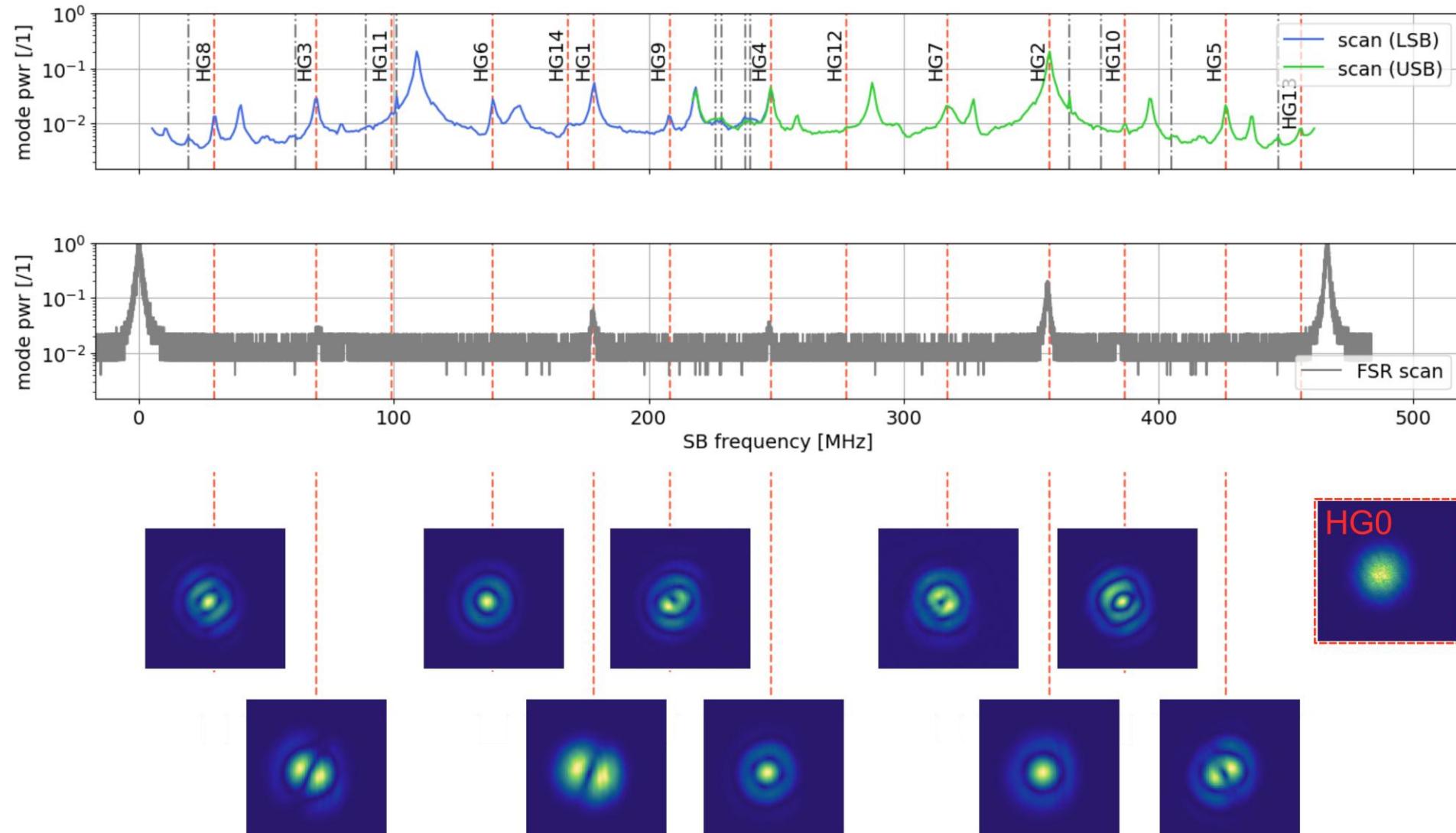


Similar sideband injection scheme

- V. Bossilkov – 1<sup>st</sup> order mode injection + QPD readout – demonstration of PI suppression. [2]
- A. Goodwin Jones – 2<sup>nd</sup> order mode injection – mode mismatch simulation of linear and coupled cavity [4]
- M. Beaumont and D. Romanini - EOM scan, and blade + photodiode for v-shaped cavity [5]
- O. Schwartz – 1<sup>st</sup> order mode injection to characterize cavity concentricity (phase-contrast electron microscopy) [6]

# Heterodyne scan results

Acquisition limited to 250 MHz but cavity FSR is 467 MHz – LSB probes first half of FSR and USB probes second half of FSR



# Cavity g-factor measurement while locked

Fit mode positions for LSB:

$$f_{LSB}(m + n) = \text{FSR}_v \frac{m + n}{\pi} \arccos(1 - L/\text{RoC})$$

Fit mode positions for USB

$$f_{USB}(m + n) = \text{FSR}_v - \text{FSR}_v \frac{m + n}{\pi} \arccos(1 - L/\text{RoC})$$

## Mode fitting results....

Mirror RoC  $0.501992 \pm 0.000070$  m

Cavity length  $0.321518 \pm 0.000030$  m

Cavity FSR  $466.213 \pm 0.043$  MHz

Cavity g-factor  $0.35951 \pm 0.00017$  MHz

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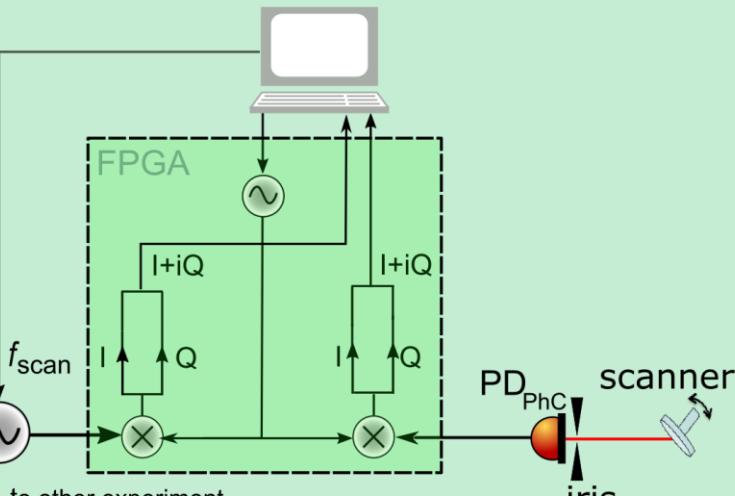
Different modes experience different round-trip losses (RTL):

- can be exploited to make RTL map.

	FWHM [MHz]	RTL [%]
	$1.75 \pm 0.07$	0.66
	$1.83 \pm 0.08$	0.77
	$1.57 \pm 0.09$	0.42
	$1.68 \pm 0.16$	0.57
	$1.74 \pm 0.26$	0.64
	$1.74 \pm 0.044$	0.65
	$1.76 \pm 0.046$	0.67
	$1.70 \pm 0.083$	0.60

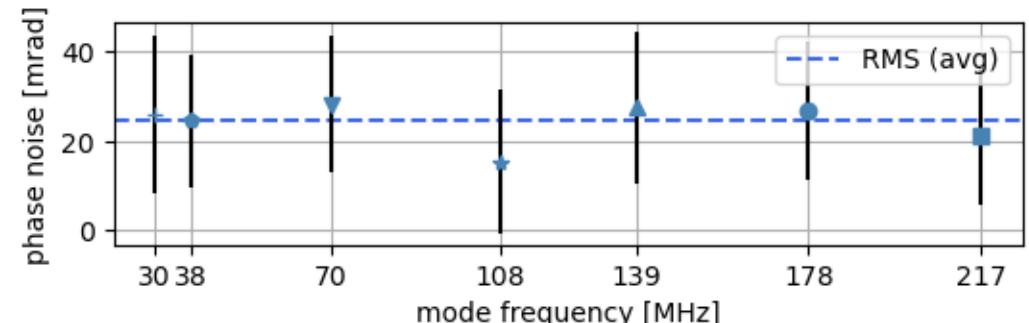
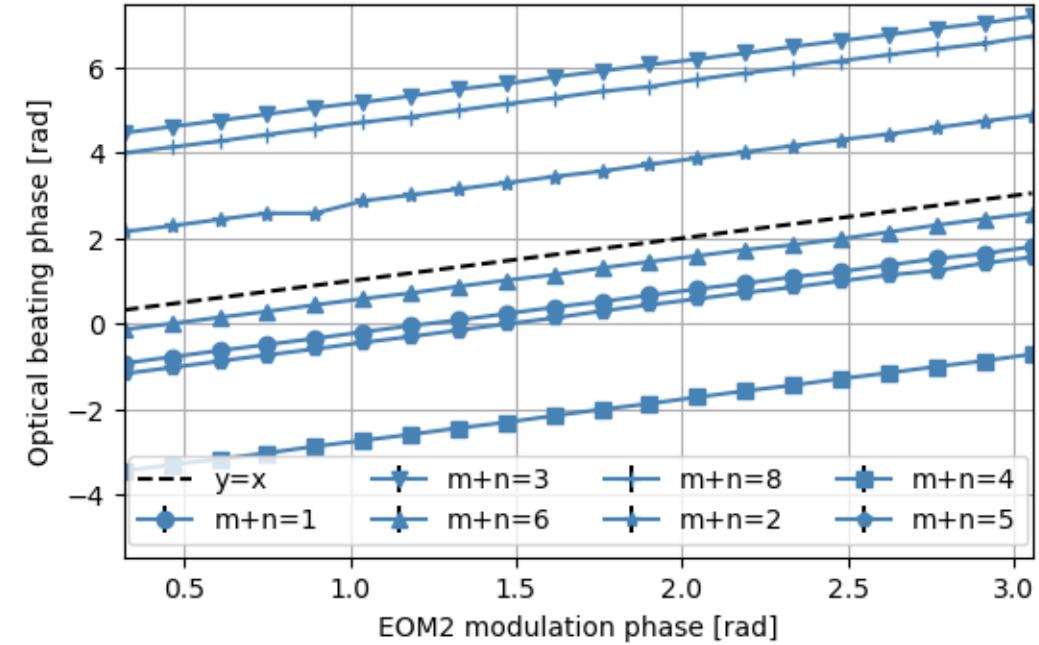
# Phase sensitive measurements

Heterodyne detection



- Phase of EOM2 modulating sine is swept.
  - Phase camera retrieves optical beating phase between carrier and sideband HOM –  $\arctan(Q/I)$
- Phase camera can be used for PI suppression of arbitrary HOMs
- Can also be used for mode mismatch and misalignment signals in transmission

$$\Phi_{beat} = \Delta R - \Delta G + \Delta L + \Delta K + \Delta \phi_{M0}$$



# Towards the MW goal in next generation detectors

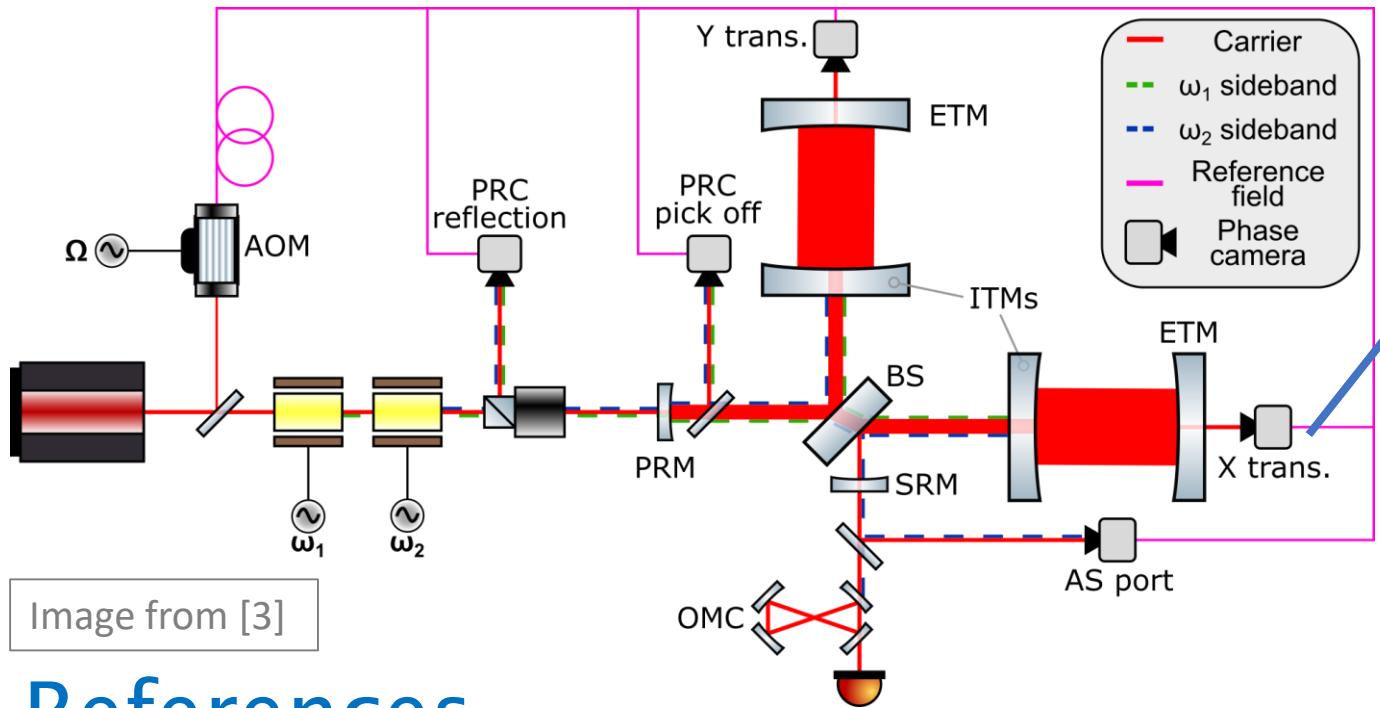


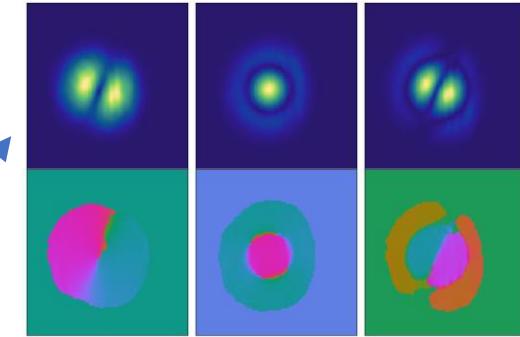
Image from [3]

## References

- [1] M. Evans et al., "Observation of parametric instability at LIGO" Phys. Rev. Lett. 114, 161102 (2015)
- [2] V. Bossilkov, Jian Liu et al., "Demonstration of the parametric instability suppression through optical feedback" Rev. D 109, 102006 (2024)
- [3] A. W. Goodwin-Jones, R. Cabrita, et al., "Transverse mode control in quantum enhanced interferometers: a review and recommendations for a new generation," Optica 11, 273-290 (2024)
- [4] A. W. Goodwin-Jones, H. Zhu, et al., "Single and coupled cavity mode sensing schemes using a diagnostic field," Opt. Express 31, 35068-35085 (2023)
- [5] M. Beaumont, I. Ventrillardet, et al., "Optical cavity spectroscopy using heterodyne detection with optical feedback laser frequency locking," Appl. Opt. 63, 2227-2233 (2024)
- [6] O. Schwartz, J. J. Axelrod, S. L. Campbell, et al., "Laser phase plate for transmission electron microscopy," Nat.methods 16, 1016–1020 (2019)

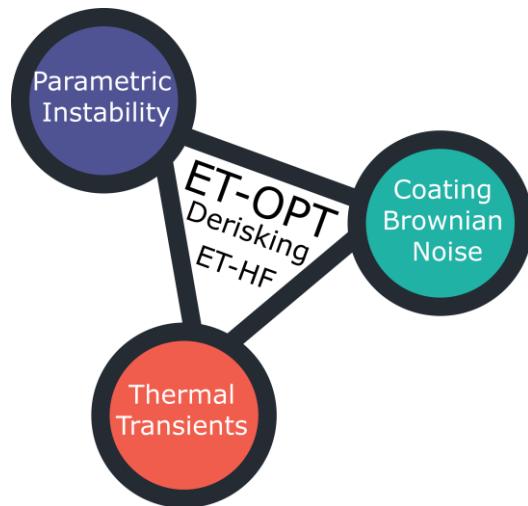
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Preprint available on arXiv:  
<https://arxiv.org/abs/2505.03525>



We propose testing the technique at Virgo

ET-OPT @ UCLouvain  
Poster by Dr. Aaron Goodwin-Jones



# Extra Slides

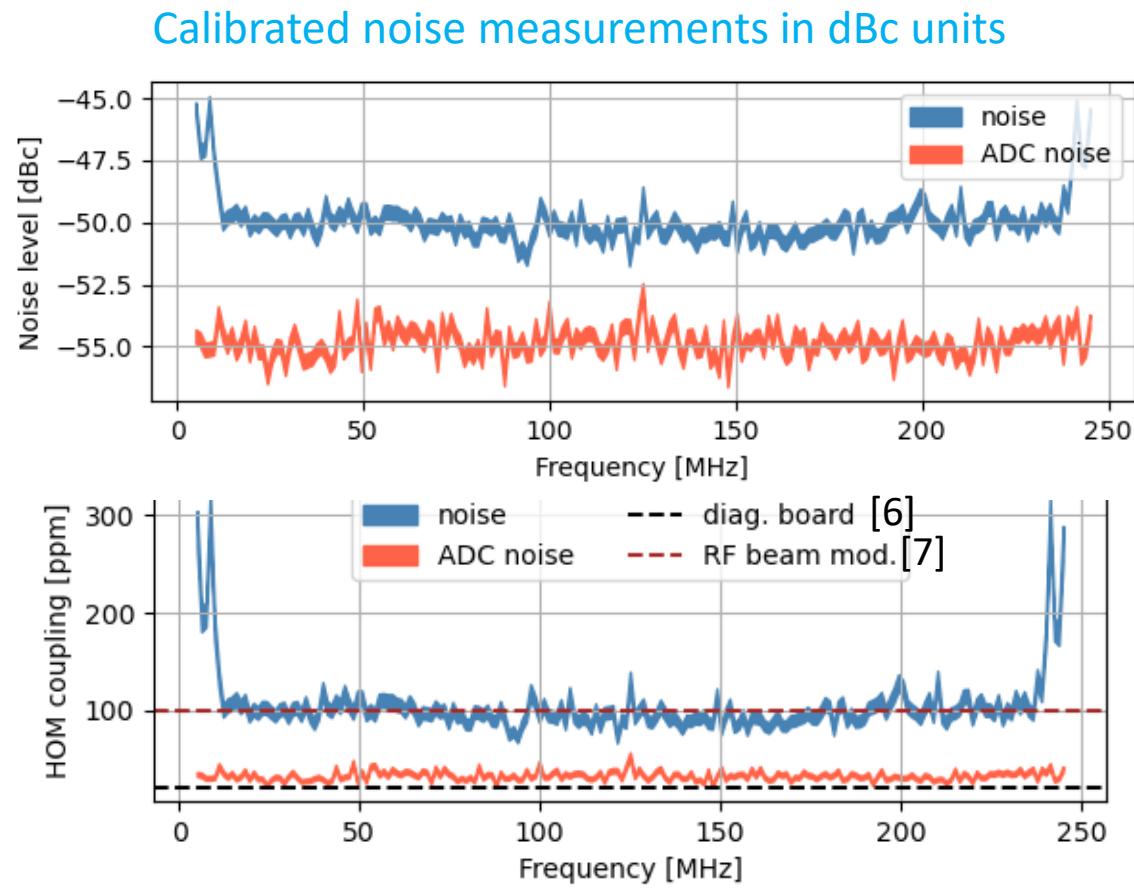
# Noise and detection limits

Power in sideband HOM in decibels relative to carrier [dBc]:

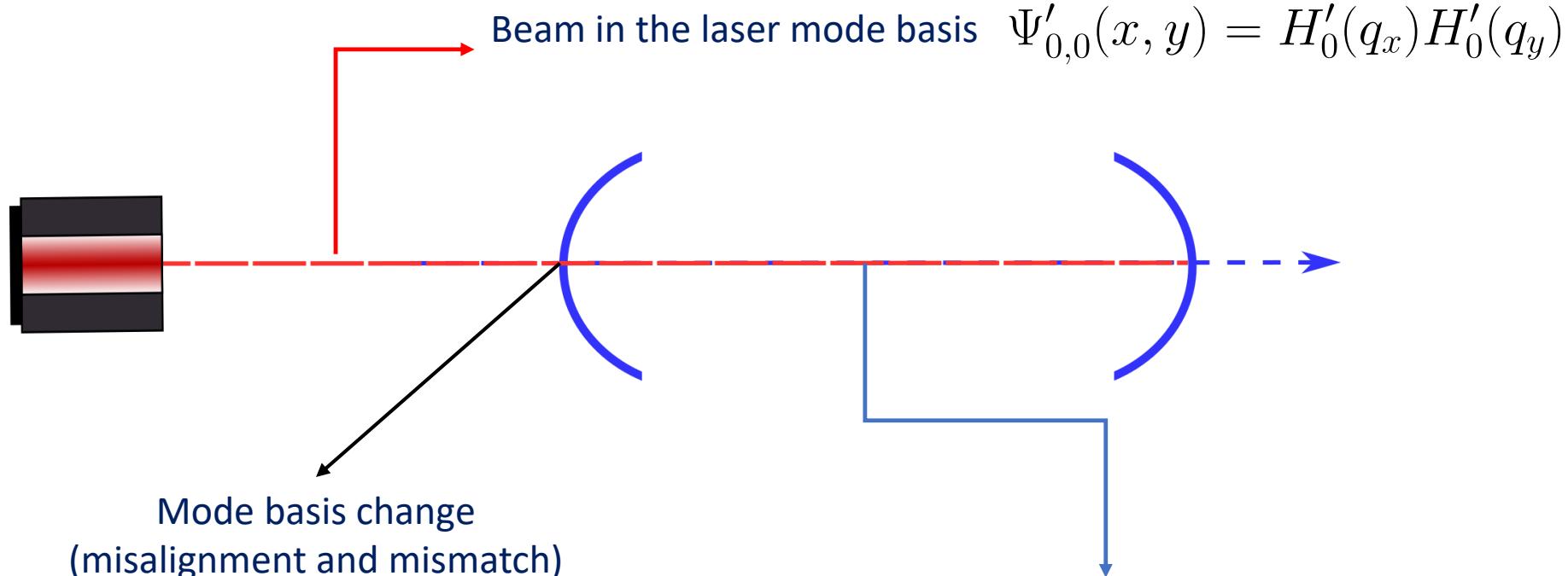
$$\text{Coupling to HOM} \quad ( \text{comparison with FSR scan} ) \quad \leftarrow 10 \log_{10} \left( |k_{mn}|^2 \frac{P_{\text{SB}}}{P_{\text{carr}}} \right) \quad [\text{dBc}]$$

Given by EOM calibration

Converted to HOM coupling  
assuming 10% sidebands.



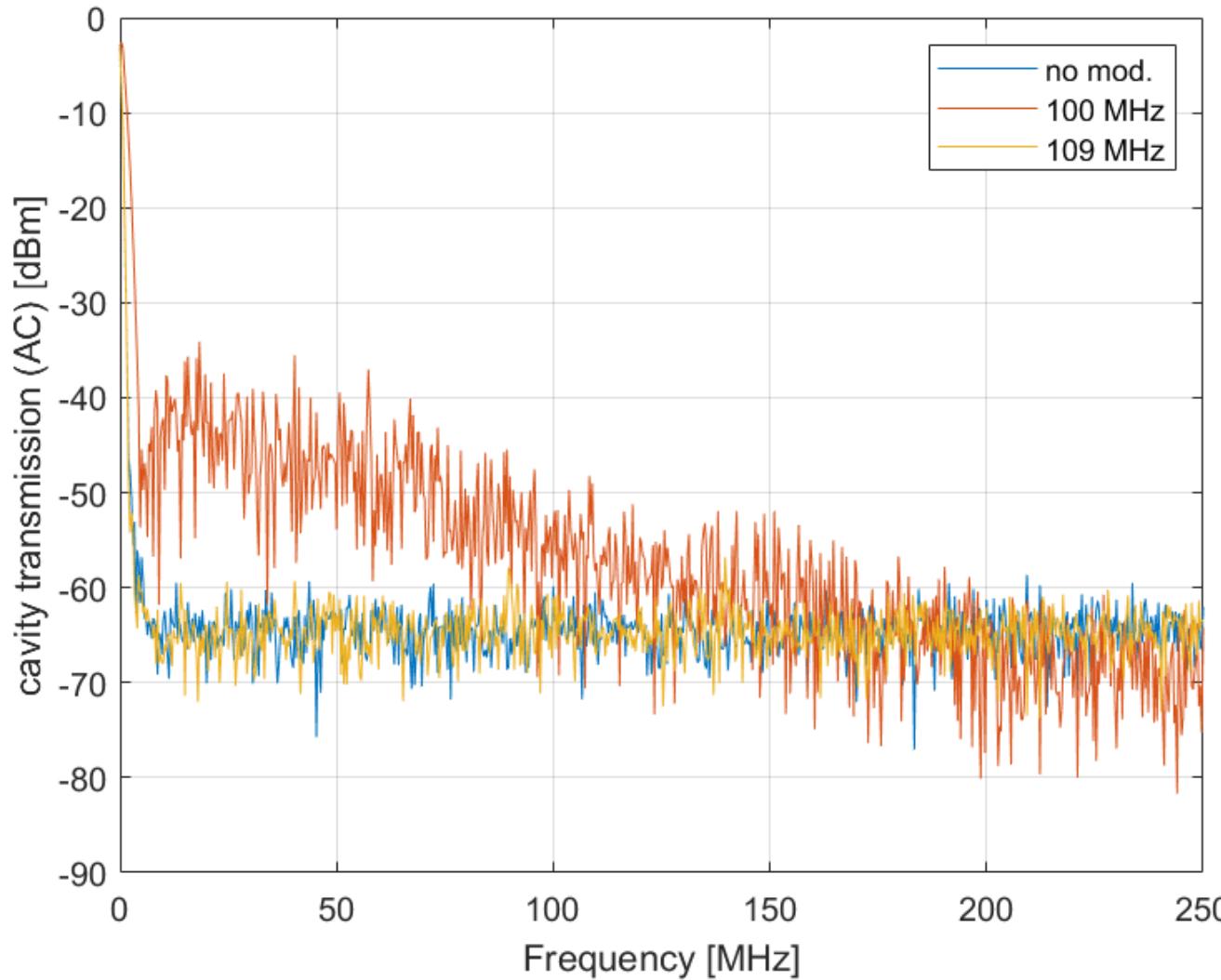
# Mode basis changes and higher order modes



$$K = \begin{pmatrix} k_{0',0} & \dots & k_{0',j} & \dots & k_{0',N} \\ \dots & \dots & \dots & \dots & \dots \\ k_{i',0'} & \dots & k_{i',j'} & \dots & k_{i',N} \\ \dots & \dots & \dots & \dots & \dots \\ k_{N',0} & \dots & k_{N',j} & \dots & k_{N',N} \end{pmatrix}$$

Beam in the cavity mode basis  
 $\Psi_{mn}(x, y) = H_m(q_x)H_n(q_y)$

# PDH + second sideband modulation



- PDH frequency = 50 MHz.
- The PDH lock is unaffected except for scanning frequencies at the PDH frequency times n (natural number).