

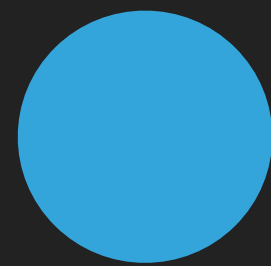
SIMULATING INTERMEDIATE- MASS BLACK HOLES IN THE FIRST STAR CLUSTERS

BENEDETTA MESTICHELLI

XV ET SYMPOSIUM - 27/05/2025

*IN COLLABORATION WITH: MANUEL ARCA SEDDA, MARICA BRANCHESI, MICHELA MAPELLI, STEFANO TORNIAMENTI, GIULIANO IORIO,
GUGLIELMO COSTA, FILIPPO SANTOLIVU, ALESSANDRO LUPI, MARTA VOLONTERI*

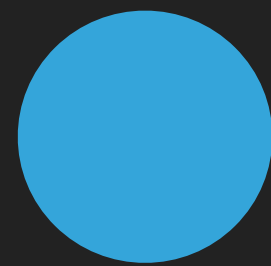
WHAT IS AN INTERMEDIATE-MASS BLACK HOLE?



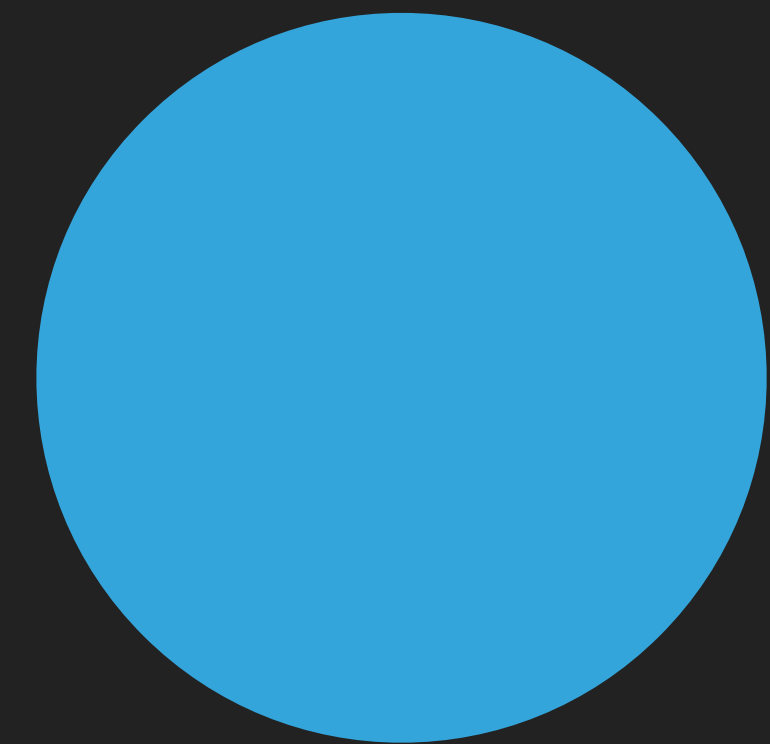
Stellar-mass BHs

$$m_{\text{BH}} \sim 5 - 10^2 M_{\odot}$$

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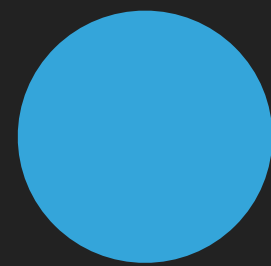


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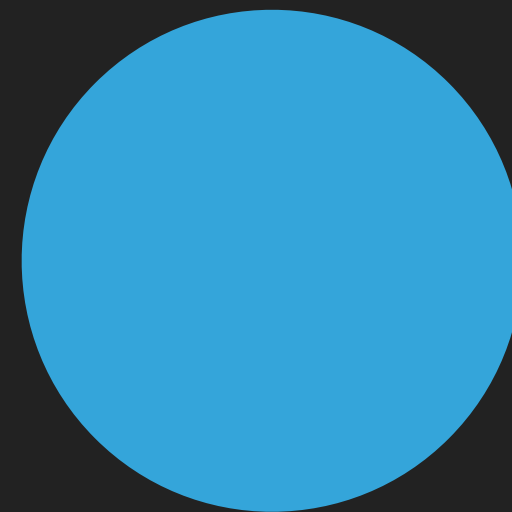


Supermassive BHs
 $m_{\text{BH}} \gtrsim 10^5 M_{\odot}$

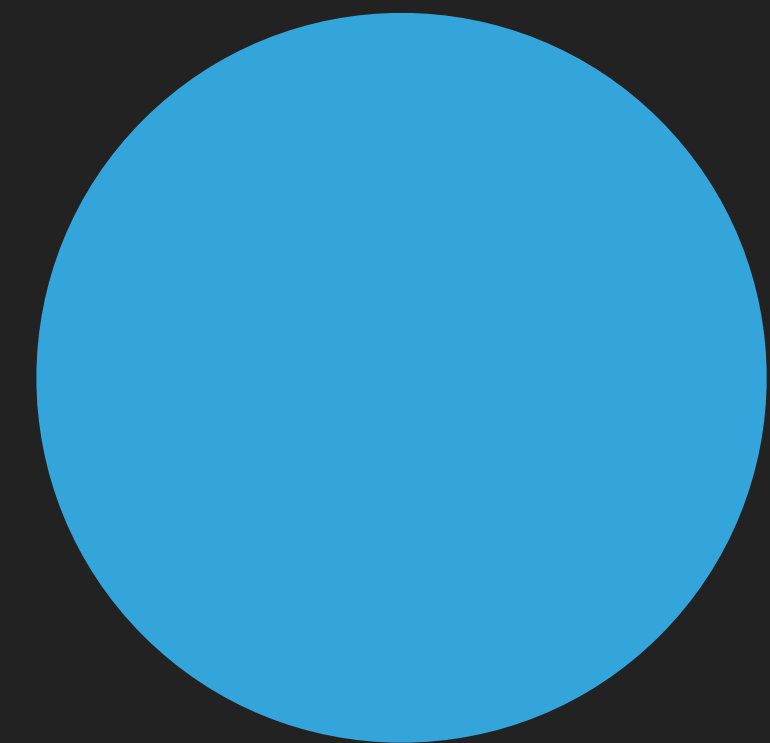
WHAT IS AN INTERMEDIATE-MASS BLACK HOLE?



Stellar-mass BHs
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Intermediate-mass BHs
 $m_{\text{BH}} \sim 10^2 - 10^5 M_{\odot}$

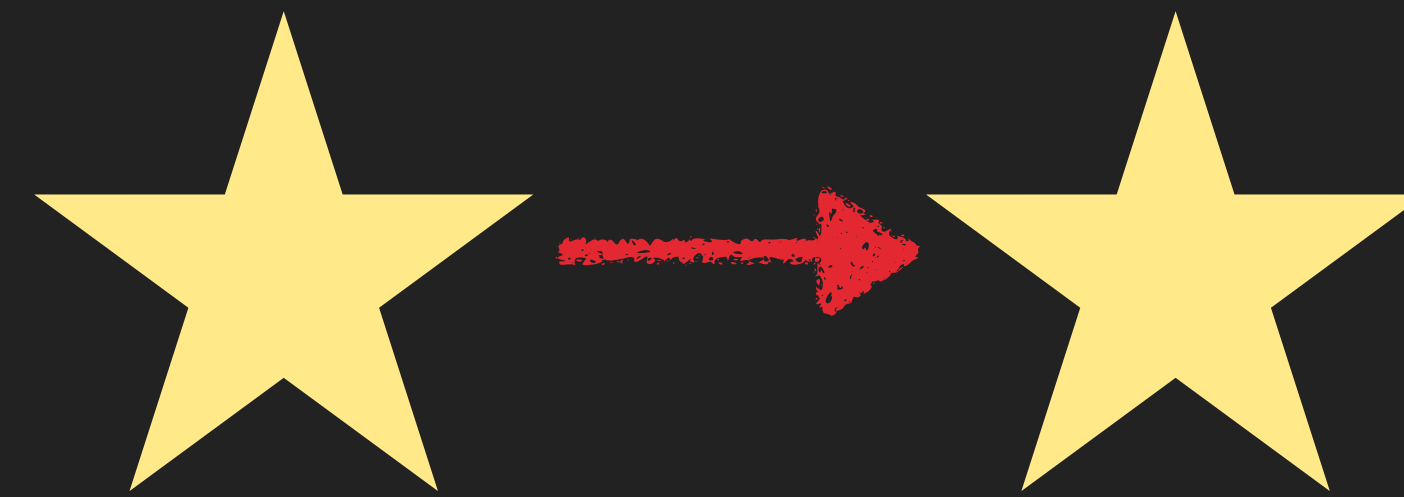


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POPULATION III STARS

- ▶ **Metal-free**

(Haiman et al. 1996; Yoshida et al. 2003)



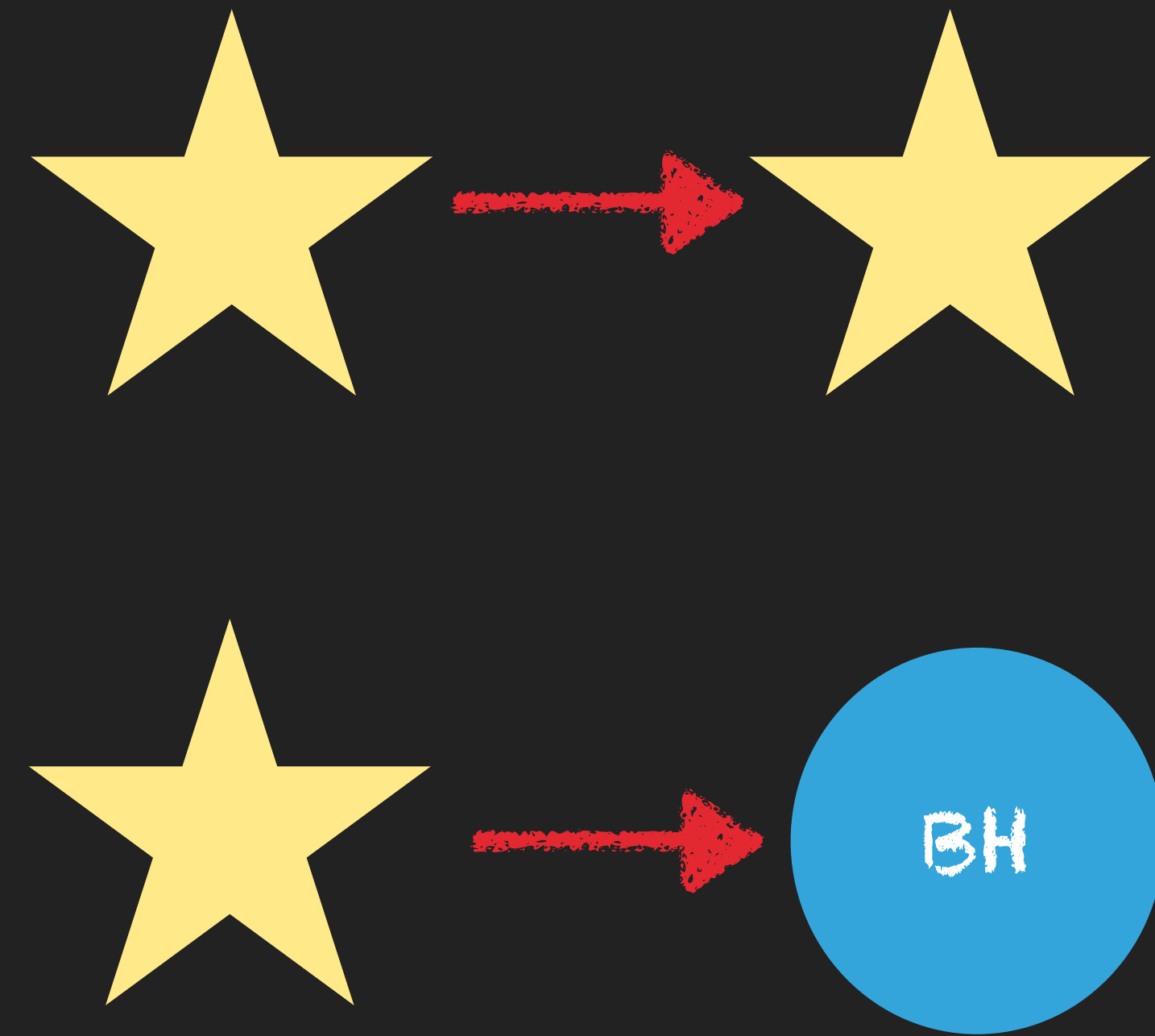
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- ▶ **Metal-free**

(Haiman et al. 1996; Yoshida et al. 2003)

- ▶ **Massive ($> 10^2 M_{\odot}$)**

(Stacy & Bromm 2013; Hirano et al. 2015;
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POPULATION III STARS

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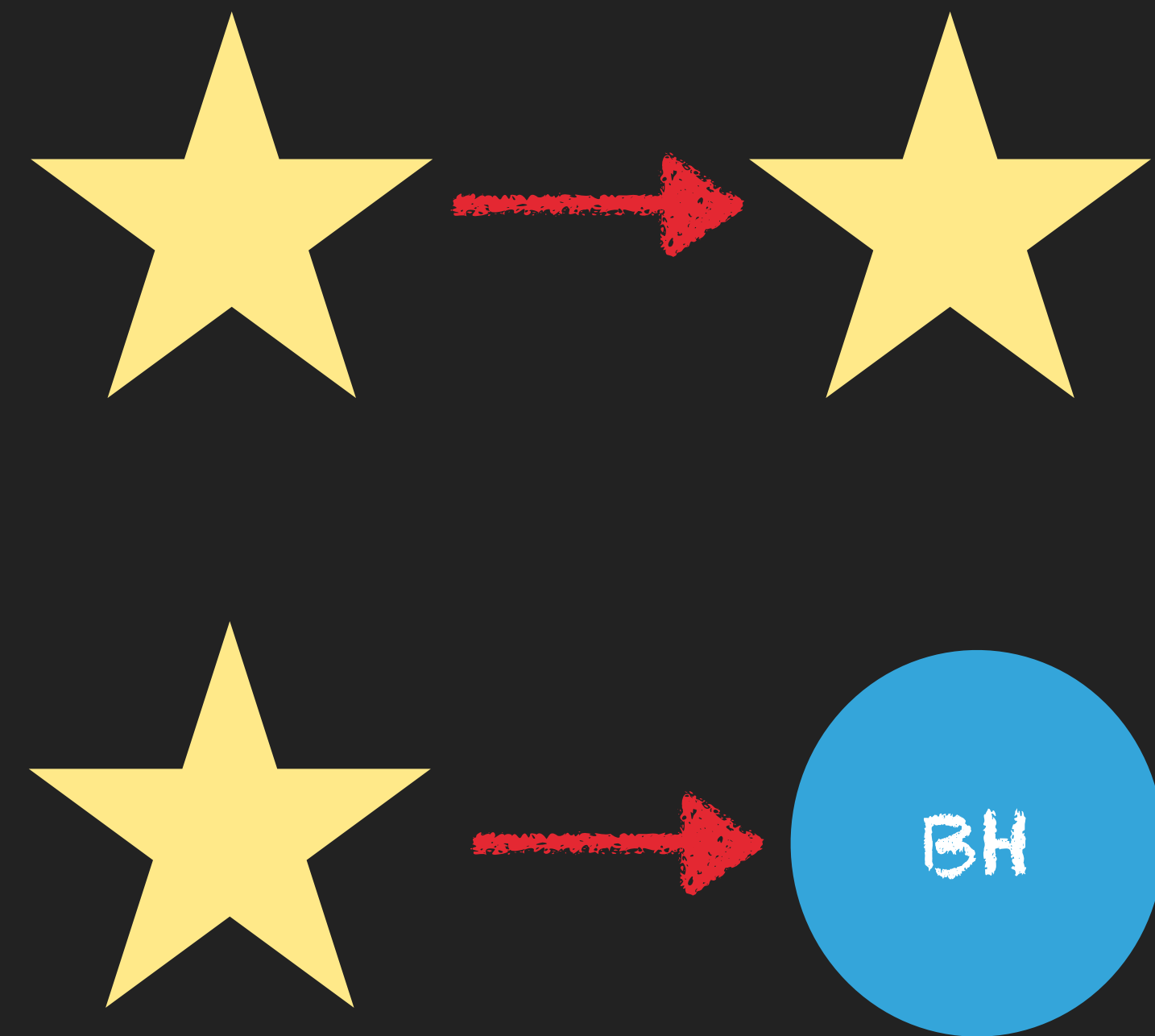
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- ▶ **Form at high redshift $z \gtrsim 20$**

(e.g. Hartwig et al. 2022)



POPULATION III STARS

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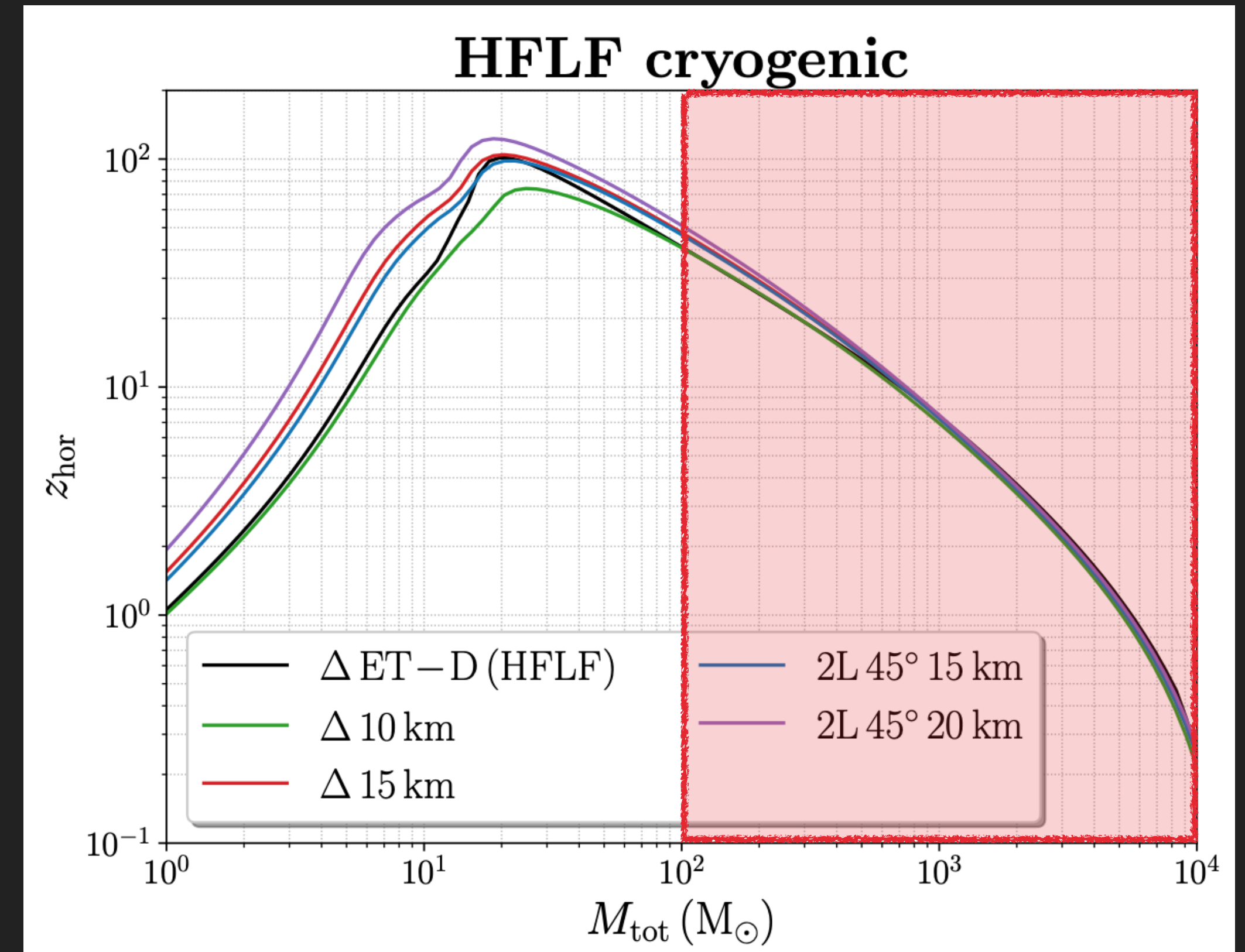
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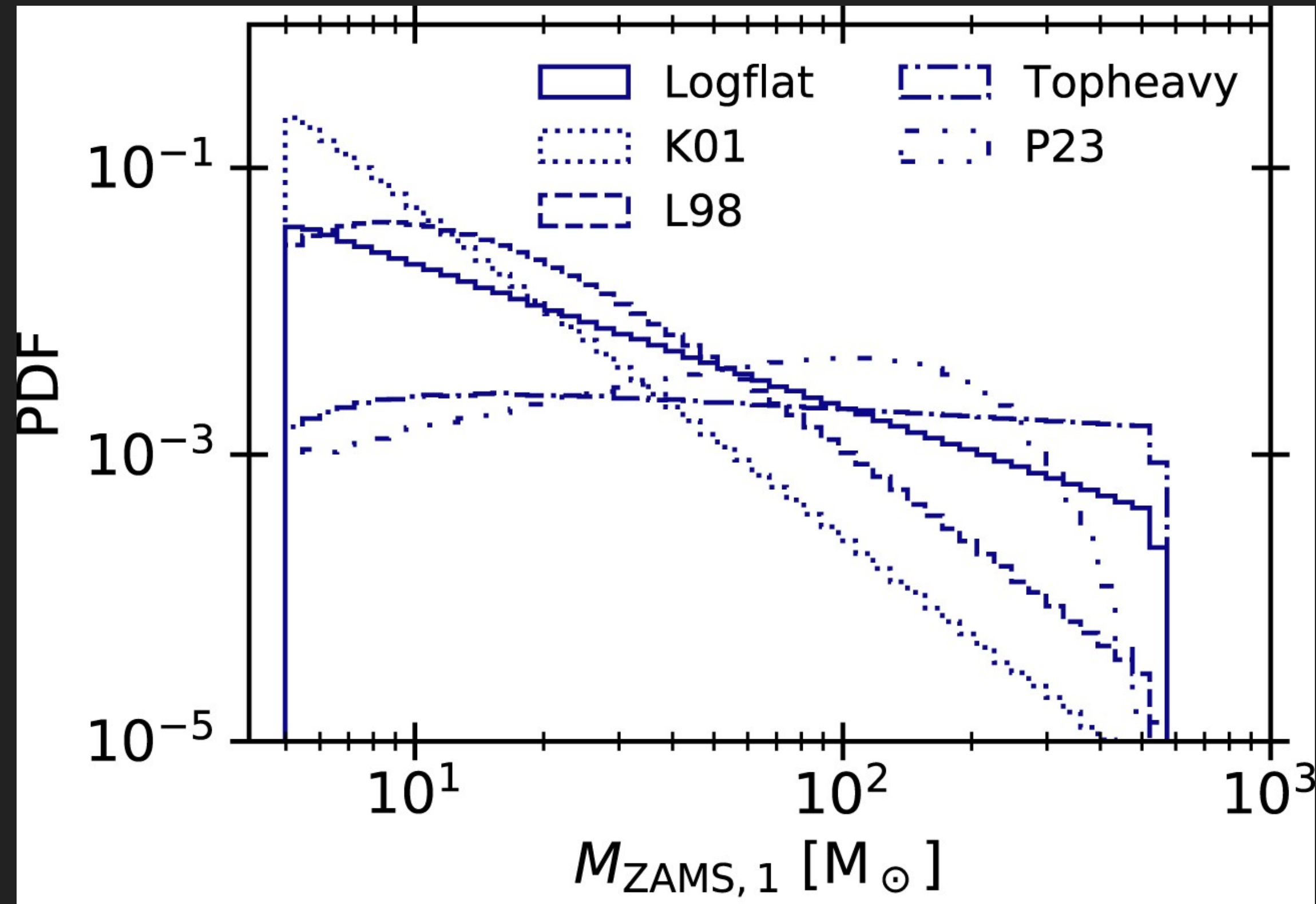
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PERFECT SOURCES OF SIGNALS FOR THIRD GENERATION INTERFEROMETERS

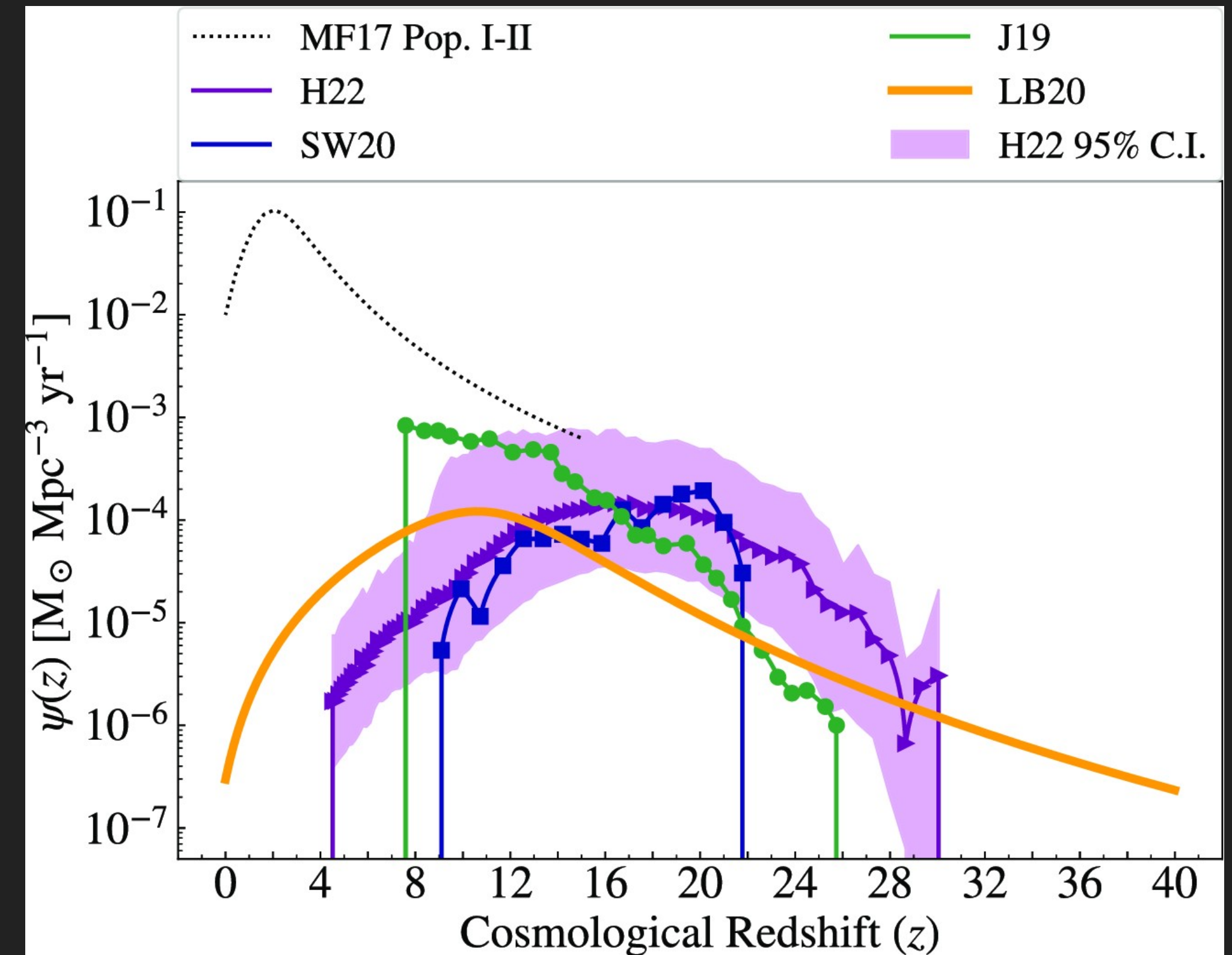


Kalogera et al. 2021; Branchesi et al. 2023

UNCERTAINTIES ON IMF AND SFR

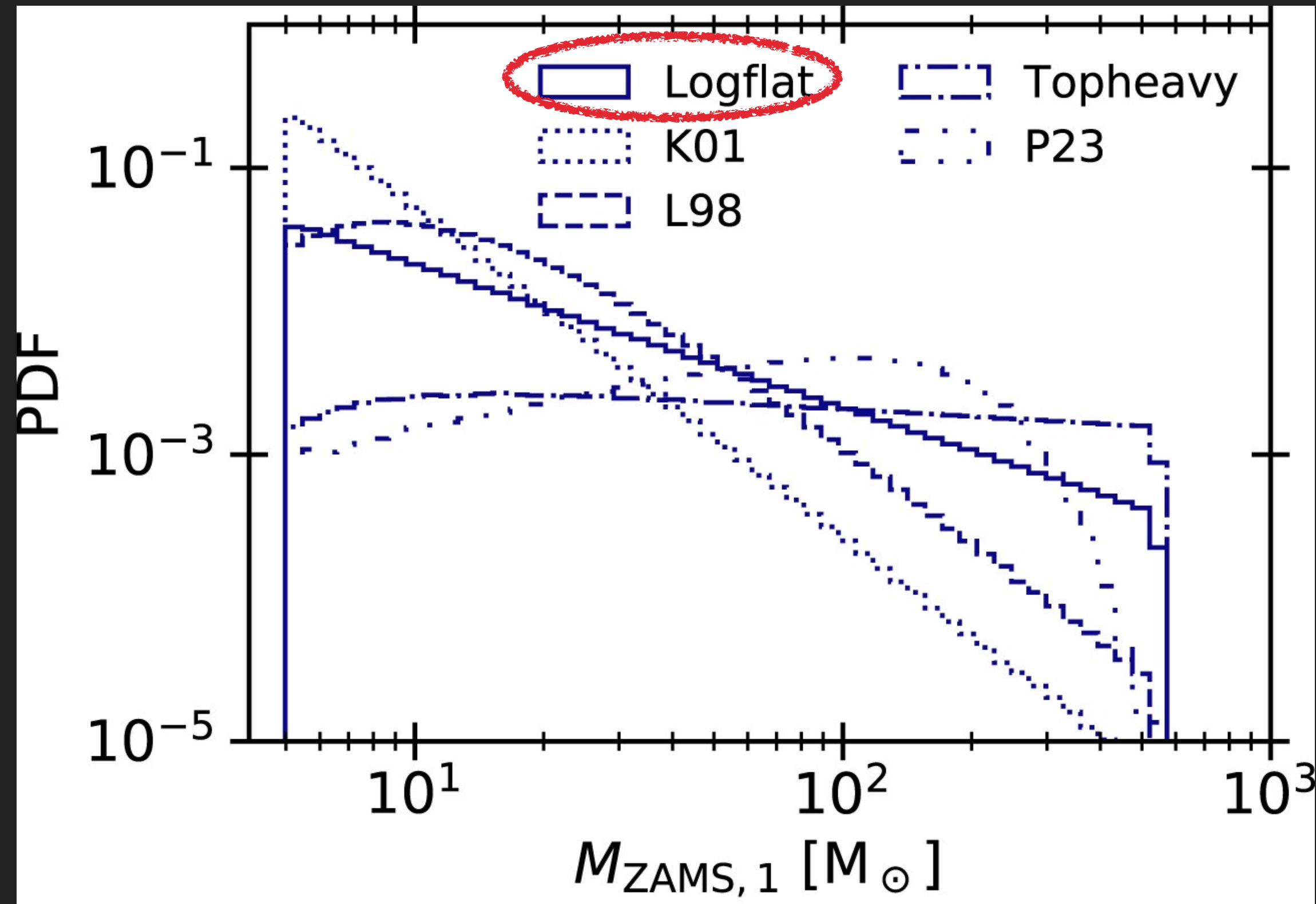


Costa et al. 2023

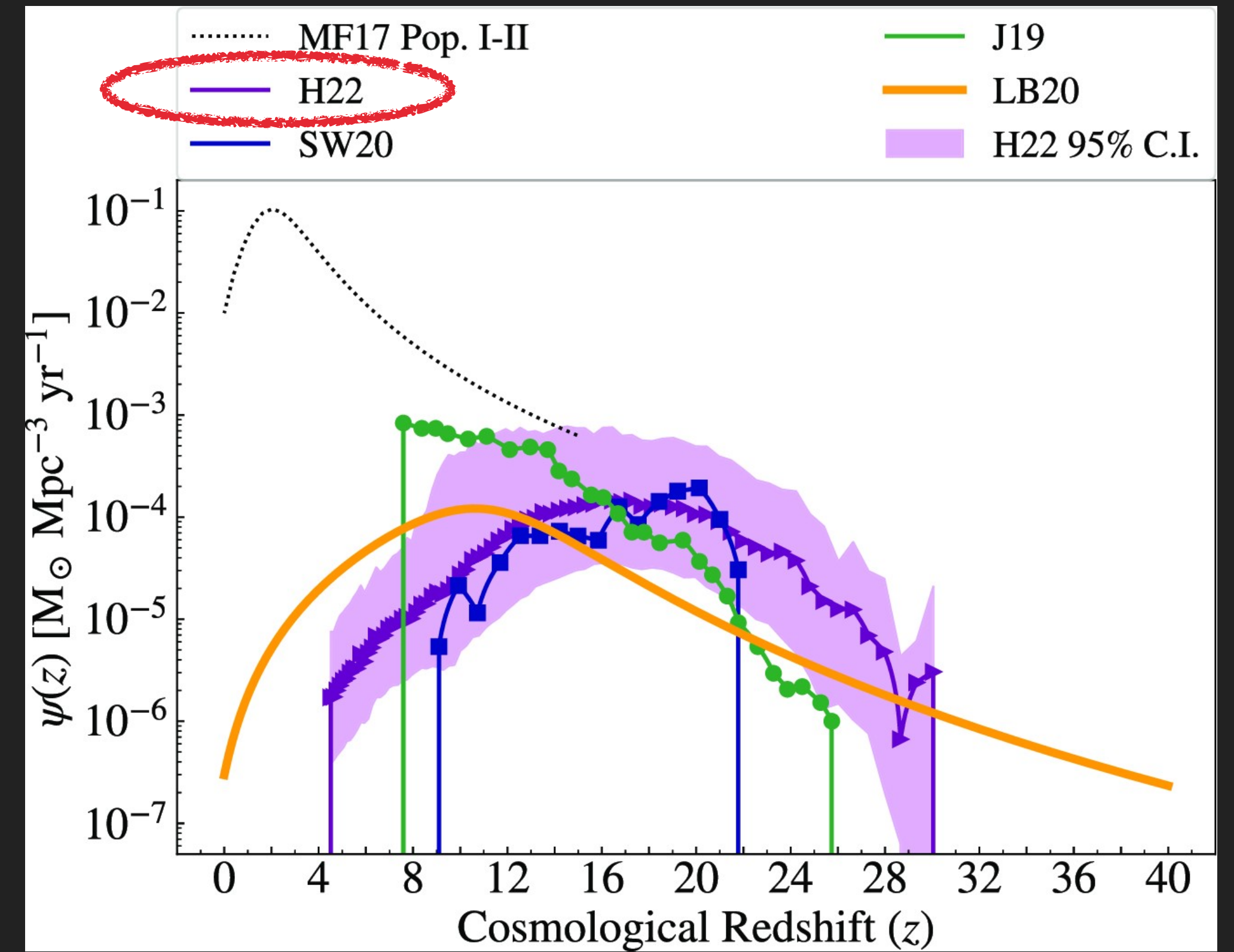


Santoliquido et al. 2023

UNCERTAINTIES ON IMF AND SFR



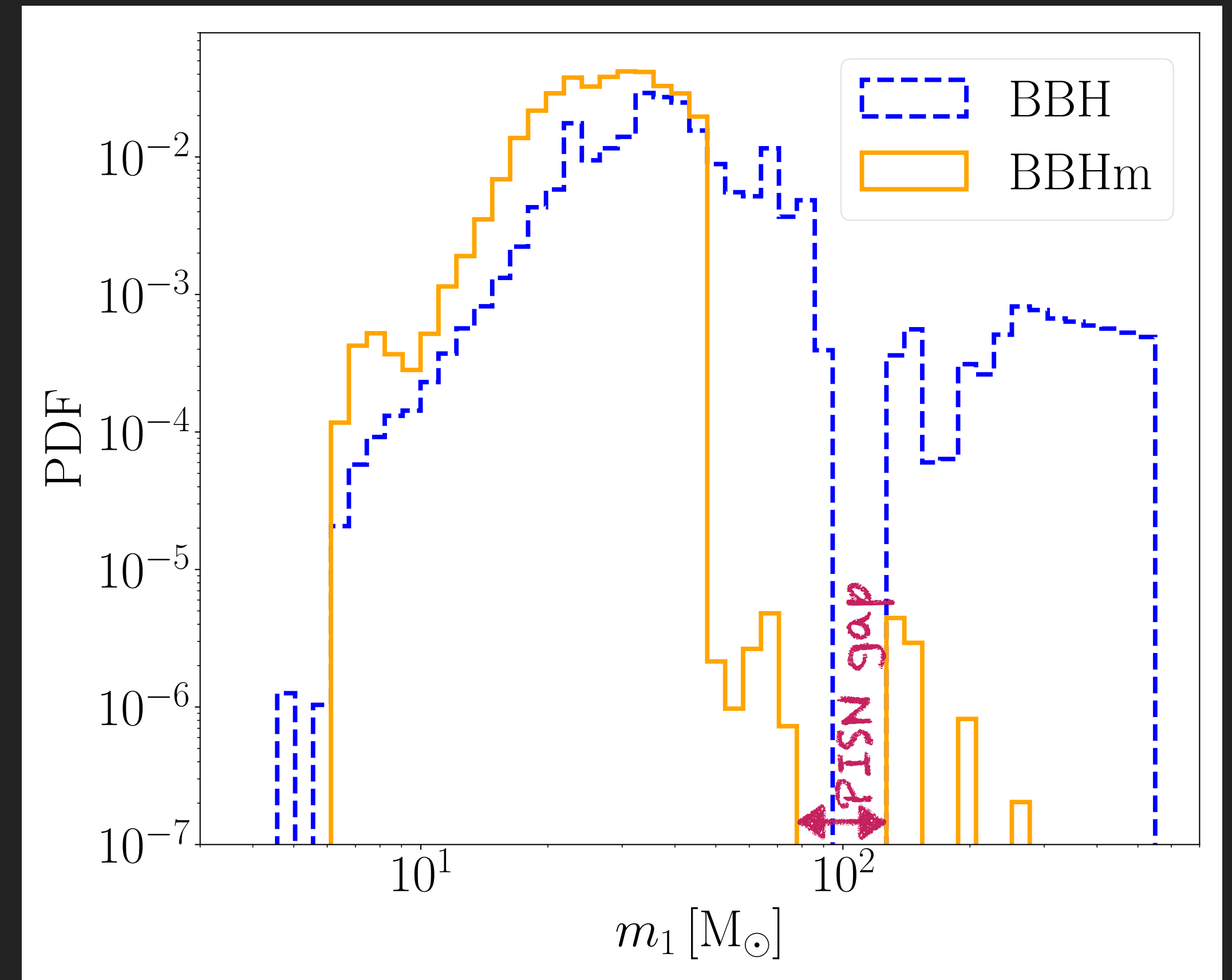
Costa et al. 2023



Santoliquido et al. 2023

POP III BINARY BLACK HOLE MERGERS ABOVE THE GAP

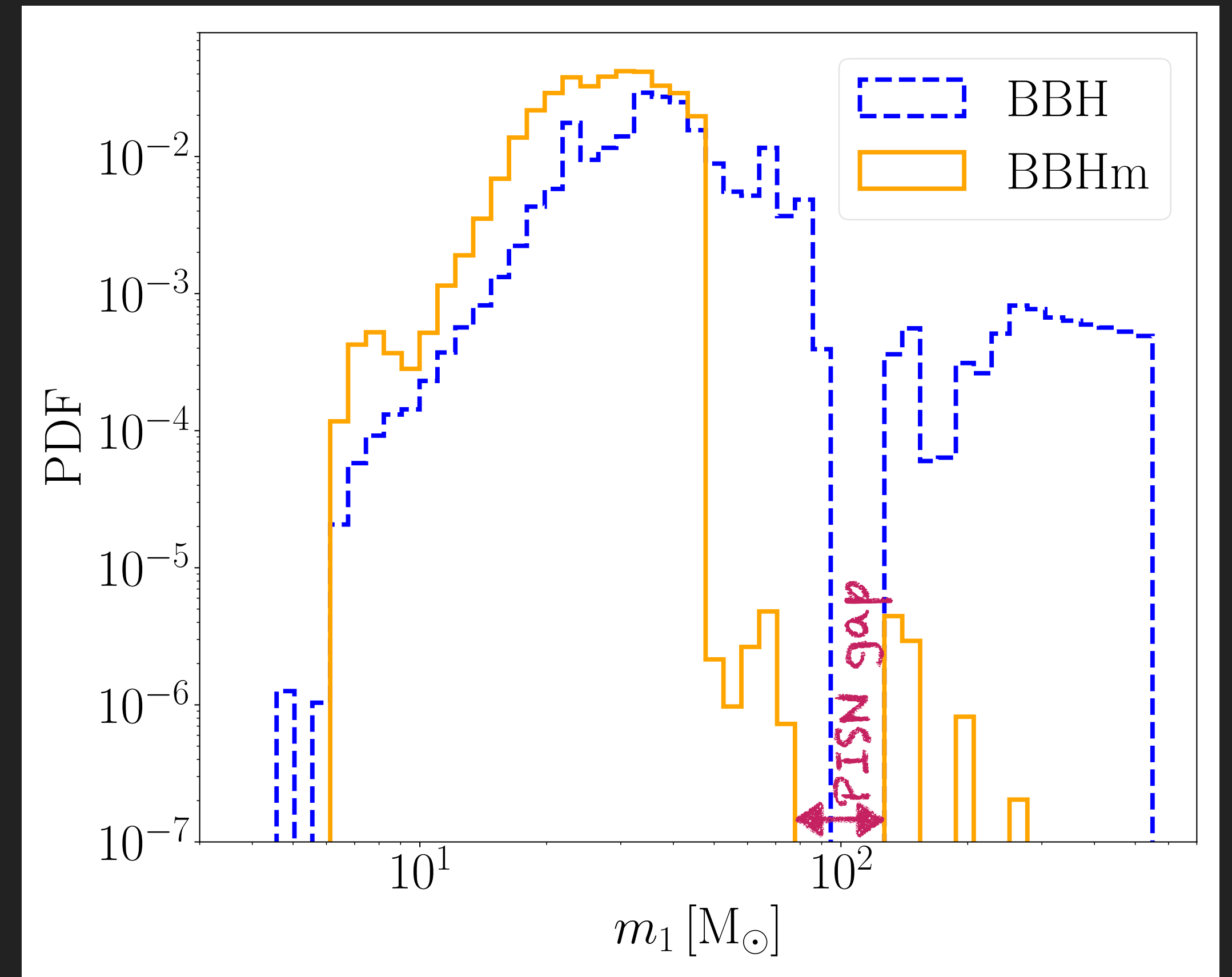
- ▶ BBHs with IMBH primary form
(Tanikawa et al. 2020-2024; Costa et al. 2023; Santoliquido et al. 2023)
- ▶ **Almost no mergers above the pair instability mass gap**



Costa et al. 2023; Mestichelli et al. 2024

POP III BINARY BLACK HOLE MERGERS ABOVE THE GAP

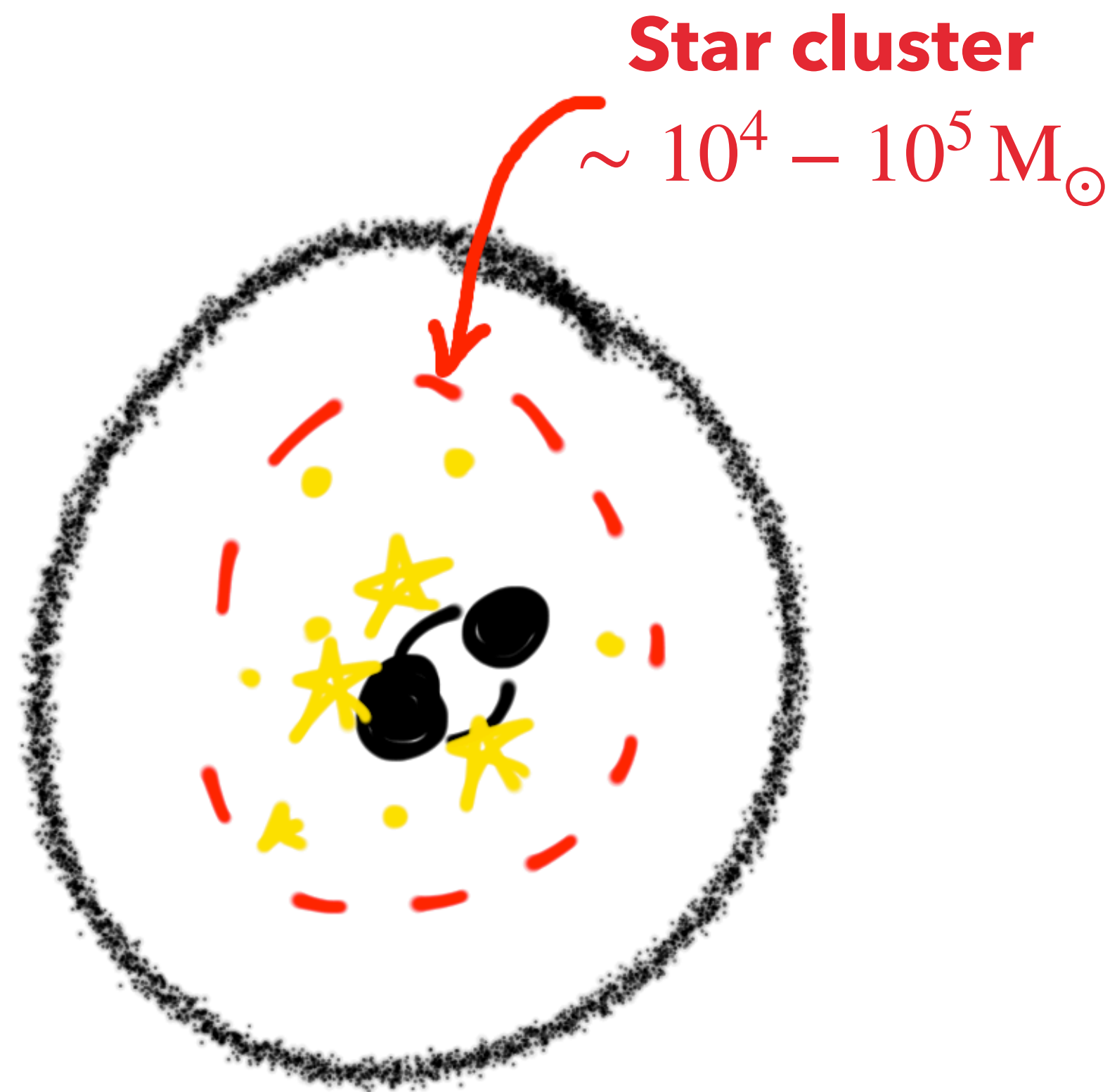
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Costa et al. 2023; Mestichelli et al. 2024

**WHAT IF THE FIRST STARS
WERE BORN IN CLUSTERS?**

- ▶ Formation of **very massive stars** via **repeated stellar collisions**
- ▶ Boost of pair-up, hardening and **merger of BBHs above gap**
 - ▶ **Dynamics pairs up massive BHs**
 - ▶ **Three-body interactions** contribute to **hardening**
- ▶ **Hierarchical mergers**

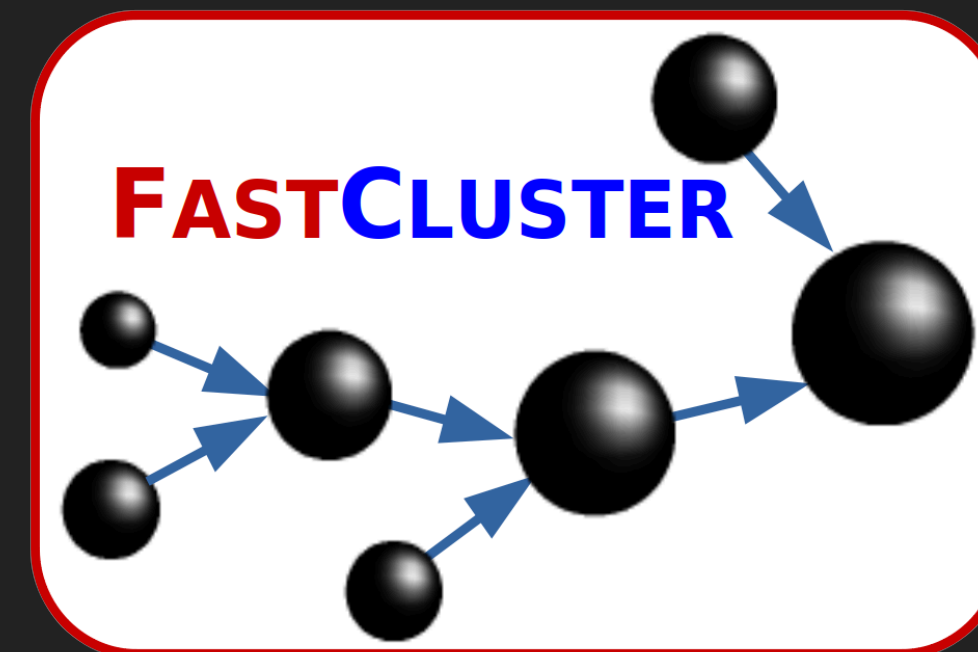


Mini-DM halo
 $\sim 10^7 M_{\odot}$

*Sakurai et al. 2017; Wang et al. 2022;
 Mestichelli et al. 2024; Reinoso et al. 2025*

MASSIVE CLUSTERS

$$\sim 10^4 - 10^5 M_{\odot}$$

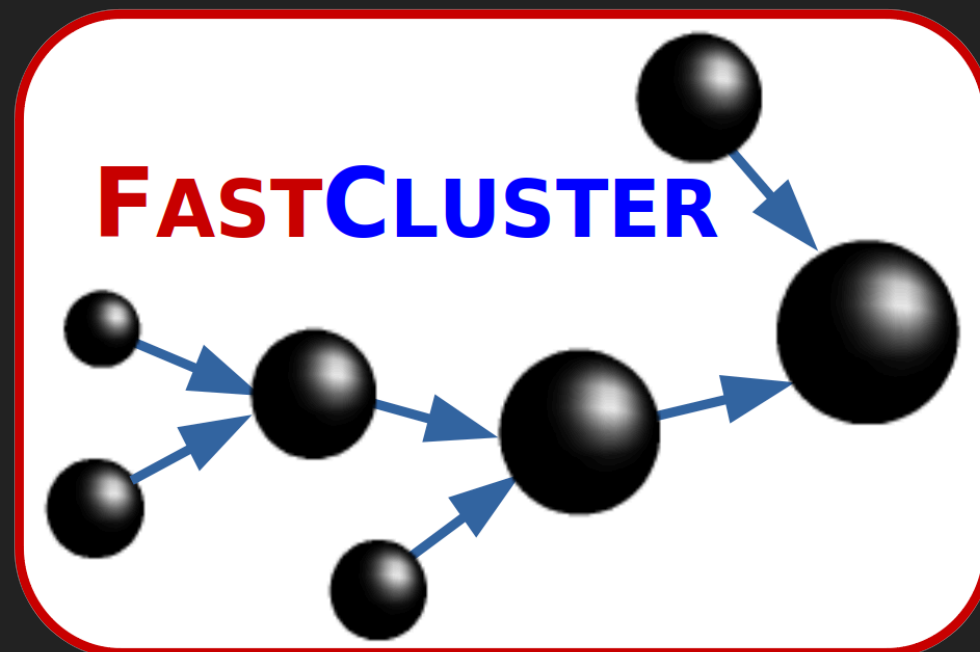


*Mapelli et al. 2021, 2022;
 Torniamenti et al. 2024*

- ▶ Semi-analytic
- ▶ $z = 20 \rightarrow 10$
- ▶ Cluster evolution
- ▶ No stellar evolution

MASSIVE CLUSTERS

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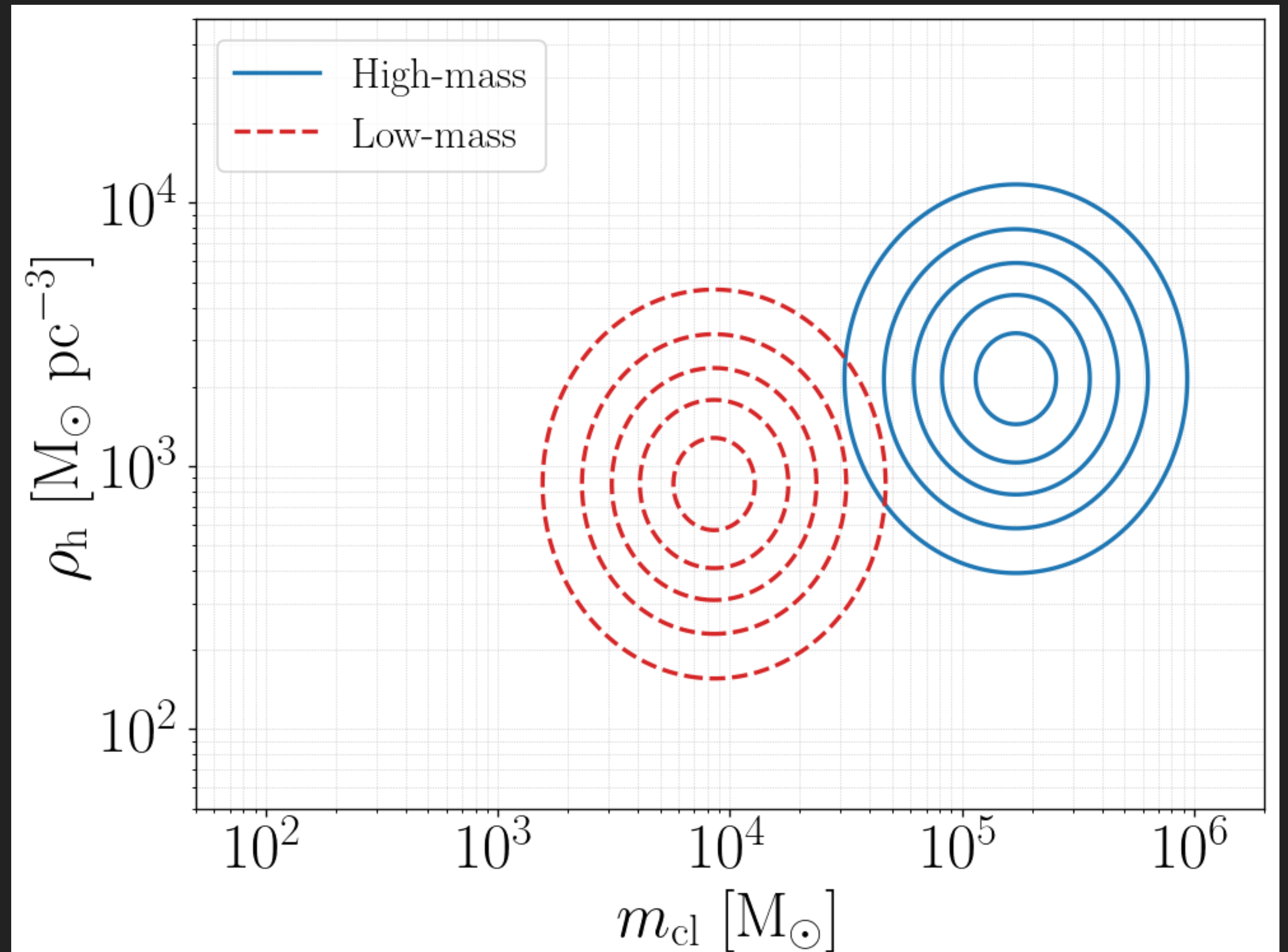
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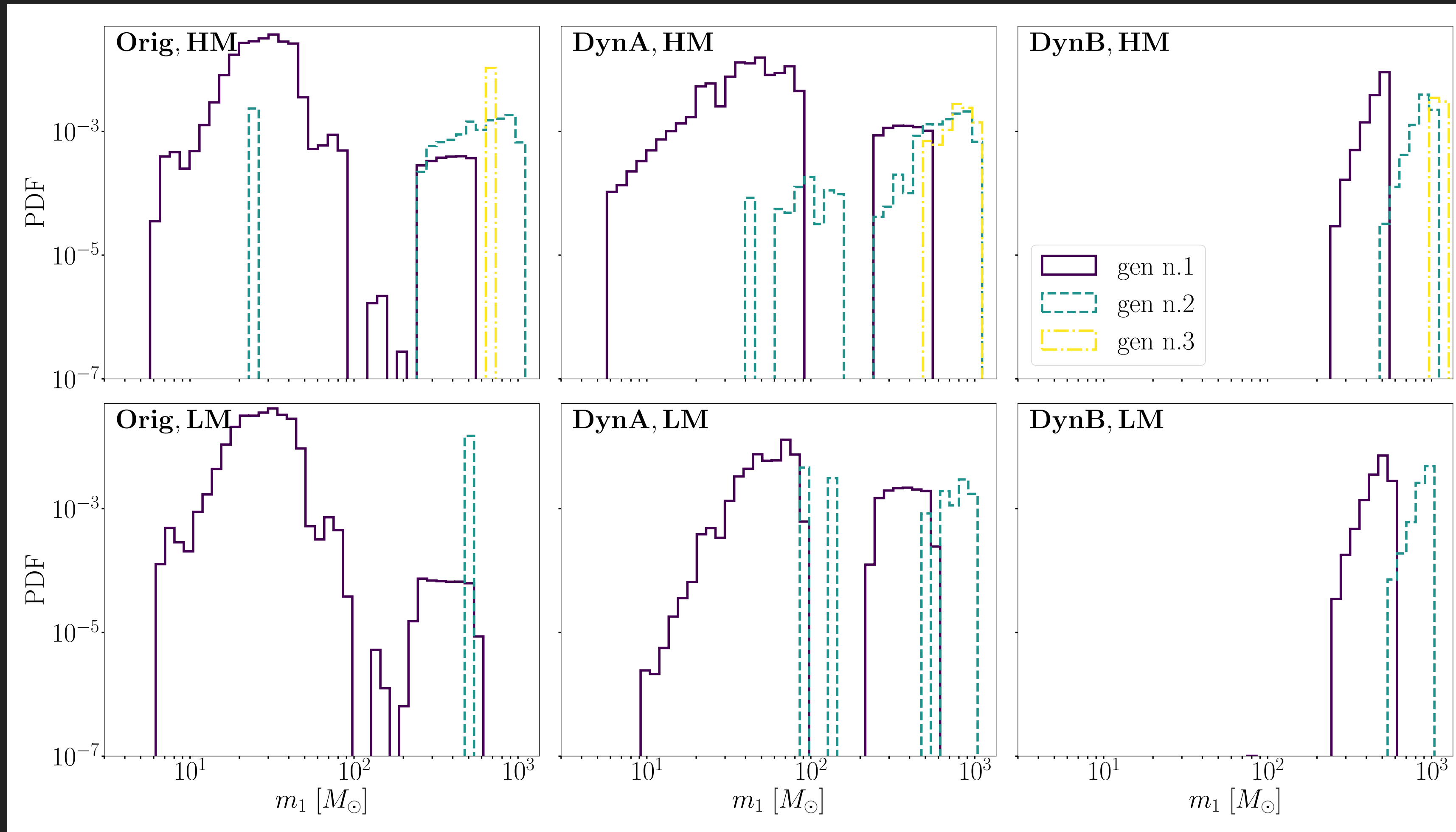
$$m_{\min} = 2 M_{\odot}$$

$$m_{\max} = 600 M_{\odot}$$

log-flat IMF



THE BOOST ABOVE THE PAIR INSTABILITY MASS GAP

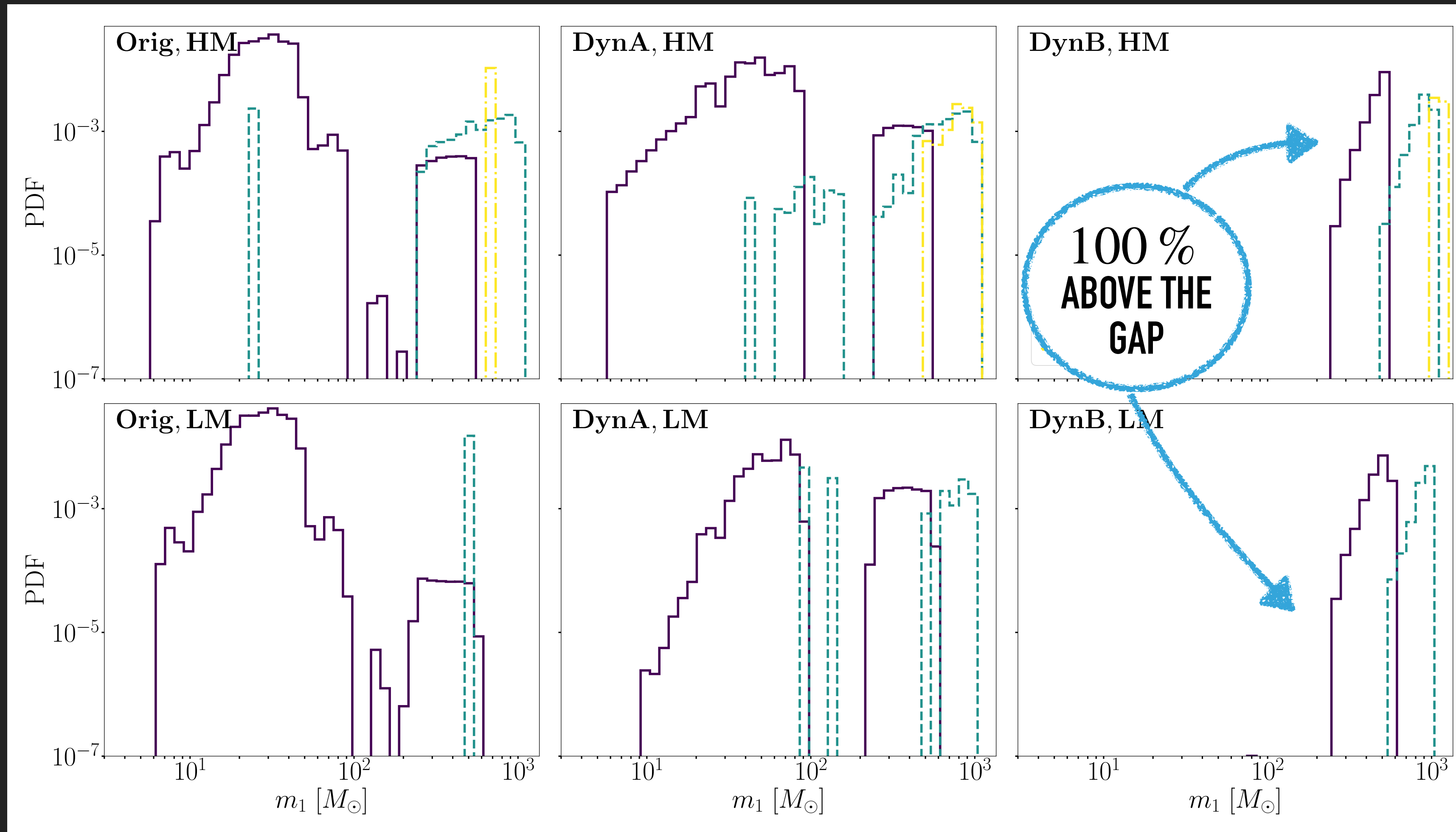


Mestichelli et al. 2024



Mestichelli et al.
2024

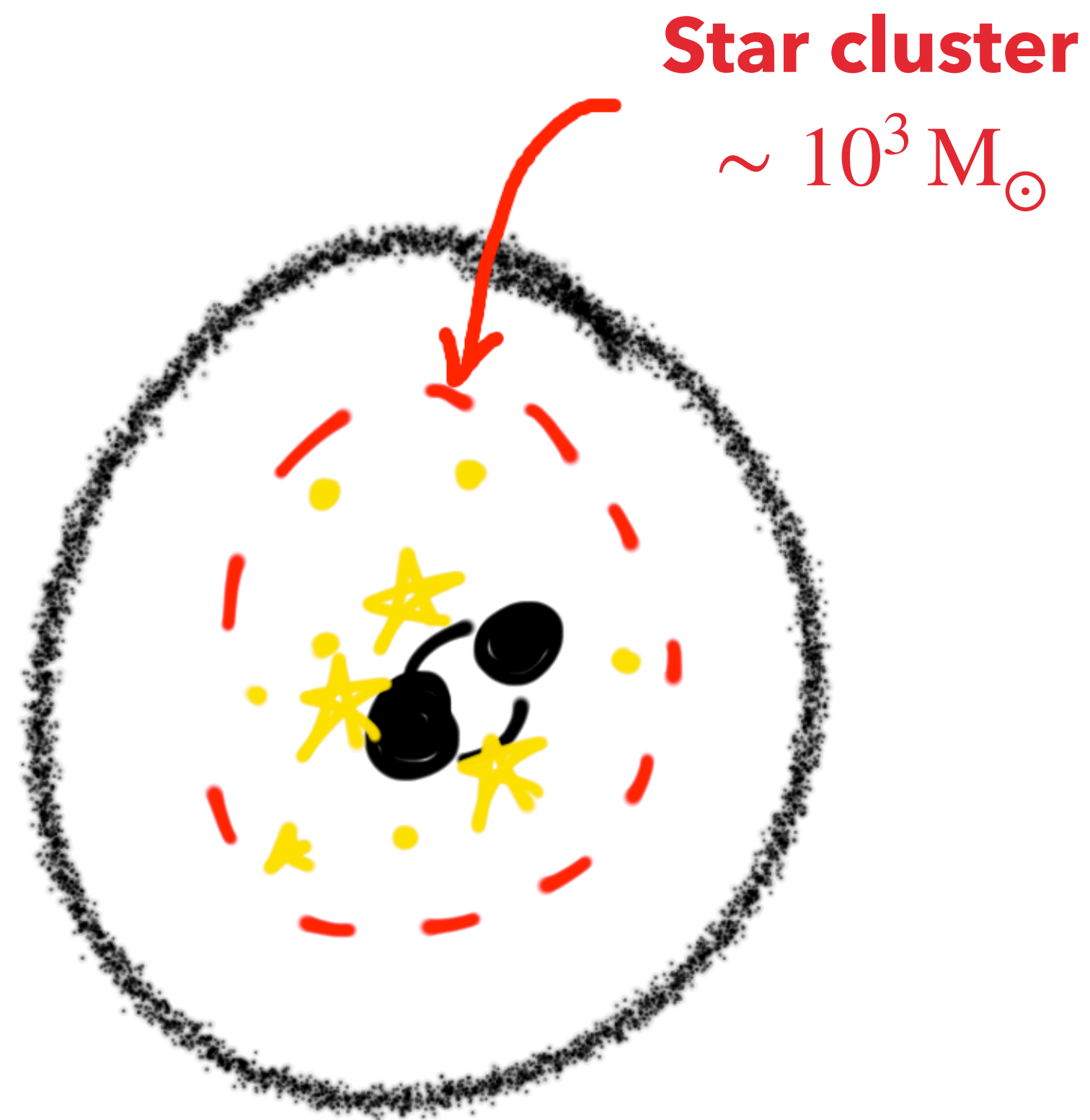
THE BOOST ABOVE THE PAIR INSTABILITY MASS GAP



Mestichelli et al. 2024



Mestichelli et al.
2024



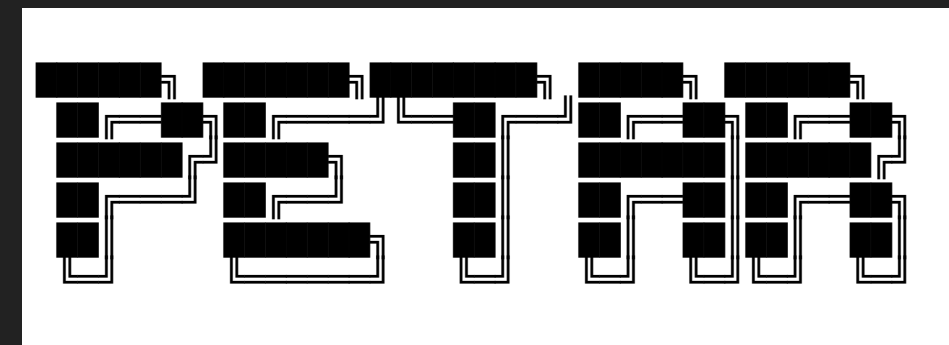
Star cluster
 $\sim 10^3 M_{\odot}$

Mini-DM halo
 $\sim 10^7 M_{\odot}$

Sakurai et al. 2017; Wang et al. 2022;
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LOW-MASS CLUSTERS

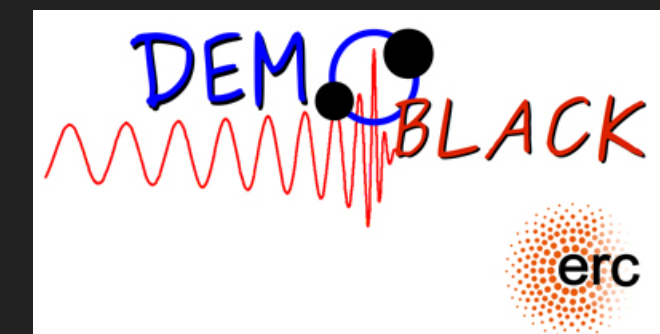
$\sim 10^3 M_{\odot}$



bseEmp

Wang et al. 2020;
Tanikawa et al. 2020

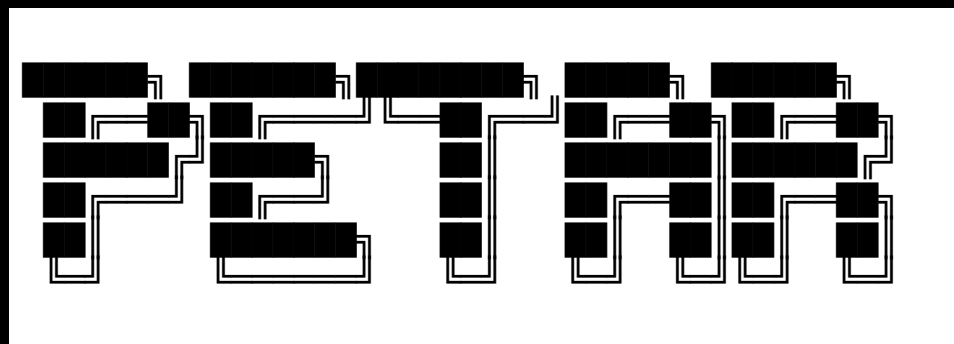
- N-body code
- $z = 20 \rightarrow 10$
- Stellar evolution (bseEmp)
- External potential (galpy)



PRELIMINARY

LOW-MASS CLUSTERS

$\sim 10^3 M_\odot$



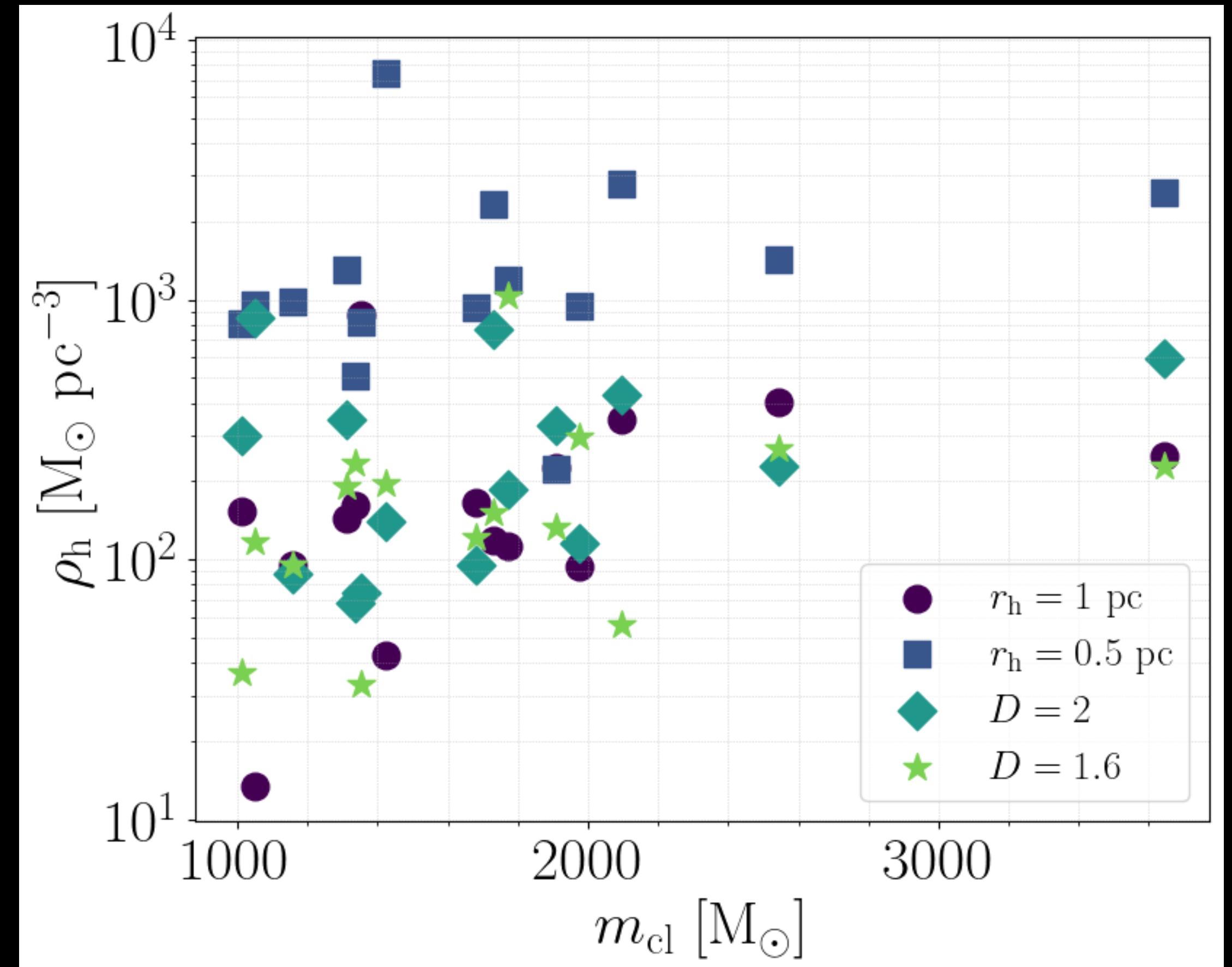
bseEmp

Wang et al. 2020;
Tanikawa et al. 2020

- ▶ N-body code
- ▶ $z = 20 \rightarrow 10$
- ▶ Stellar evolution (bseEmp)
- ▶ External potential (galpy)

$$m_{\min} = 0.8 M_\odot$$
$$m_{\max} = 300 M_\odot$$

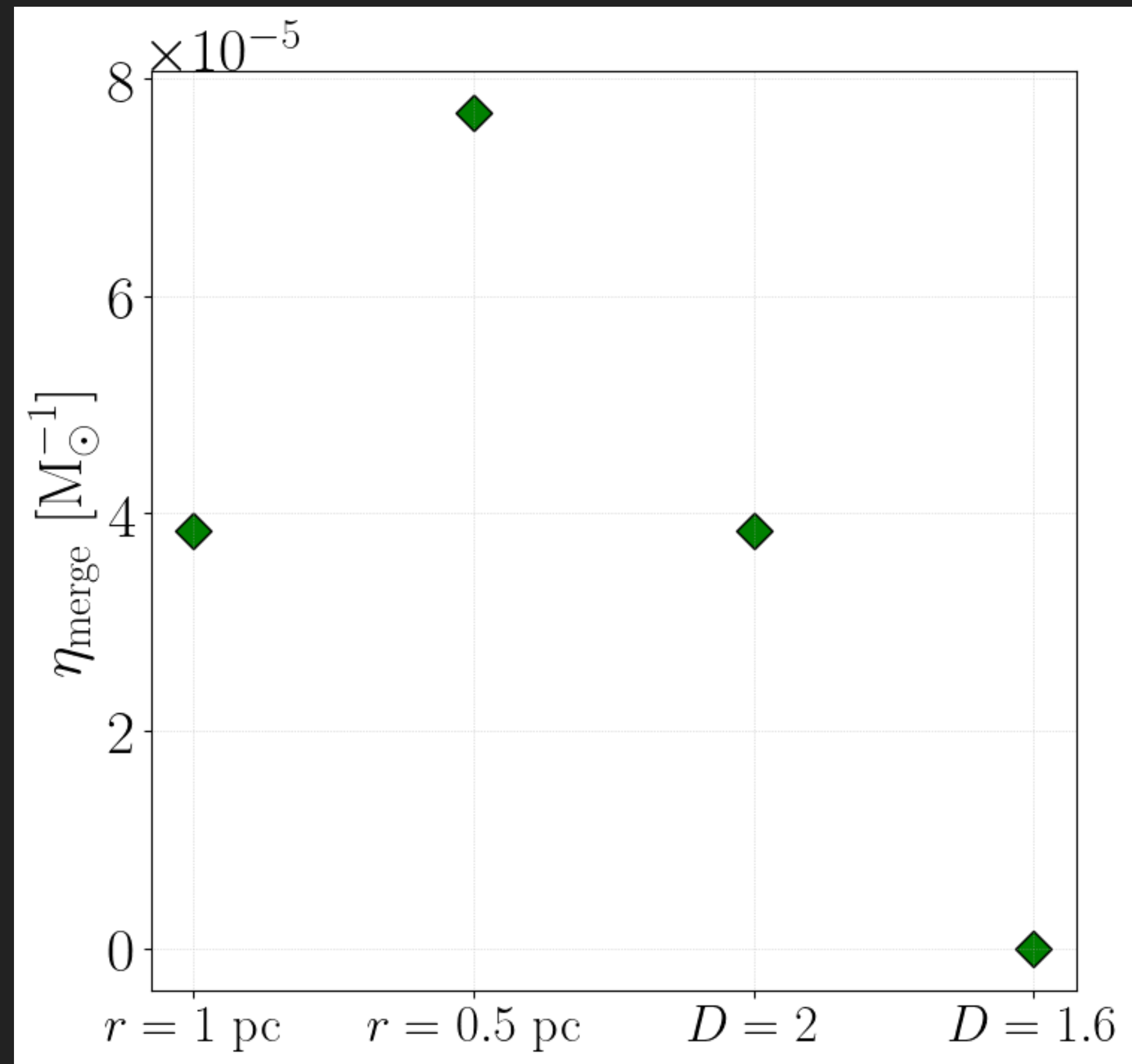
log-flat IMF



Mestichelli et al., in prep.

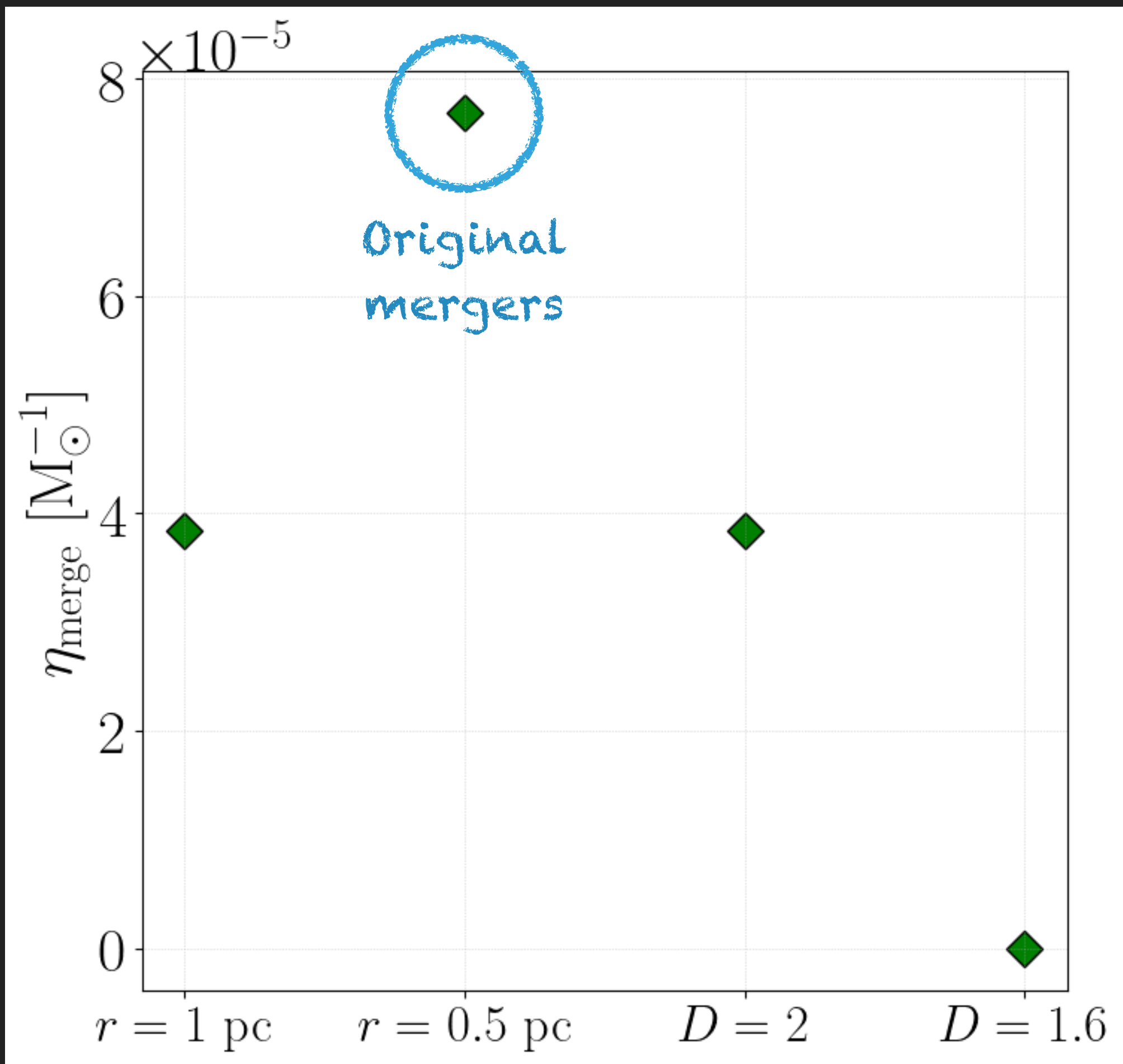
PRELIMINARY

MERGER EFFICIENCIES: A COMPARISON

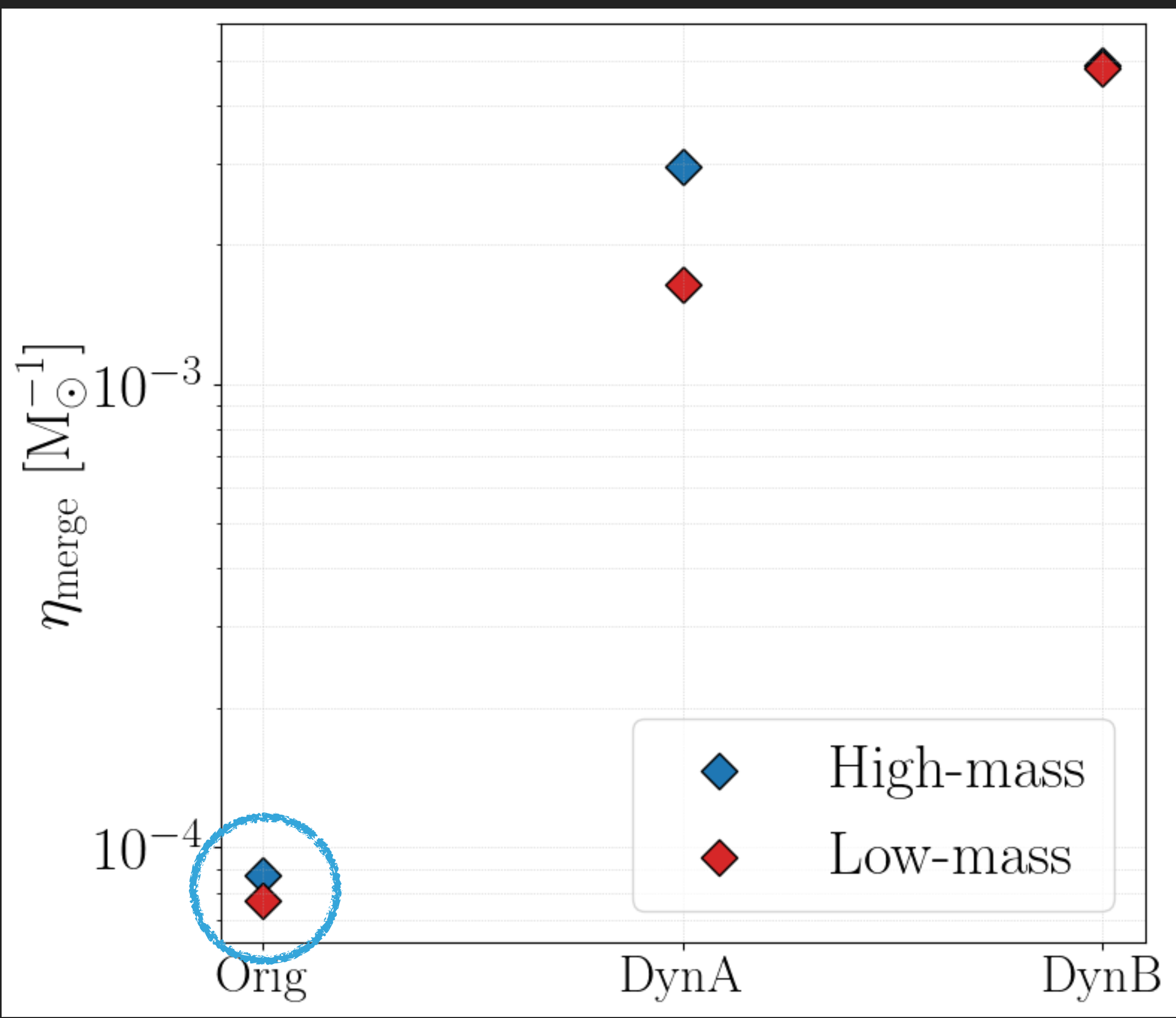


Mestichelli et al., in prep.

MERGER EFFICIENCIES: A COMPARISON



Mestichelli et al., in prep.



Mestichelli et al. 2024

CONCLUSIONS

- ▶ **Pop. III stars** are candidate **progenitors** of **intermediate-mass black holes**
 - ▶ *Simulations in field*: binaries with intermediate-mass black hole primaries **form efficiently but don't merge**
- ▶ **Stellar dynamics** in the first star clusters can **enhance mergers** above upper-mass gap
 - ▶ Massive clusters (fastcluster): up to **100 %** of mergers with intermediate-mass black hole primary
 - ▶ Low-mass clusters (PeTar+bseEmp): only original BBH mergers
 - ▶ **Same order of magnitude of merger efficiency**

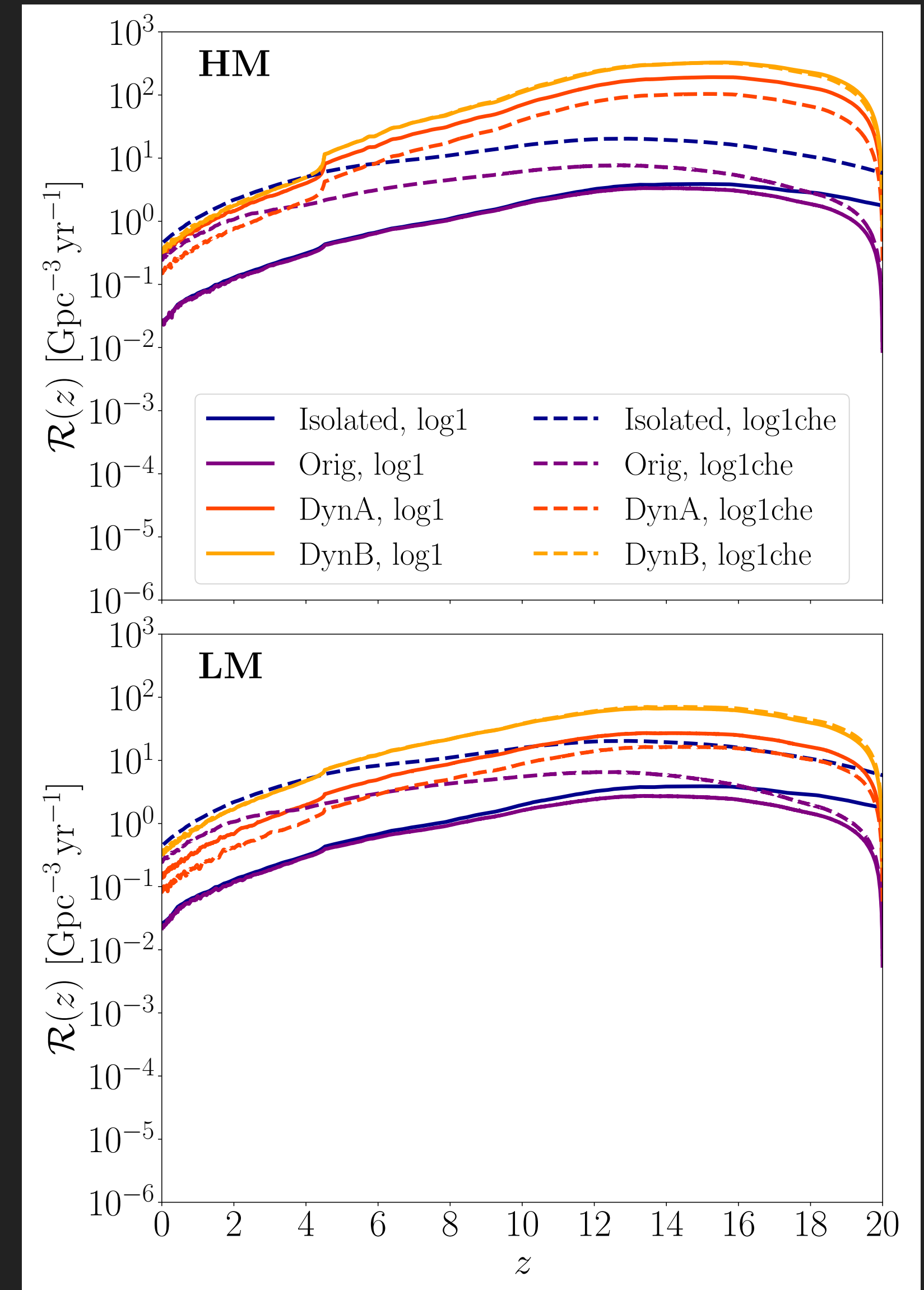
BACK-UP SLIDES

MASSIVE CLUSTERS: MERGER RATE DENSITY



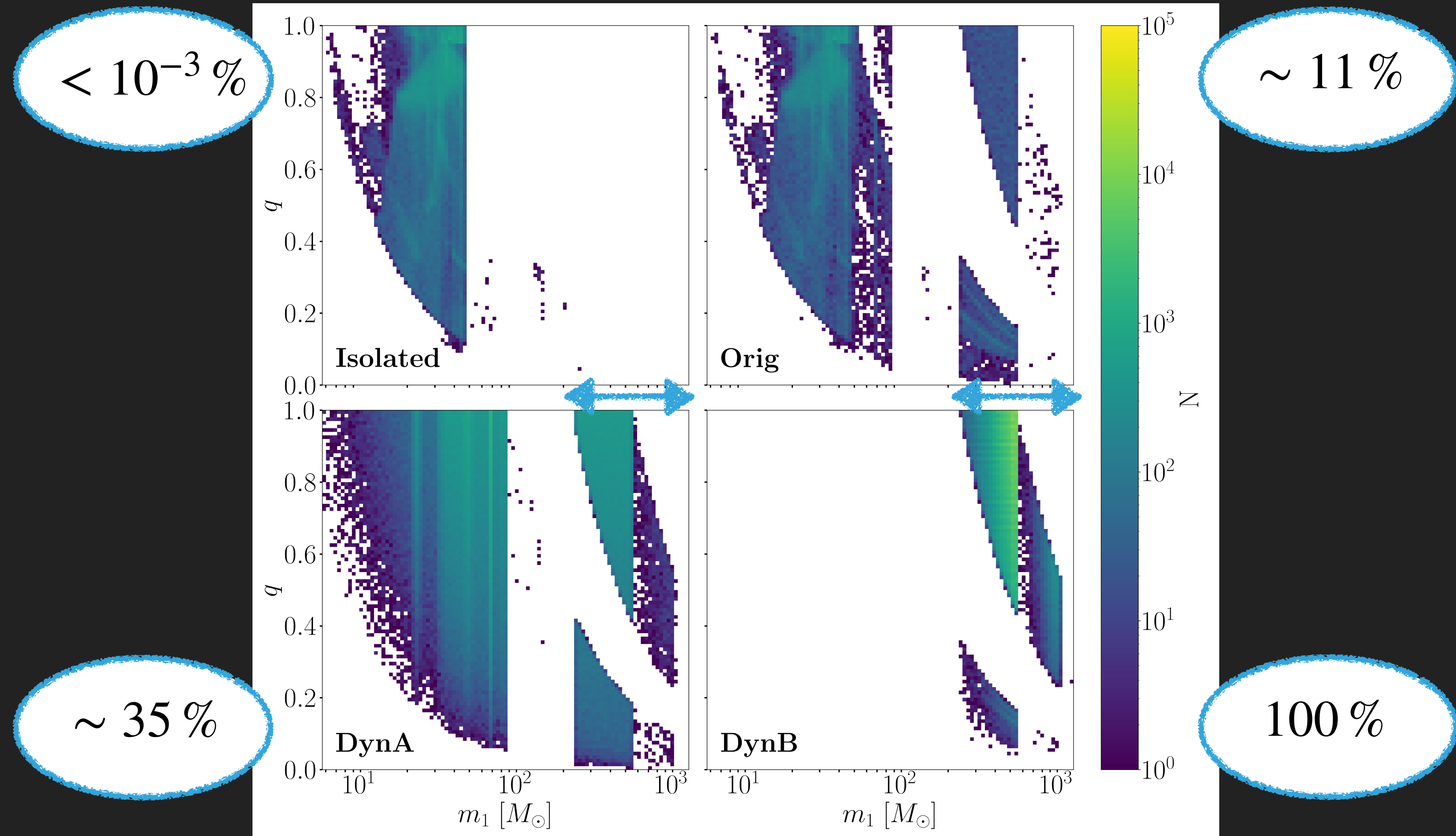
Santoliquido et al. 2020, 2021

- ▶ **MRD of dynamical BBHs two orders higher than original/isolated MRD**
- ▶ **MRD higher in HM clusters**
- ▶ **MRD of CHE BBHs higher**

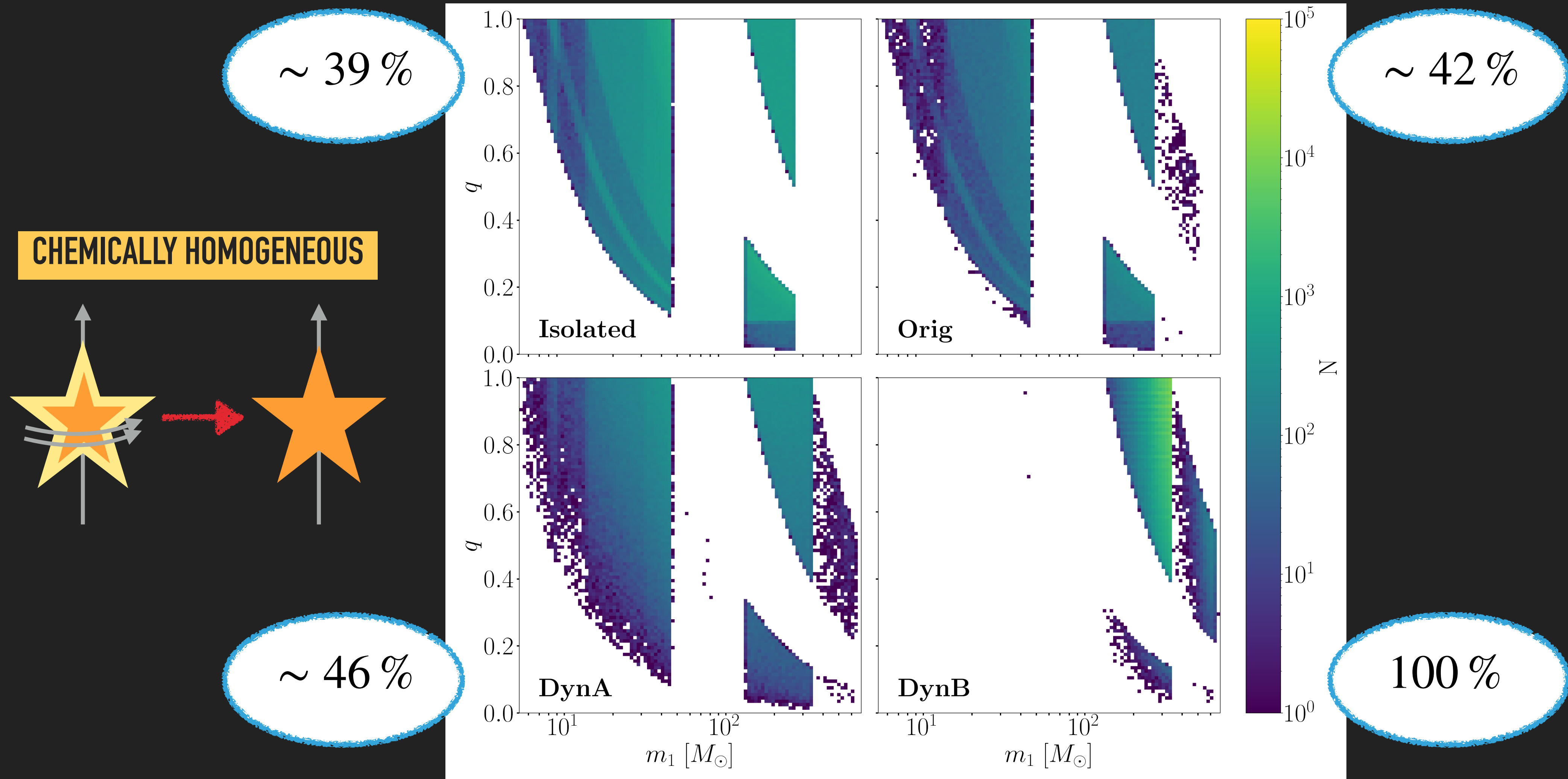


Mestichelli et al. 2024

THE BOOST ABOVE THE PAIR INSTABILITY MASS GAP



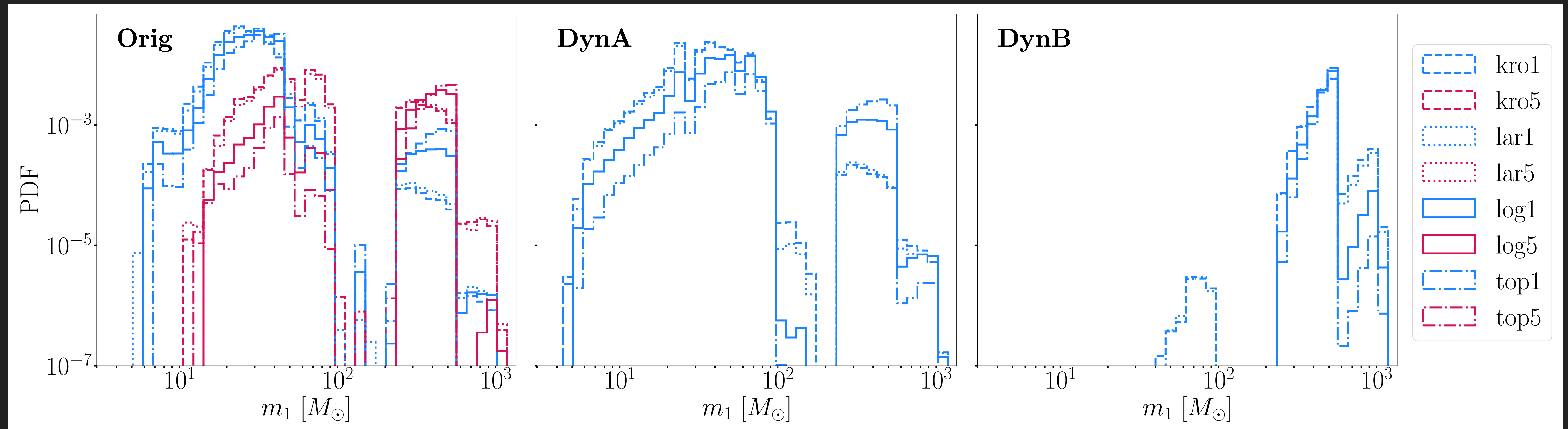
MASSIVE CLUSTERS: CHEMICAL HOMOGENEOUS STARS



MASSIVE CLUSTERS: DEPENDENCE ON INITIAL CONDITIONS

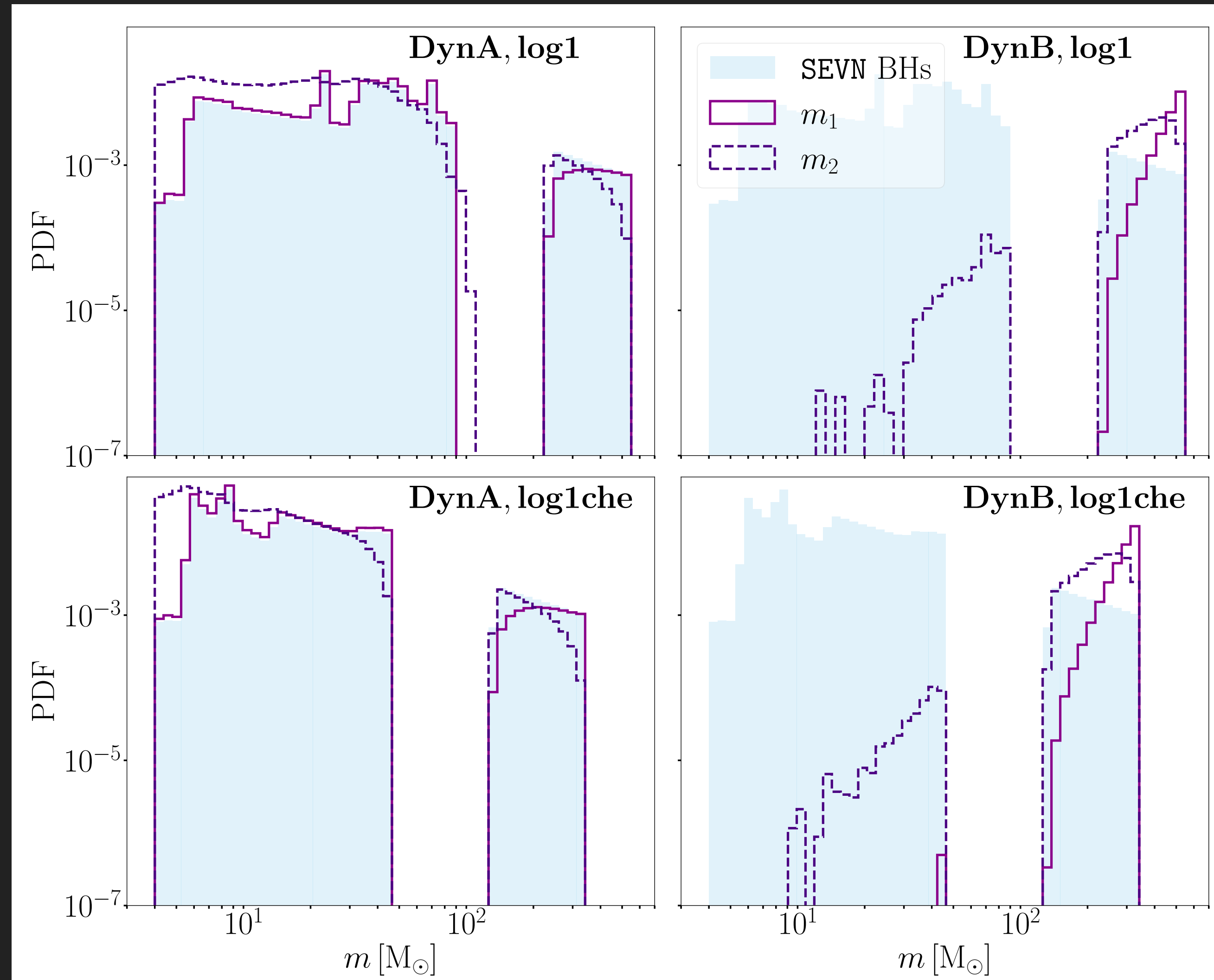
1 = SANA ET AL. 2012

5 = STACY & BROMM 2013



Mestichelli et al. 2024

DYNAMICAL BBHs: MASS SAMPLING FUNCTIONS



MERGER RATE DENSITY

$$\mathcal{R} = \int_{z_{\max}}^z \psi(z') \frac{dt(z')}{dz'} \left[\int_{Z_{\min}}^{Z_{\max}} \eta(Z) \mathcal{F}(z', z, Z) dZ \right] dz'$$

$\psi(z')$ → SFR density (Hartwig et al. 2022)
 $\frac{dt(z')}{dz'}$ → 1
 $\eta(Z)$ → Merger efficiency (different for orig and dyn)
 $\mathcal{F}(z', z, Z)$ → $f_{\text{CL}}(z', M_{\text{cl}}) \frac{\mathcal{N}(z', z, Z)}{\mathcal{N}_{\text{TOT}}(Z)} p(z', Z)$

$$H_0 (1 + z') [(1 + z')^3 \Omega_M + \Omega_\Lambda]^{1/2}$$

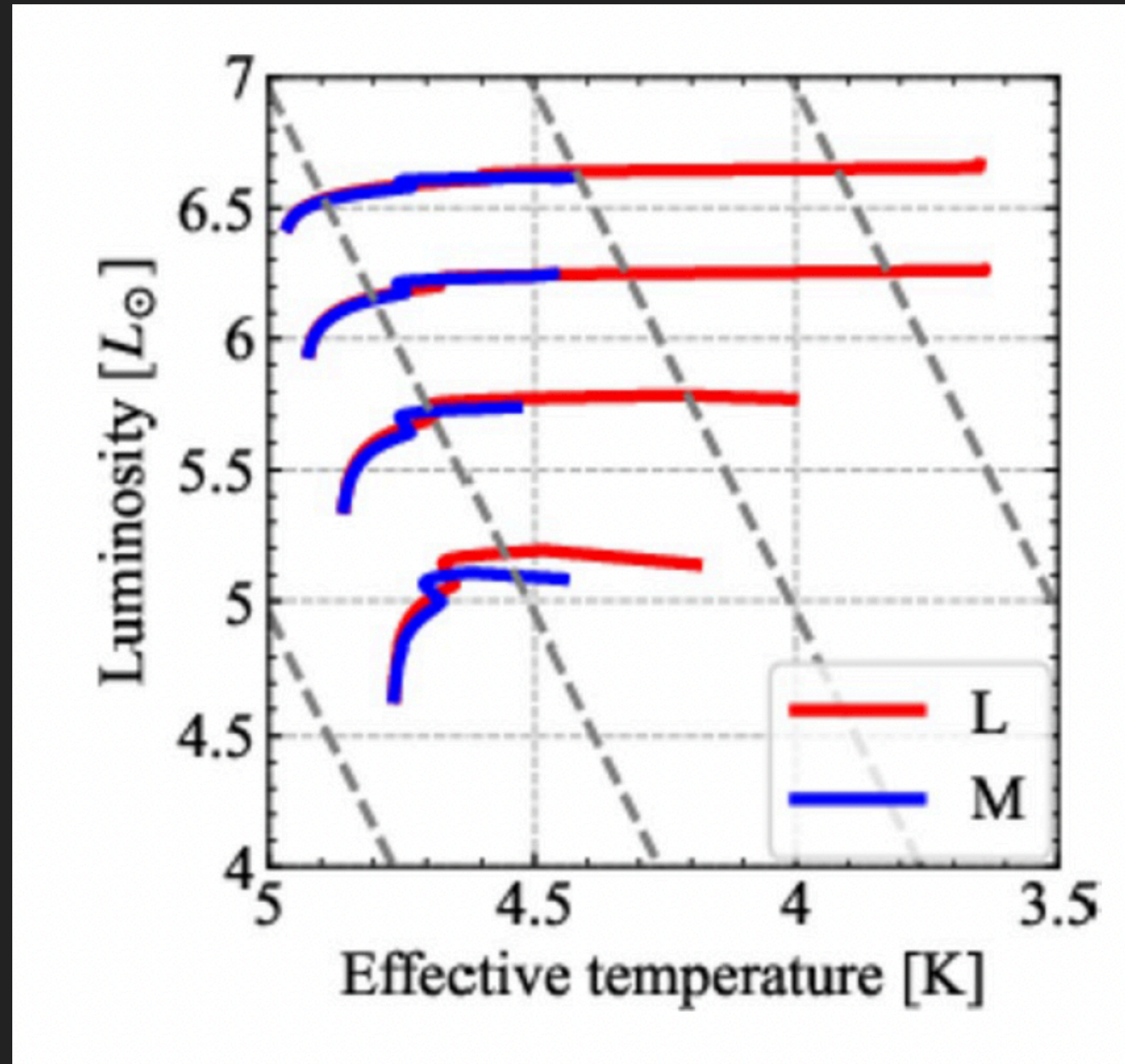


Santoliquido et al. 2020,
2021

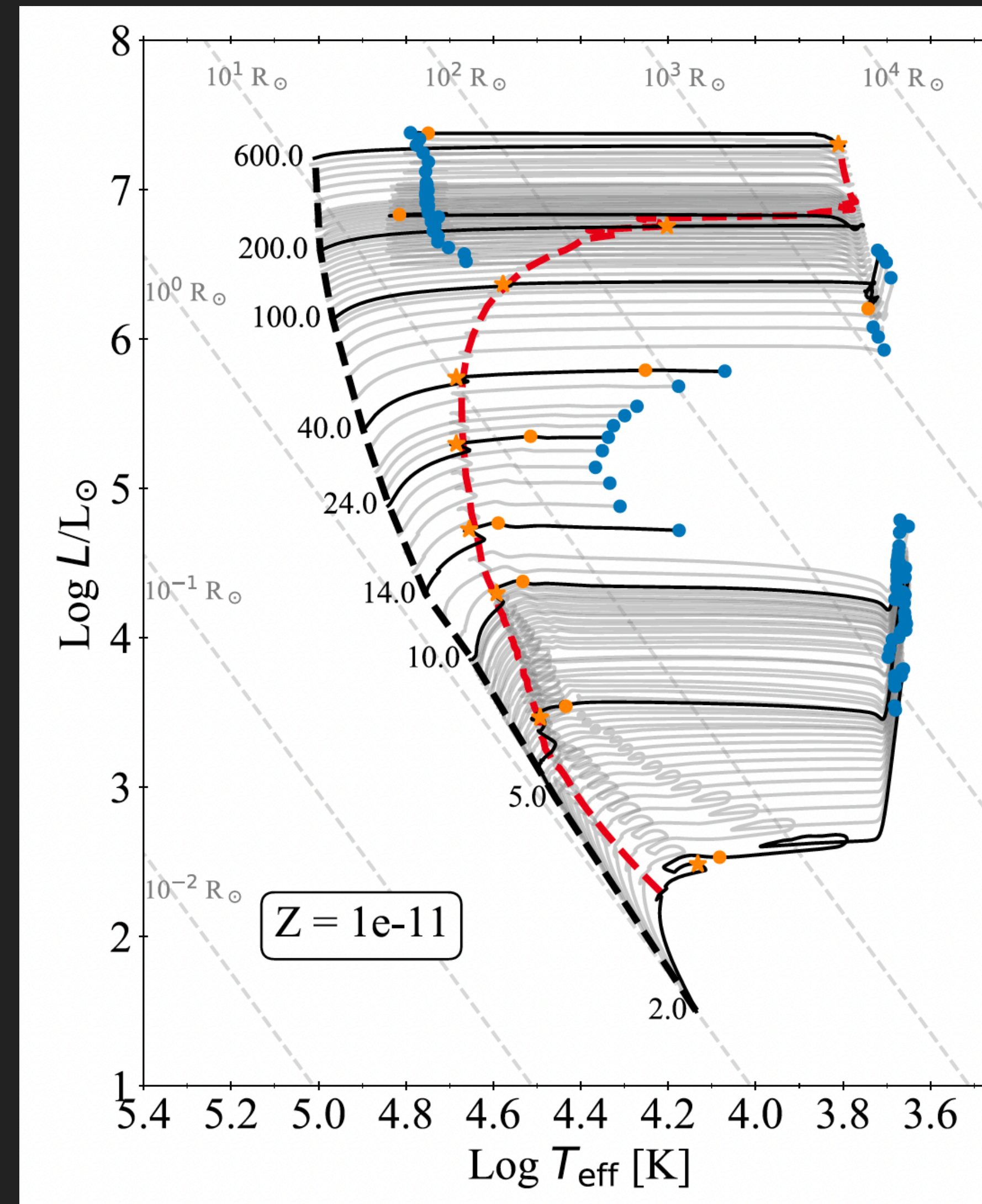
FASTCLUSTER: ORBITAL EVOLUTION

$$\begin{aligned}
 \frac{da}{dt} &= \underbrace{-2\pi\xi \frac{G\rho_c}{\sigma} a^2}_{\text{Dynamical hardening (Heggie 1976)}} - \underbrace{\frac{64}{5} \frac{G^3 m_1 m_2 (m_1 + m_2)}{c^5 a^3 (1 - e^2)^{7/2}} f_1(e)}_{\text{GW emission (Peters 1964)}} \\
 \frac{de}{dt} &= 2\pi\xi\kappa \frac{G\rho_c}{\sigma} a - \frac{304}{15} e \frac{G^3 m_1 m_2 (m_1 + m_2)}{c^5 a^4 (1 - e^2)^{5/2}} f_2(e)
 \end{aligned}$$

STELLAR TRACKS

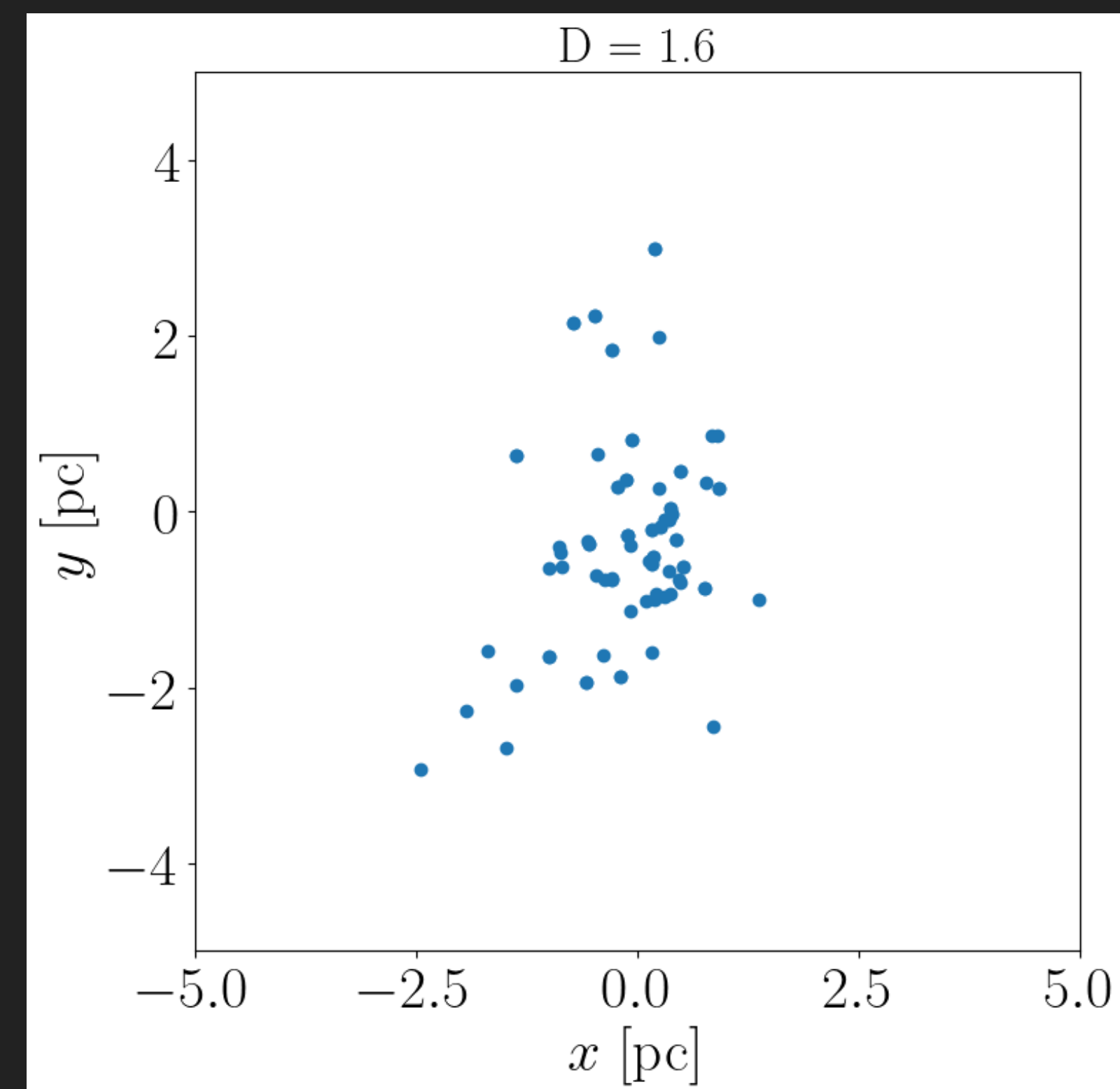
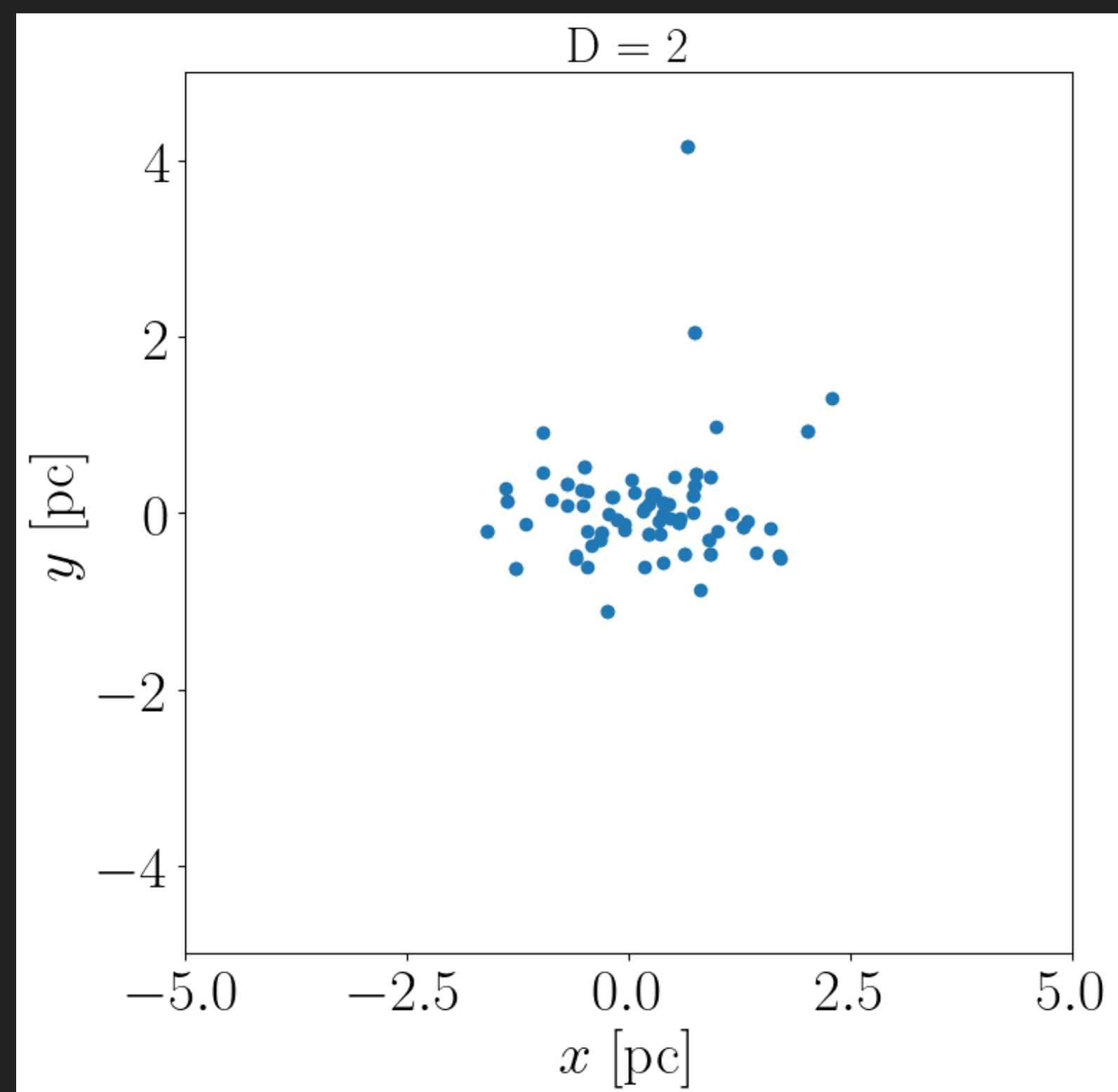
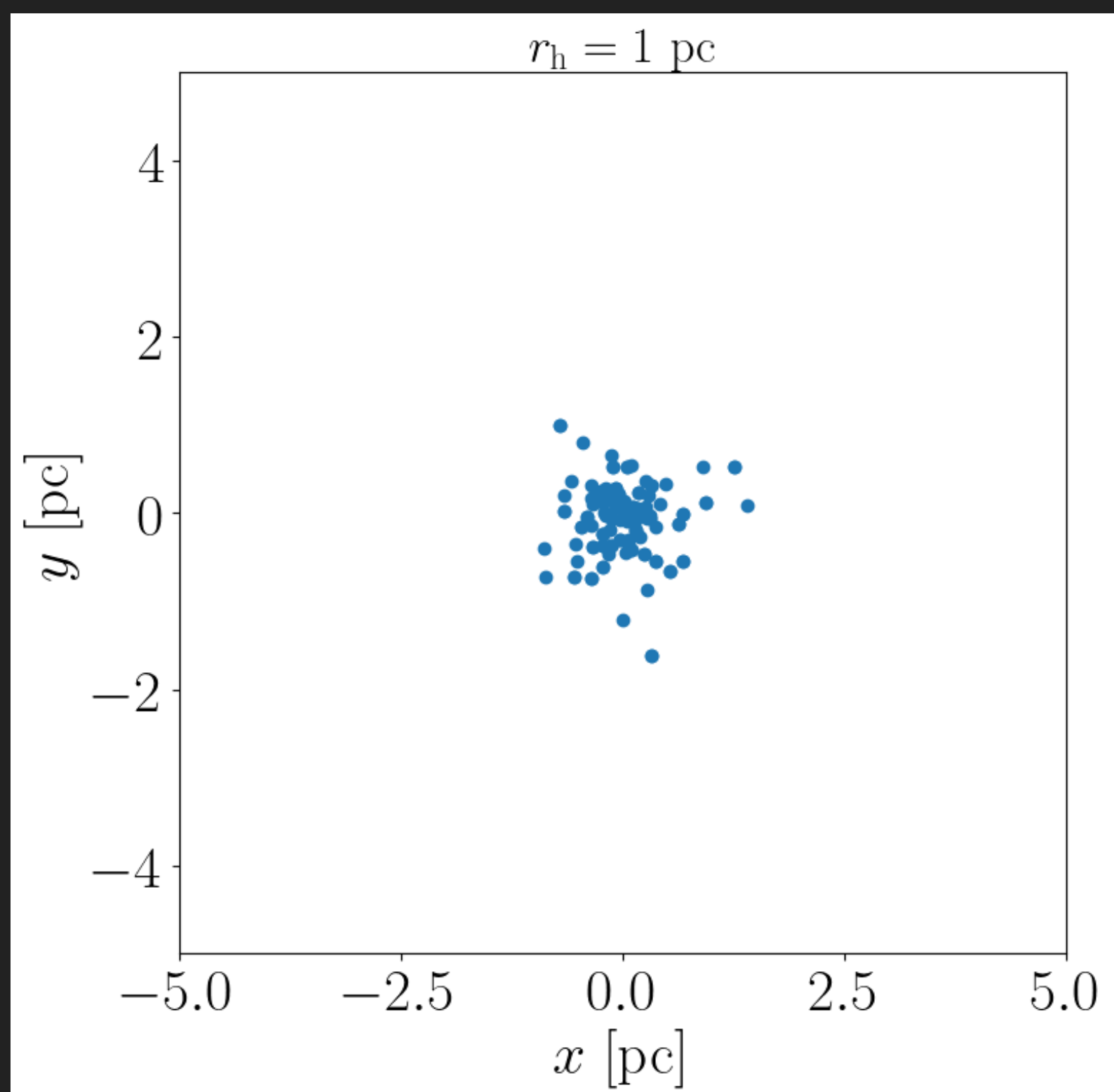


bseEMP; Tanikawa et al. 2020-2024



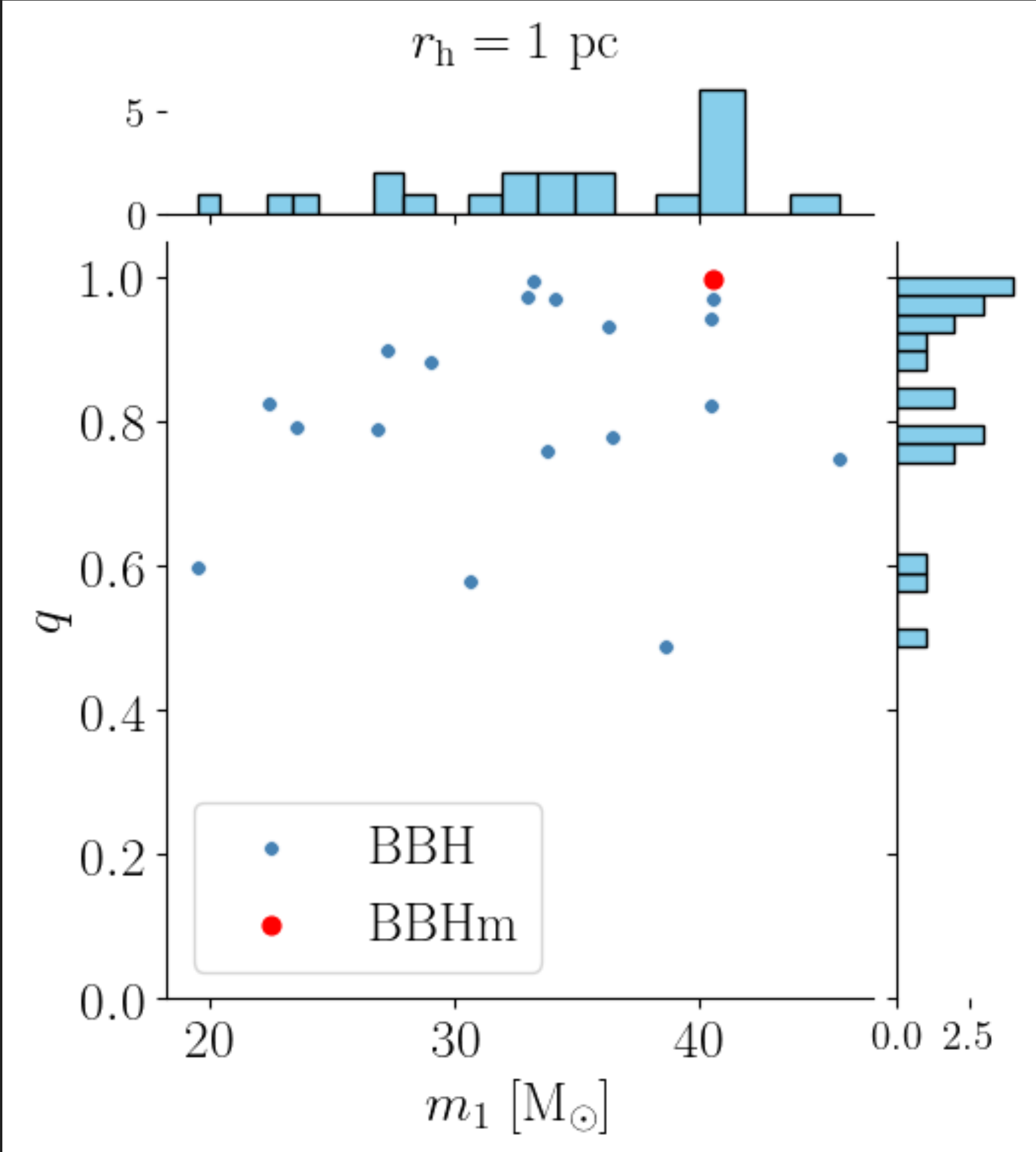
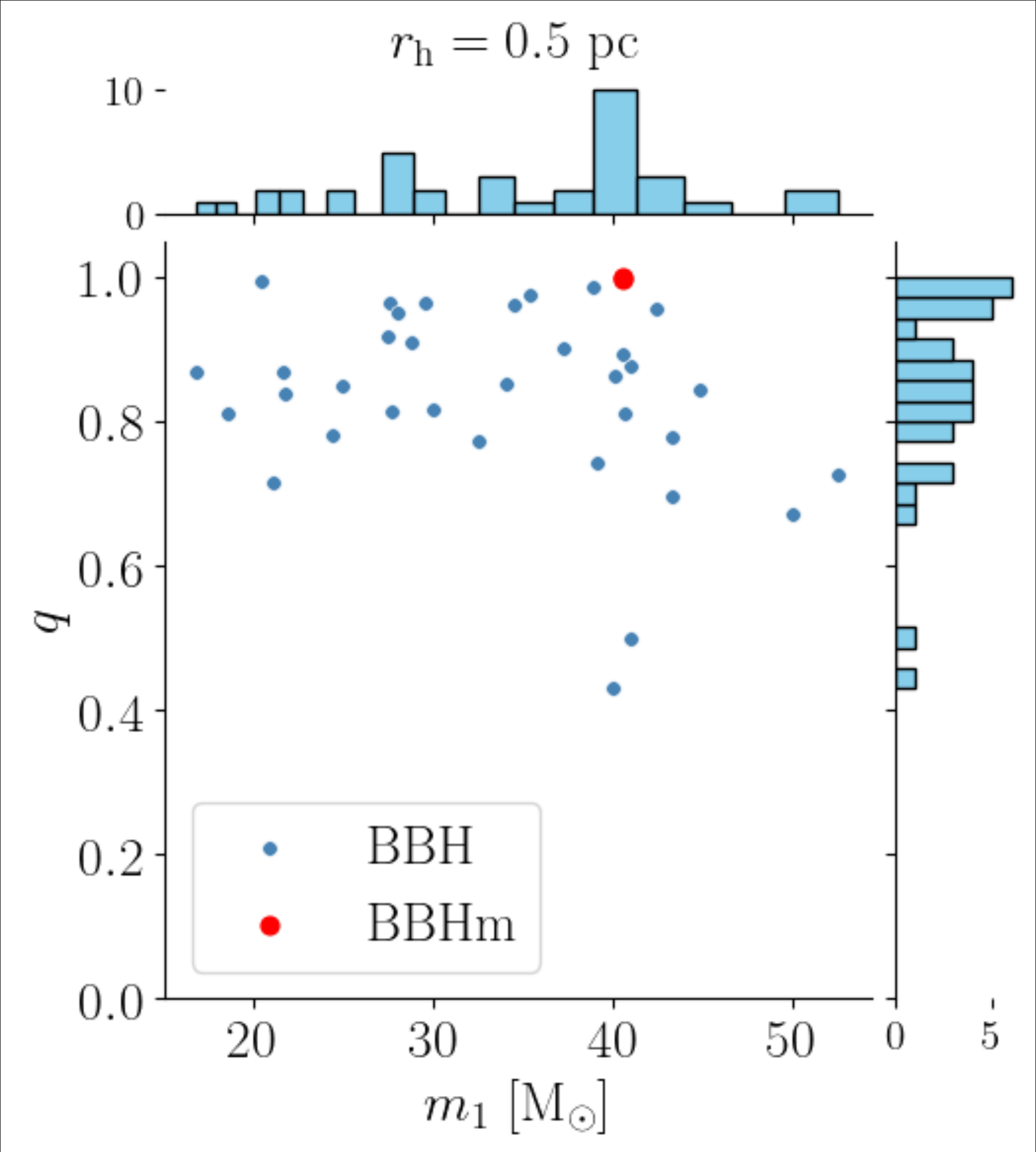
SEVN; Costa et al. 2023

INITIAL POSITIONS

PRELIMINARY

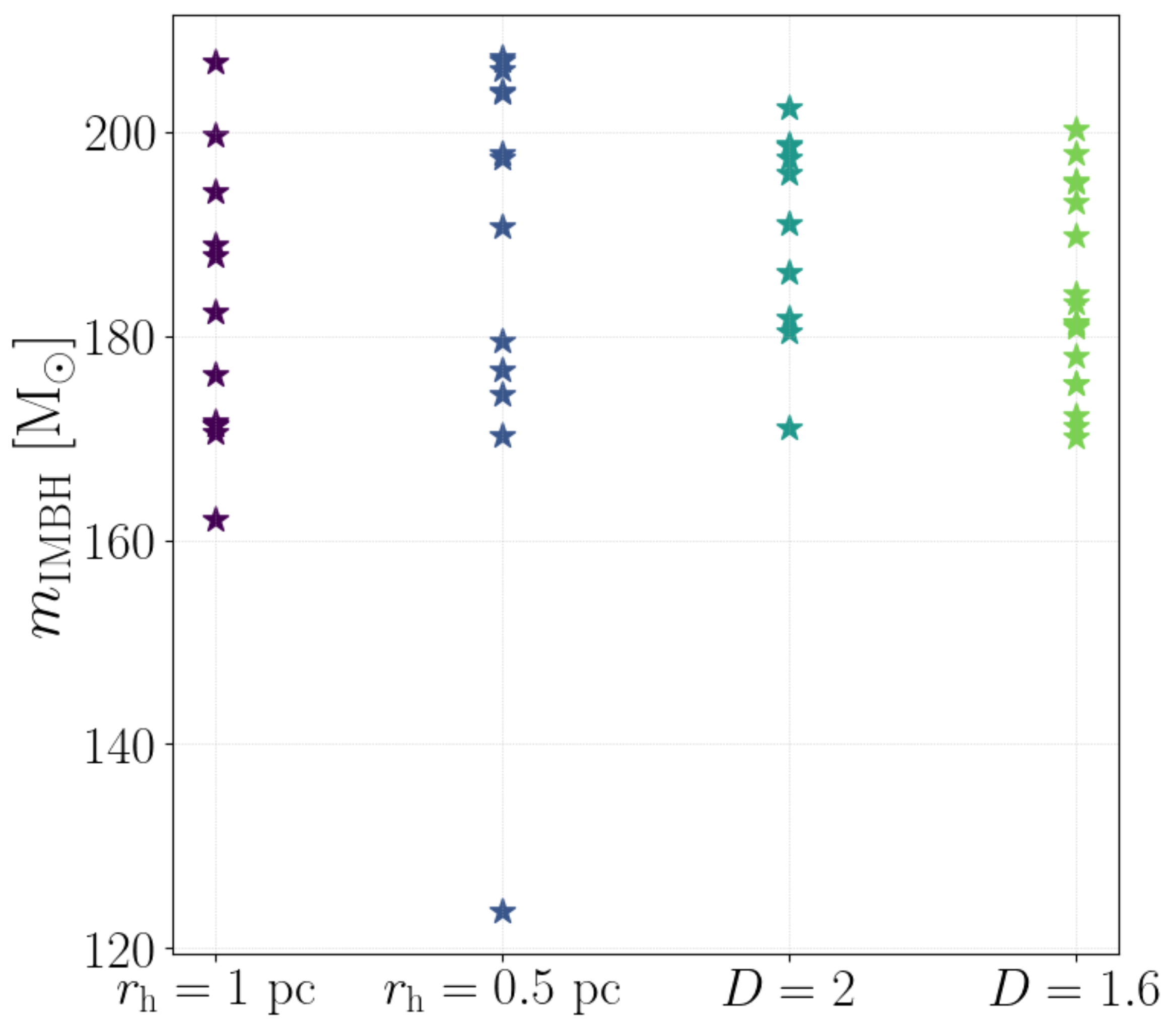
PRELIMINARY

BBH MASS SPECTRUM IN SMALL CLUSTERS

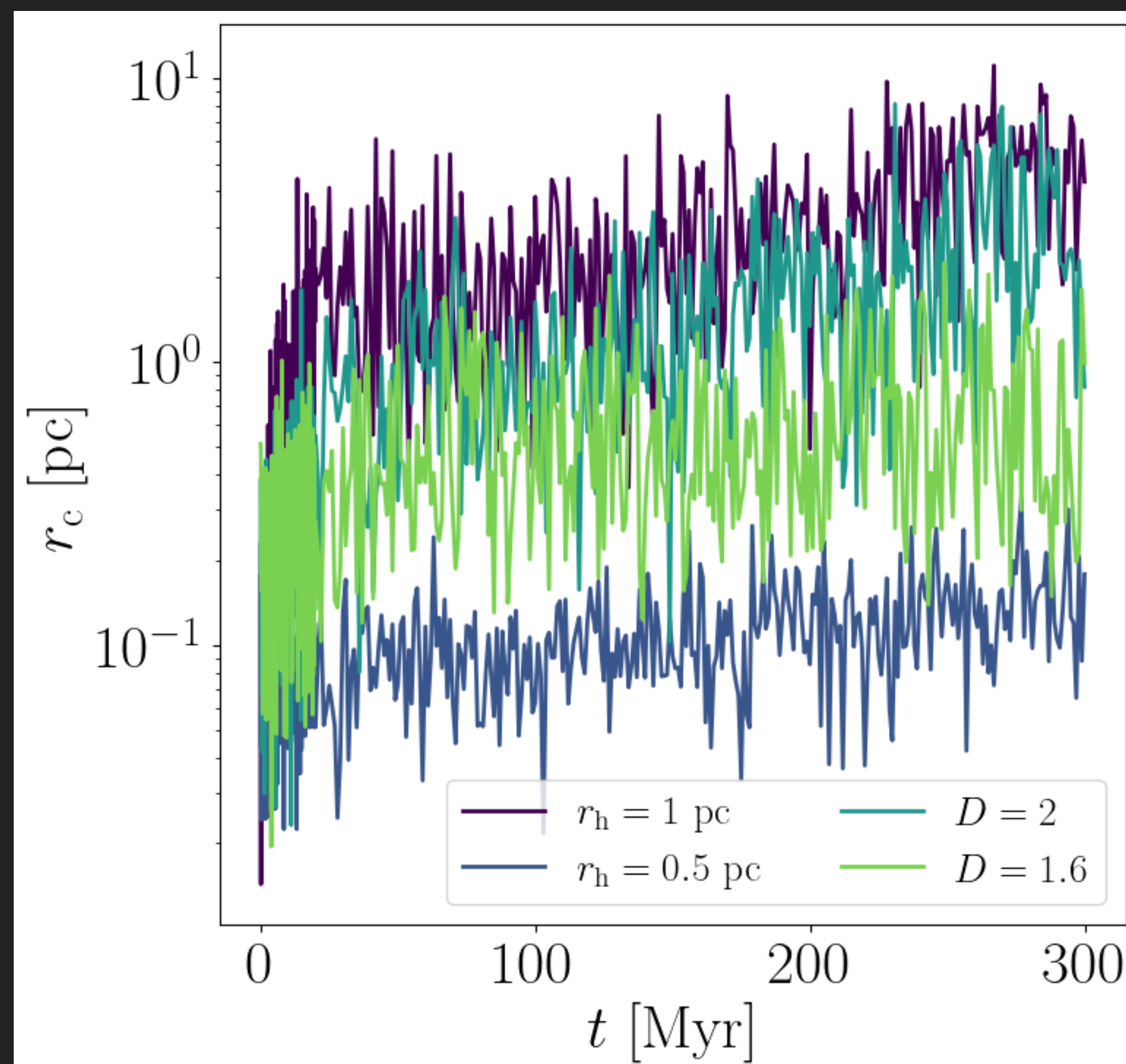
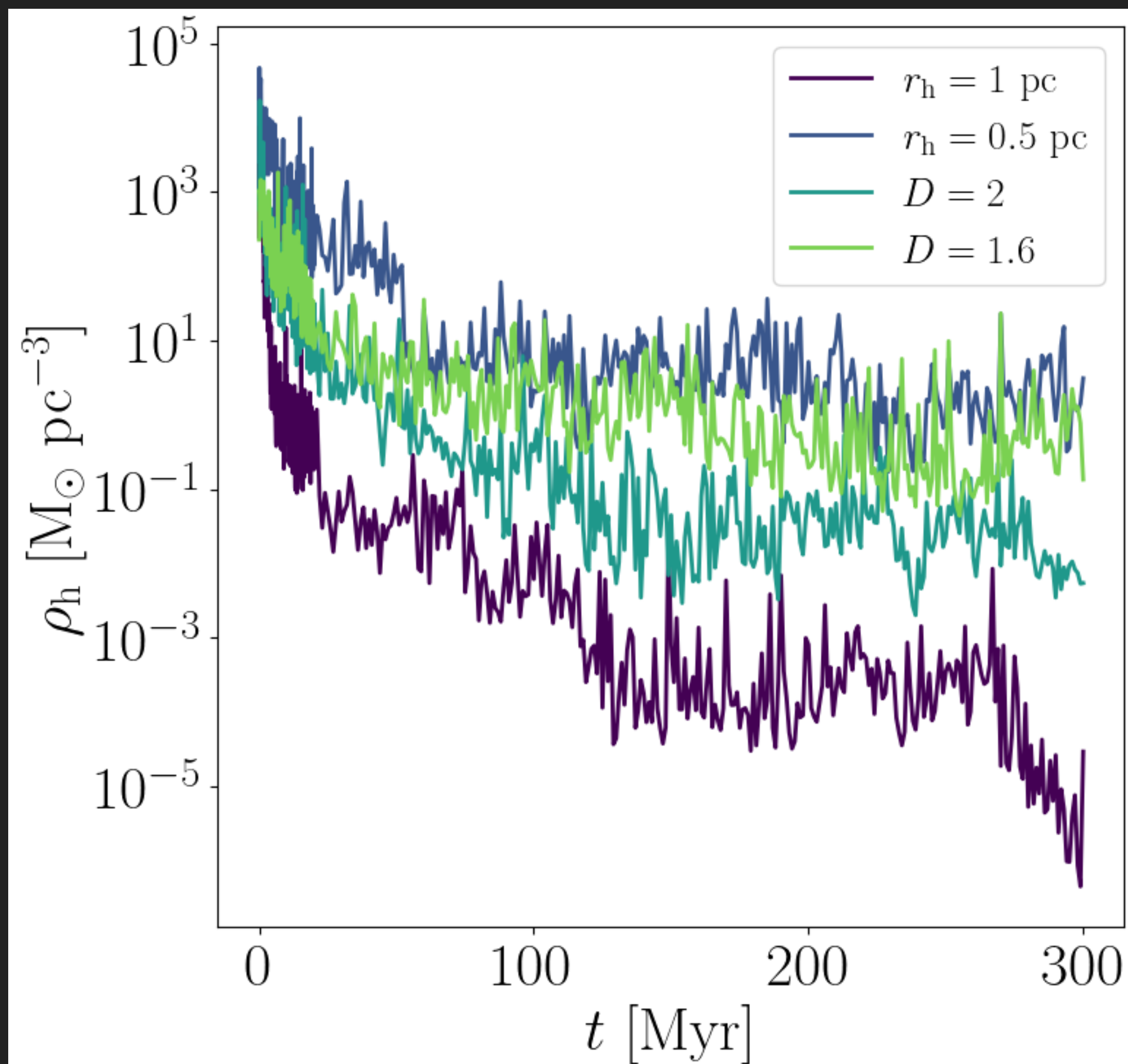


PRELIMINARY

INTERMEDIATE-MASS BLACK HOLES IN SMALL CLUSTERS



CLUSTER EVOLUTION

PRELIMINARY

WHAT'S NEXT: CLUSTER MERGERS

- ▶ **Up to 7 clusters** distributed according to **Plummer density profile** in **free fall**
- ▶ Which configuration leads to **higher merger efficiency**?
- ▶ Which configuration leads to **IMBH mergers**?

