

Divyajyoti
Stephen Fairhurst, Mark Hannam
Cardiff University



27th May, 2025

XV ET Symposium



Introduction

- BBH mergers can serve as standard sirens, offering an independent means to study cosmic expansion and star formation
- Current GW detectors can probe redshifts upto z ~ 1. Current observations suggest a redshift distribution which follows a power law
- Astrophysical models suggest a peak in the star formation rate between redshift of 1 < z < 3
- With future detectors like Cosmic Explorer and Einstein Telescope, we can probe the high redshift regime
- Mapping the z_peak:
 - Closely tied to the star formation rate and metallicity evolution
 - Test competing formation scenarios and astrophysical models



Methodology



BBH population

- Madau Dickinson redshift with time delay
- GWTC-3 mass distribution, precessing spins

Perform PE on detected events

- Fisher matrix analysis (GWBench)
- { $\log M_c$, η , ϕ_c , t_c , $\log D_L$, ι , α , δ , ψ }

Convert to multivariate gaussian

- {M_c, η, φ_c, t_c, D_L, ι, α, δ, ψ}
- Construct z posteriors for each event

Population analysis on z

- Redshift model: Madau Dickinson
- Hyperparameters: $\{\gamma, \kappa, z_{peak}\}$





Redshift distribution

• The Madau-Dickinson star-formation rate, and time delay distribution:

•
$$\psi(z) \propto rac{(1+z)^{\gamma}}{1+\left(rac{1+z}{1+z_{neak}}
ight)^{\kappa}}$$
 , $p(t_m|t_f, au) = rac{1}{ au}, t_m < au < t_f$

• The volumetric merger rate in the source-frame:

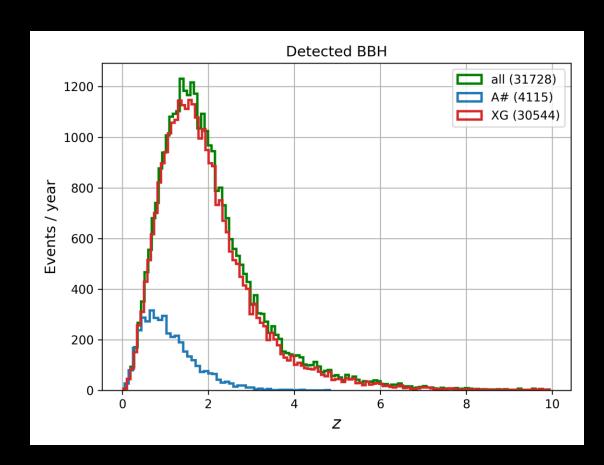
$${\cal R}_m(z_m) \propto \int_{z_m}^{\infty} dz_f rac{dt_f}{dz_f} \psi(z_f) p(t_m|t_f, au)$$

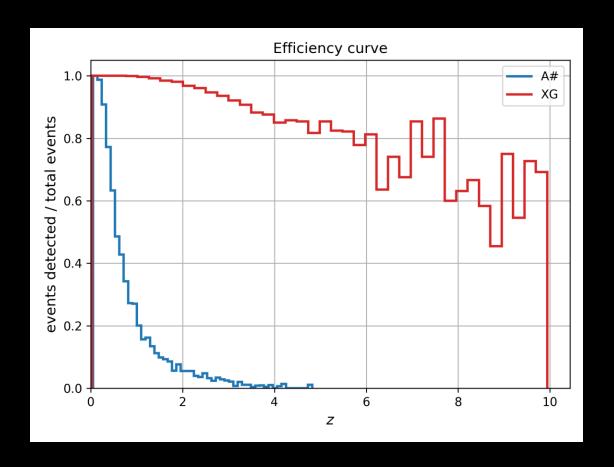
Redshift distribution:

$$p(z_m) \propto rac{dV_c}{dz} rac{1}{1+z} \mathcal{R}_m(z_m)$$



Input BBH population

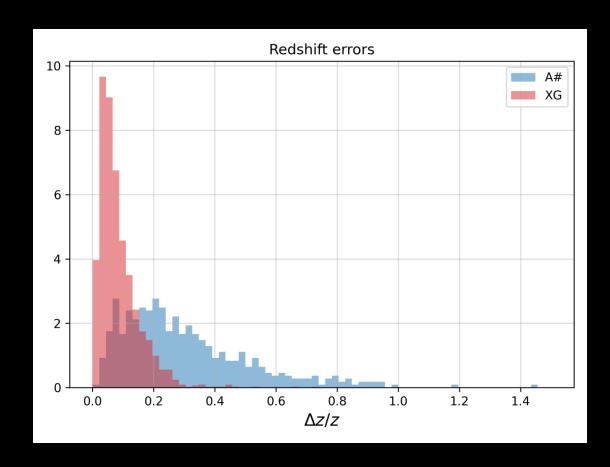


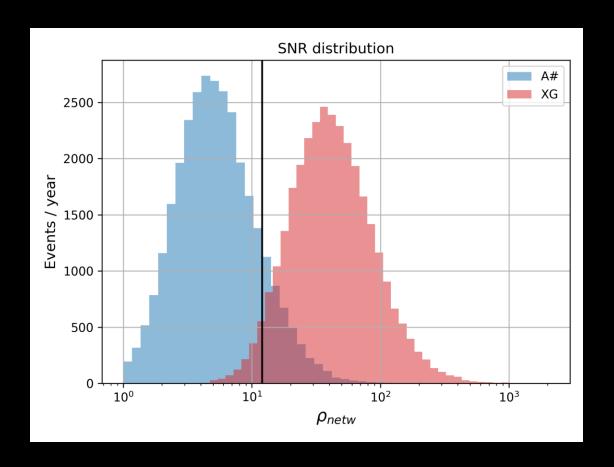


Detection criteria: SNR_{det} > 5 for two detectors, SNR_{netw} > 12 Networks: A#: L, H, I XG: CE40, CE20, ET (triangle)



Fisher Matrix analysis





FM analysis dimensions: $\{\log \mathcal{M}_c, \eta, \log D_L, \iota, t_c, \phi_c, \alpha, \delta, \psi\}$





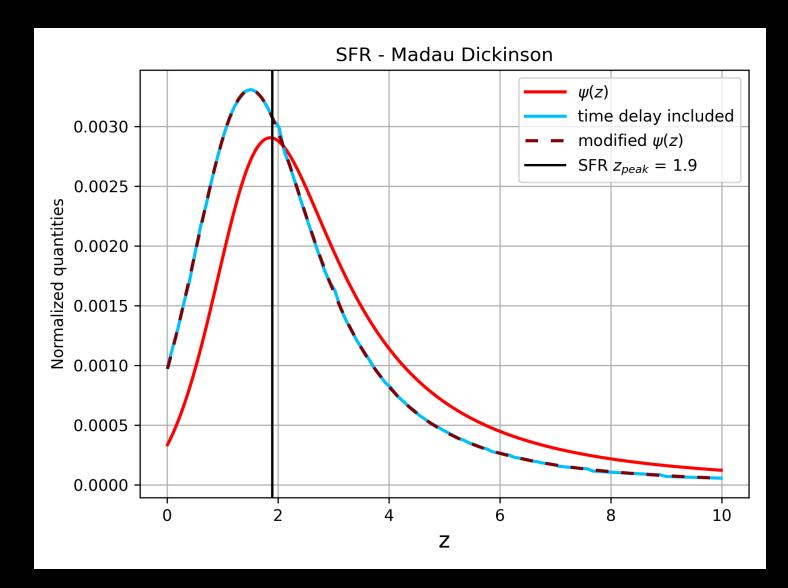
Fitting the redshift distribution

True parameters:

$$\gamma=2.7, \ \kappa=5.6,$$

$$\kappa = 5.6$$

$$z_{peak} = 1.9$$



Fitted parameters:

$$\gamma = 1.8032,$$

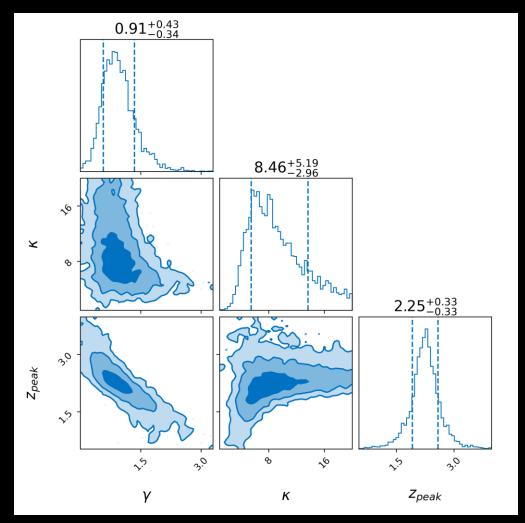
$$\kappa = 5.3023,$$

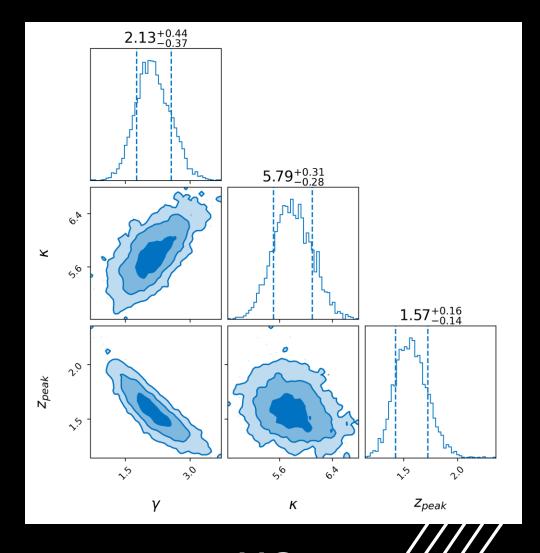
$$z_{peak} = 1.8362$$





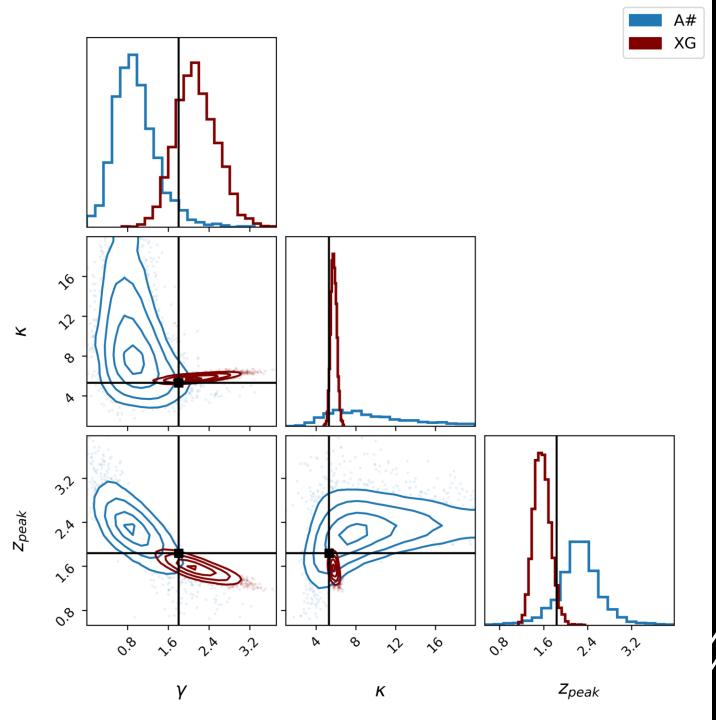
Population analysis results





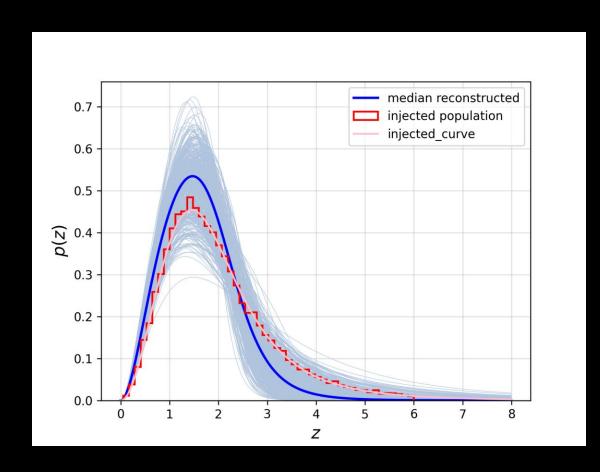


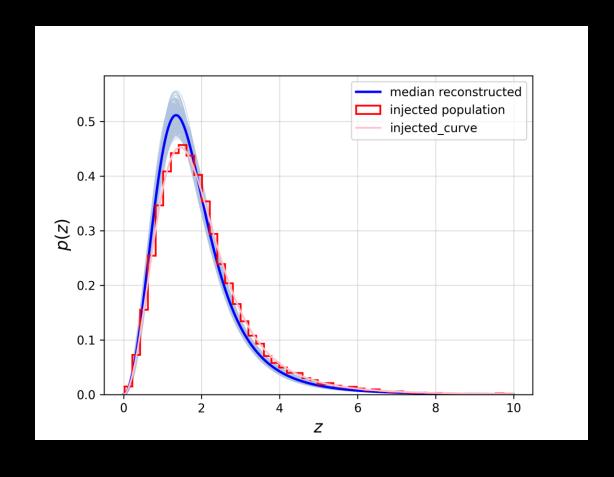
Population analysis results





Population analysis results





A#

XG



Summary and next steps

- A# and next generation detector network can probe the high redshift regime allowing us to look beyond the peak of the star formation
- Currently we analyzed 500 and 1500 events for A# and XG
 - Plan to include more events
- Study the curves for different mass ranges
- Include efficiency factor due to metallicity in the merger rate

